The Name of the Title Is Hope

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ABSTRACT

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CCS CONCEPTS

• **Theory of computation** → **Cryptographic primitives**.

KEYWORDS

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1 INTRODUCTION

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2 PRELIMINARY

2.1 Basic Notations

Point and multi-point functions. Given a domain size N and Abelian group $\mathbb{G}$, a *point function* $f_{\alpha,\beta} : [N] \to \mathbb{G}$ for $\alpha \in [N]$ and $\beta \in \mathbb{G}$ evaluates to β on input α and to $0 \in \mathbb{G}$ on all other inputs. We denote by $\hat{f}_{\alpha,\beta} = (N, \hat{\mathbb{G}}, \alpha, \beta)$ the representation of such a point function.

Enote: MPF. Also representation of groups.

2.2 Distributed Multi-Point Functions

Enote: should directly adapt to multi-point function case

We begin by defining a slightly generalized notion of distributed point functions (DPFs), which accounts for the extra parameter $\mathbb{G}'$.

Definition 1 (DPF [1, 3]). *A (2-party)* distributed point function (DPF) *is a triple of algorithms* $\Pi = (\mathsf{Gen}, \mathsf{Eval}_0, \mathsf{Eval}_1)$ *with the following syntax:*

- $\mathsf{Gen}(1^\lambda, \hat{f}_{\alpha,\beta}) \to (k_0, k_1)$*: On input security parameter* $\lambda \in \mathbb{N}$ *and point function description* $\hat{f}_{\alpha,\beta} = (N, \hat{\mathbb{G}}, \alpha, \beta)$*, the (randomized) key generation algorithm* Gen *returns a pair of keys* $k_0, k_1 \in \{0,1\}^*$*. We assume that* N *and* $\mathbb{G}$ *are determined by each key.*
- $\mathsf{Eval}_i(k_i, x) \to y_i$*: On input key* $k_i \in \{0,1\}^*$ *and input* $x \in [N]$ *the (deterministic) evaluation algorithm of server* i, Eval_i *returns* $y_i \in \mathbb{G}$.

We require Π *to satisfy the following requirements:*

- ***Correctness:*** *For every* λ, $\hat{f} = \hat{f}_{\alpha,\beta} = (N, \hat{\mathbb{G}}, \alpha, \beta)$ *such that* $\beta \in \mathbb{G}$*, and* $x \in [N]$*, if* $(k_0, k_1) \leftarrow \mathsf{Gen}(1^\lambda, \hat{f})$*, then*

$$\Pr\left[\sum_{i=0}^{1} \mathsf{Eval}_i(k_i, x) = f_{\alpha,\beta}(x)\right] = 1$$

- ***Security:*** *Consider the following semantic security challenge experiment for corrupted server* $i \in \{0,1\}$*:*
  1. *The adversary produces two point function descriptions* $(\hat{f}^0 = (N, \hat{\mathbb{G}}, \alpha_0, \beta_0), \hat{f}^1 = (N, \hat{\mathbb{G}}, \alpha_1, \beta_1)) \leftarrow \mathcal{A}(1^\lambda)$*, where* $\alpha_i \in [N]$ *and* $\beta_i \in \mathbb{G}$.
  2. *The challenger samples* $b \leftarrow \{0,1\}$ *and* $(k_0, k_1) \leftarrow \mathsf{Gen}(1^\lambda, \hat{f}^b)$.
  3. *The adversary outputs a guess* $b' \leftarrow \mathcal{A}(k_i)$.

  Denote by $\mathsf{Adv}(1^\lambda, \mathcal{A}, i) = \Pr[b = b'] - 1/2$ *the advantage of* $\mathcal{A}$ *in guessing* b *in the above experiment. For every non-uniform polynomial time adversary* $\mathcal{A}$ *there exists a negligible function* ν *such that* $\mathsf{Adv}(1^\lambda, \mathcal{A}, i) \le \nu(\lambda)$ *for all* $\lambda \in \mathbb{N}$.

We will also be interested in applying the evaluation algorithm on *all* inputs. Given a DPF $(\mathsf{Gen}, \mathsf{Eval}_0, \mathsf{Eval}_1)$, we denote by $\mathsf{FullEval}_i$ an algorithm which computes Eval_i on every input x. Hence, $\mathsf{FullEval}_i$ receives only a key k_i as input.

2.3 Batch Codes

combinatorial/probabilistic batch codes, with cuckoo hashing a concrete instantiation

2.4 Oblivious Key-Value Stores

Definition 2 (OKVS[2, 4]). *An Oblivious Key-Value Stores (OKVS) scheme is a pair of randomized algorithms* $(\mathsf{Encode}_r, \mathsf{Decode}_r)$ *with respect to a statistical security parameter* λ_{stat} *and a computational security parameter* λ*, a randomness space* $\{0,1\}^\kappa$*, a key space* $\mathcal{K}$*, a value space* $\mathcal{V}$*, input length n and output length m. The algorithms are of the following syntax:*

- $\mathsf{Encode}_r(\{(k_1, v_1), (k_2, v_2), \cdots, (k_n, v_n)\}) \to P$*: On input* n *key-value pairs with distinct keys, the encode algorithm with randomness* r *in the randomness space outputs an encoding* $P \in \mathcal{V}^m \cup \perp$.
- $\mathsf{Decode}_r(P, k) \to v$*: On input a (nonempty) encoding from* $\mathcal{V}^m$ *and a key* $k \in \mathcal{K}$*, output a value* v.

We require the scheme to satisfy

- ***Correctness:*** *For every* $S \in (\mathcal{K} \times \mathcal{V})^n$, $\Pr_{r \leftarrow \{0,1\}^\kappa}[\mathsf{Encode}_r(S) = \perp] \le 2^{-\lambda_{\mathsf{stat}}}$.
- ***Obliviousness:*** *For any distinct key sets* $\{k_1^0, k_2^0, \cdots, k_n^0\}$ *and* $\{k_1^1, k_2^1, \cdots, k_n^1\}$ *that are different, if they are paired with random values then their encodings are computationally indistinguishable, i.e.,*

$$\{r, \mathsf{Encode}_r(\{(k_1^0, v_1), \cdots, (k_n^0, v_n)\})\}_{v_1,\cdots,v_n \leftarrow \mathcal{V}, r \leftarrow \{0,1\}^\kappa}$$
$$\approx_c \{r, \mathsf{Encode}_r(\{(k_1^1, v_1), \cdots, (k_n^1, v_n)\})\}_{v_1,\cdots,v_n \leftarrow \mathcal{V}, r \leftarrow \{0,1\}^\kappa}$$

concrete instantiations(polynomial, sparse matrix). mention some connections to cuckoo hashing

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3 NEW DMPF CONSTRUCTIONS

3.1 Big-State DMPF

display the big-state DMPF (plus distributed gen)

3.2 Batch-Code DMPF

display the batch-code DMPF

3.3 OKVS-based DMPF

display the OKVS-based DMPF (plus distributed gen)

3.4 Comparison

Comparison table dependent to PRG & F-MUL(list the formulas?)
analyze tradeoff
distributed gen advantage

4 APPLICATIONS

4.1 PCG for OLE from Ring-LPN

Characterize parameters
show nonregular optimization
plug in new DMPF and show overall optimization

4.2 PSI-WCA

plug in new DMPF and analyze advantage interval
plug in distributed gen

4.3 Heavy-hitters

private heavy-hitter
or parallel ORAM?

5 ACKNOWLEDGMENTS

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A BATCH-CODE DMPF SCHEME

B SECURITY PROOFS