

CS143 Midterm

Spring 2020

- Please read all instructions (including these) carefully.
- There are 5 questions on the exam, some with multiple parts. You have 95 minutes to both finish the exam and upload it. After 95 minutes, gradescope will close your exam and automatically submit it, so make sure submit what you have by then.
- The exam is open note. You may use laptops, phones, e-readers, and the internet, but you may not consult anyone.
- You must upload the answer to each question as an image file or a PDF. You may submit images of hand-written answers taken with your phone (but allow yourself time to send the image to your computer, so you can upload it to gradescope). It is your responsibility, however, to ensure they are legible. Computer typed answers as a PDF are also permitted.
- Solutions will be graded on correctness and clarity. Each problem has a relatively simple and straightforward solution. You may get as few as 0 points for a question if your solution is far more complicated than necessary. Partial solutions will be graded for partial credit.

Problem	Max points	Points
1	20	
2	15	
3	15	
4	25	
5	25	
TOTAL	100	

In accordance with both the letter and spirit of the Honor Code, I have neither given nor received assistance on this examination.

Type your name as a signature below:

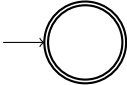
1. Regular Expressions, NFAs and CFGs

This question asks you to fill in missing

- English,
- Regular Expression,
- NFA, and
- CFG

descriptions of three languages. For each language, we have given you one of the four descriptions and it is your job to fill in the rest.

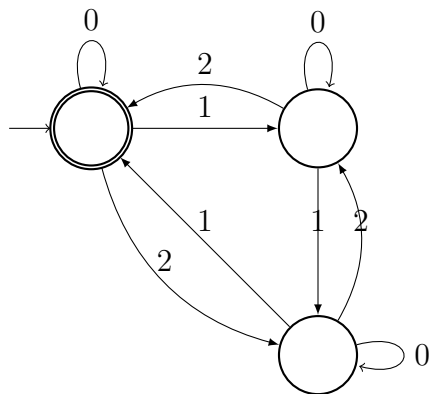
For example:

- English: The empty string
- Regular Expression: ϵ
- NFA:

- CFG: $S \rightarrow \epsilon$

(a) **CFG:** $S \rightarrow \epsilon \mid aS$

(b) **Regular Expression:** $0^*1+ \mid 1+2^+$

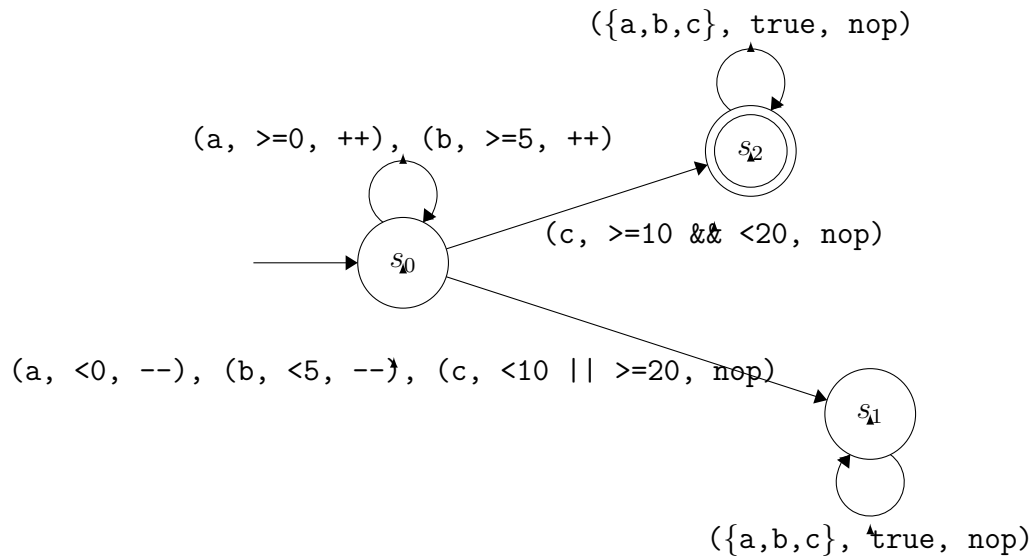
(c) **NFA** (you only need to give the English and CFG descriptions of this NFA, and *not* the regular expression):



2. Counting DFA

In this problem, we will augment the DFA model with a global counter. A Counting DFA contains a single global integer counter that can be updated when state transitions occur. In addition, every transition specifies a predicate on the counter that must be true for the transition to happen.

Specifically, every transition is now a three-tuple (**char**, **boolean expression**, **counter op**). A transition is taken if the next character read from the input matches **char** and the boolean expression is satisfied with respect to the counter. Counter operations are applied after the boolean expression is evaluated and can be ++ (increment), -- (decrement), or nop (no change). Each character needs a transition from each state for all possible counter values, but not all possible counter ops. The counter is set to 0 upon entering the DFA. Here is an example over the alphabet {a,b,c}, showing how transitions are specified:



Draw a Counting DFA that accepts a string of balanced square brackets: $\{[{}^i]{}^i \mid i \geq 0\}$.

3. Syntax-Directed Translation

Suppose you are a taxi driver in a city laid out as a grid. You can drive north (n), south (s), east (e), and west (w). The following grammar describes the routes you take that bring you back to where you started (these are not all possible routes):

$$\begin{array}{lcl} S & \rightarrow & PS \\ & | & \epsilon \\ P & \rightarrow & nPs \\ & | & sPn \\ & | & ePw \\ & | & wPe \\ & | & \epsilon \end{array}$$

Add semantic actions that, given a route, computes the maximal distance west of your starting point that your route took you. For example, **wnsee** takes you two distance units west.

4. Top-Down Parsing

Produce an LL(1) parsing table for the language described by the following CFG with terminals $\{a, b, (,)\}$.

$$\begin{aligned} S &\rightarrow ST \mid \epsilon \\ T &\rightarrow (a) \mid (b) \end{aligned}$$

Hint: you may have to factor the grammars.

5. Bottom-Up Parsing

Below is the skeleton of an LR parsing automaton, showing (numbered) states and transitions arrows, but not items or transition labels.

- (a) Provide the missing right-hand sides of the following grammar of the state diagram. There should be three terminals.

$$S' \rightarrow S$$

$$S \rightarrow$$

$$S \rightarrow$$

- (b) For each state, provide the LR(0) items from your grammar, and for each label, provide the correct transition symbols. There should be no shift-reduce or reduce-reduce conflicts in your automaton (under LR(0) parsing rules). You may not add any additional states or transitions to the diagram.

In your answer, you may use the numbers to identify states (e.g., 1: *items*) and transitions (e.g., $2 \rightarrow 1$: *transition*).

