

Problem Solving

Codility and Leetcode Practitioner

Problem

Where love begins



Problems

Description:

Write a function `fib(n)` that takes in a number as an argument and return the n-th number of the Fibonacci sequence.

Example:

- `fib(1)` is 1
- `fib(2)` is 1
- `fib(3)` is 2
- `fib(4)` is 3
- `fib(n)` is `fib(n-1)+fib(n-2)`

Brute-force

Costly but work

```
public long fib(int n) {  
    if (n <= 2) return 1;  
  
    return fib(n-1) + fib(n-2);  
}
```

Use stack memory
Limited size (1-8Mb)

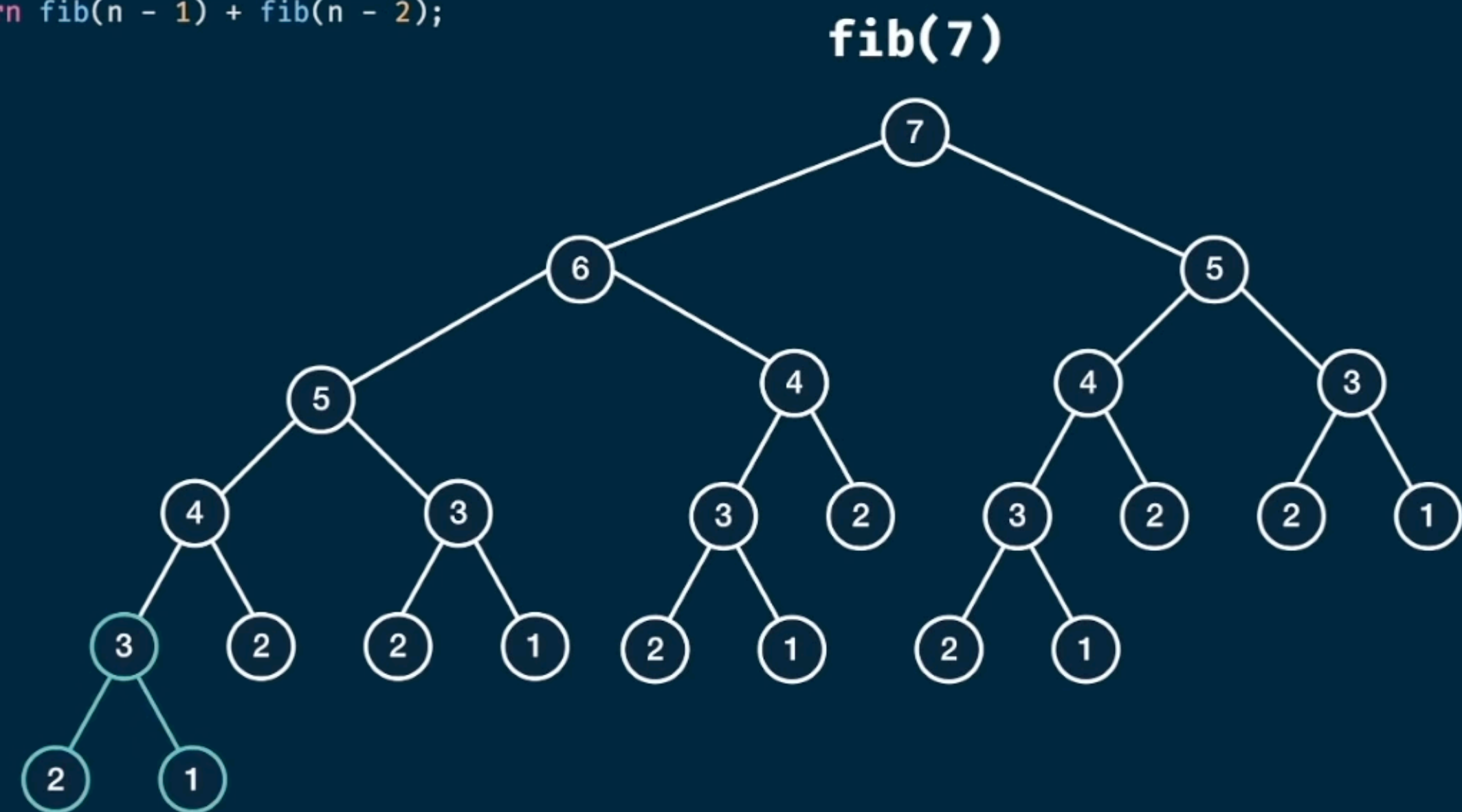
```
public long fibWithoutRecursion(int n) {  
    if (n <= 2) return 1;  
  
    Stack<Integer> stack = new Stack<>();  
    long result = 0;  
  
    stack.push(n);  
  
    while (!stack.isEmpty()) {  
        int current = stack.pop();  
  
        if (current <= 2) {  
            result += 1;  
        } else {  
            // Push both subproblems to stack  
            stack.push(current - 1);  
            stack.push(current - 2);  
        }  
    }  
  
    return result;  
}
```

Use Heap memory
Much larger than stack

Brute-force

Costly but work

```
1 const fib = (n) => {  
2   if (n <= 2) return 1;  
3   return fib(n - 1) + fib(n - 2);  
4 };
```



$O(2^N)$

Memoization

Remove duplicate by Caching

```
public long fib(int n) { 2 usages new *
    if (n <= 2) return 1L;

    return fib(n - 1) + fib(n - 2);
}

public long fibWithMem(int n, Map<Integer, Long> mem) { 2 usages new *
    if (mem.containsKey(n)) {
        return mem.get(n);
    }

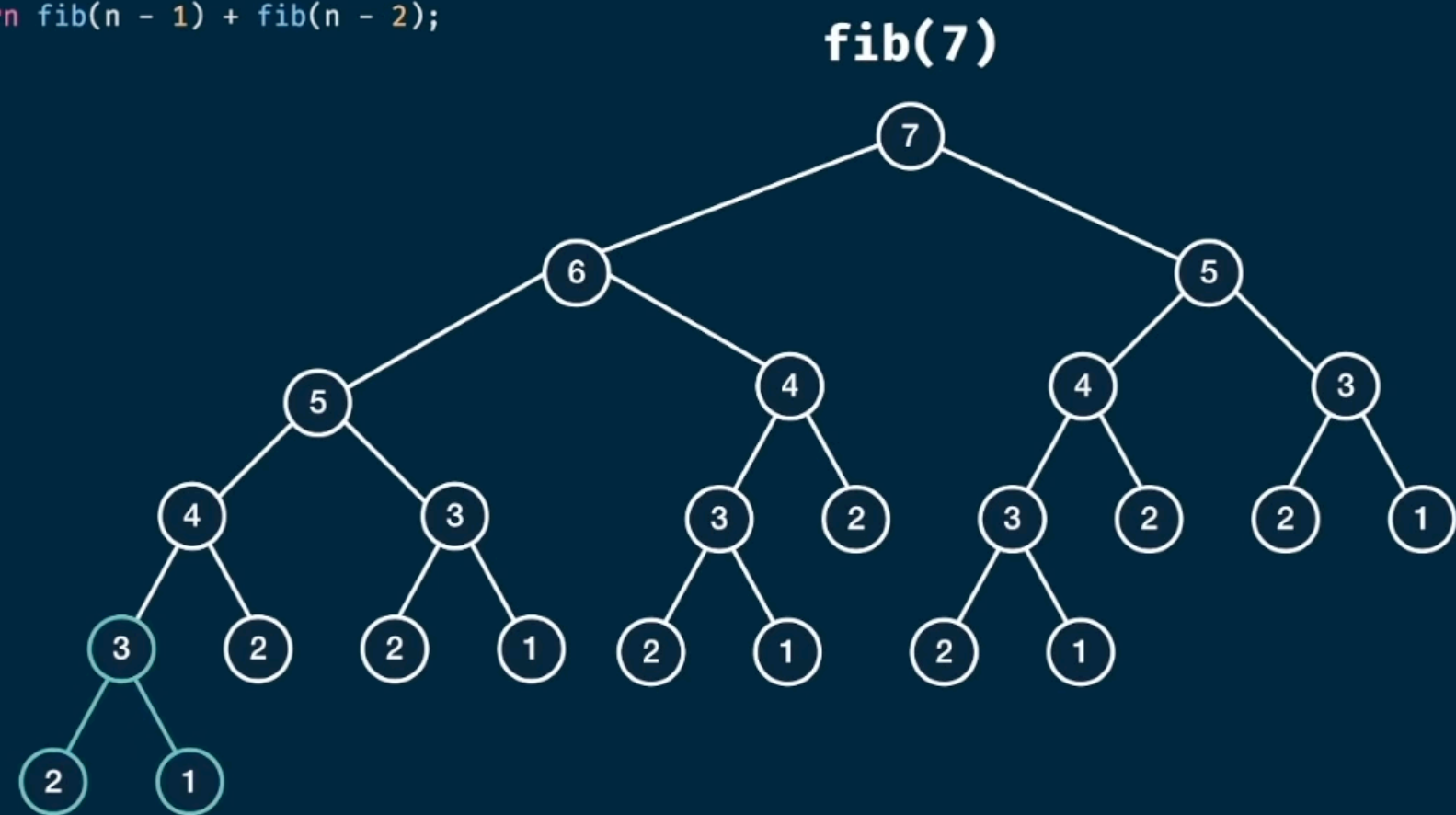
    if (n <= 2) {
        mem.put(n, 1L);
        return 1L;
    }

    long result = fibWithMem(n - 1, mem) + fibWithMem(n - 2, mem);
    mem.put(n, result);

    return result;
}
```

Brute-force (2^N)

```
1 const fib = (n) => {  
2   if (n <= 2) return 1;  
3   return fib(n - 1) + fib(n - 2);  
4 };
```



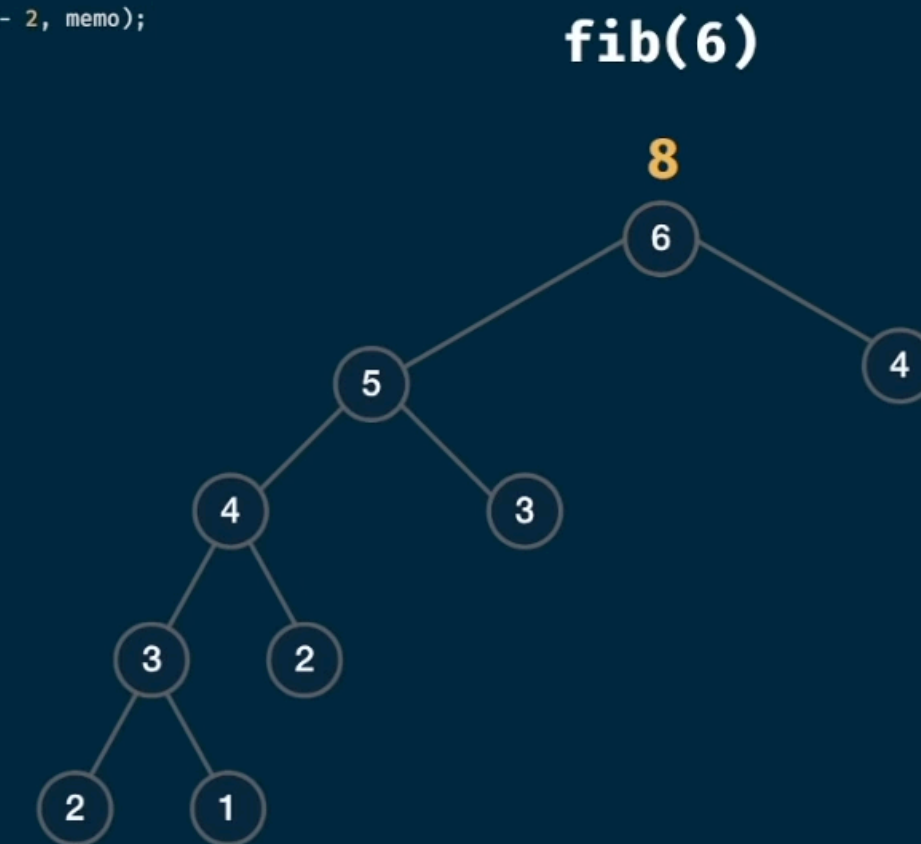
$O(2^N)$

Memoization ($2N$)

```
1 const fib = (n, memo = {}) => {  
2   if (n in memo) return memo[n];  
3   if (n <= 2) return 1;  
4  
5   memo[n] = fib(n - 1, memo) + fib(n - 2, memo);  
6   return memo[n];  
7 };
```

memo

```
{  
  3: 2,  
  4: 3,  
  5: 5,  
  6: 8  
}
```



$O(2N) \sim O(N)$

Thank you

Don't give up