

# Introduction to Database Systems - Normalization

Radim Bača

Department of Computer Science, FEECS

radim.baca@vsb.cz

dbedu.cs.vsb.cz

# Content

- 1NF
- 2NF
- 3NF
- BCNF
  - BCNF problem
- Database scheme decomposition
- Algorithm of a scheme decomposition
- Summary

# Database Scheme Design

- There is a lot of ways how to design a database scheme corresponding to a particular assignment
- Some solutions are comparably good, others are considerably worse
- There exists an elegant theory for the database design

# First Normal Form

A table must satisfy the following to be in a first normal form:

- The values in each attribute has to be atomic

| eID | eName   | eSkill     |
|-----|---------|------------|
| 1   | Cayley  | C++ Python |
| 2   | Laplace | C++ Java   |

# First Normal Form

A table must satisfy the following to be in a first normal form:

- The values in each attribute has to be atomic

| eID | eName   | eSkill     |
|-----|---------|------------|
| 1   | Cayley  | C++ Python |
| 2   | Laplace | C++ Java   |

# First Normal Form

A table must satisfy the following to be in a first normal form:

- The values in each attribute has to be atomic

| eID | eName   | eSkill     |
|-----|---------|------------|
| 1   | Cayley  | C++ Python |
| 2   | Laplace | C++ Java   |

→

| eID | eName   | eSkill |
|-----|---------|--------|
| 1   | Cayley  | C++    |
| 1   | Cayley  | Python |
| 2   | Laplace | C++    |
| 2   | Laplace | Java   |

# First Normal Form

A table must satisfy the following to be in a first normal form:

- The values in each attribute has to be atomic

| eID | eName   | eSkill     |
|-----|---------|------------|
| 1   | Cayley  | C++ Python |
| 2   | Laplace | C++ Java   |

→

| eID | eName   | eSkill |
|-----|---------|--------|
| 1   | Cayley  | C++    |
| 1   | Cayley  | Python |
| 2   | Laplace | C++    |
| 2   | Laplace | Java   |

Such table is considered to be in the **first normal form**

## Second Normal Form

A table must satisfy the following to be in a second normal form:

- Table is in 1NF and
- there is no partial functional dependencies



## Second Normal Form

A table must satisfy the following to be in a second normal form:

- Table is in 1NF and
- there is no partial functional dependencies

But what is a partial functional dependency?

## Second Normal Form

A table must satisfy the following to be in a second normal form:

- Table is in 1NF and
- there is no partial functional dependencies

But what is a partial functional dependency?

It is closely related to the candidate keys ...

## Candidate for a Key

- There can exist more keys for one table
- Candidates for a key of a scheme are all attributes  $\overline{K}$  for which there is no  $\overline{K}' \subset \overline{K}$  representing also a key
- In other words, we speak about shortest keys

## Candidate for a Key - Example

Let us slightly extend the previous employee table

| eID | eEmail         | eName   | eSkill |
|-----|----------------|---------|--------|
| 1   | cayley@vsb.cz  | Cayley  | C++    |
| 1   | cayley@vsb.cz  | Cayley  | Python |
| 2   | laplace@vsb.cz | Laplace | C++    |
| 2   | laplace@vsb.cz | Laplace | Java   |

Functional dependencies:

- $eID \rightarrow eName\ eEmail$
- $eEmail \rightarrow eID$

## Candidate for a Key - Example

Let us slightly extend the previous employee table

| eID | eEmail         | eName   | eSkill |
|-----|----------------|---------|--------|
| 1   | cayley@vsb.cz  | Cayley  | C++    |
| 1   | cayley@vsb.cz  | Cayley  | Python |
| 2   | laplace@vsb.cz | Laplace | C++    |
| 2   | laplace@vsb.cz | Laplace | Java   |

Functional dependencies:

- $eID \rightarrow eName\ eEmail$
- $eEmail \rightarrow eID$

What are the candidate keys?

## Candidate for a Key - Example

Let us slightly extend the previous employee table

| eID | eEmail         | eName   | eSkill |
|-----|----------------|---------|--------|
| 1   | cayley@vsb.cz  | Cayley  | C++    |
| 1   | cayley@vsb.cz  | Cayley  | Python |
| 2   | laplace@vsb.cz | Laplace | C++    |
| 2   | laplace@vsb.cz | Laplace | Java   |

Functional dependencies:

- $eID \rightarrow eName\ eEmail$
- $eEmail \rightarrow eID$

$$\{eID\}^+ = \{eID, eName, eEmail\}$$

$$\{eEmail\}^+ = \{eID, eName, eEmail\}$$

## Candidate for a Key - Example

Let us slightly extend the previous employee table

| eID | eEmail         | eName   | eSkill |
|-----|----------------|---------|--------|
| 1   | cayley@vsb.cz  | Cayley  | C++    |
| 1   | cayley@vsb.cz  | Cayley  | Python |
| 2   | laplace@vsb.cz | Laplace | C++    |
| 2   | laplace@vsb.cz | Laplace | Java   |

Functional dependencies:

- $eID \rightarrow eName, eEmail$
- $eEmail \rightarrow eID$

$$\{eID, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$

$$\{eEmail, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$

## Candidate for a Key - Example

Let us slightly extend the previous employee table

| eID | eEmail         | eName   | eSkill |
|-----|----------------|---------|--------|
| 1   | cayley@vsb.cz  | Cayley  | C++    |
| 1   | cayley@vsb.cz  | Cayley  | Python |
| 2   | laplace@vsb.cz | Laplace | C++    |
| 2   | laplace@vsb.cz | Laplace | Java   |

Functional dependencies:

- $eID \rightarrow eName, eEmail$
- $eEmail \rightarrow eID$

$$\{eID, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$

$$\{eEmail, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$



## Candidate for a Key - Example

Functional dependencies:

- $eID \rightarrow eName\ eEmail$
- $eEmail \rightarrow eID$

$\{eID, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$

$\{eEmail, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$

Ok, but what is a partial functional dependency?

## Candidate for a Key - Example

Functional dependencies:

- $eID \rightarrow eName\ eEmail$
- $eEmail \rightarrow eID$

$$\{eID, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$

$$\{eEmail, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$

In this case the first *functional dependency is partial* because has a proper subset of a candidate key on the left side and non-key attribute on the right side.

## Candidate for a Key - Example

Functional dependencies:

- $eID \rightarrow eName\ eEmail$
- $eEmail \rightarrow eID$

$$\{eID, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$

$$\{eEmail, eSkill\}^+ = \{eID, eName, eEmail, eSkill\}$$

In this case the first *functional dependency is partial* because has a proper subset of a candidate key on the left side and non-key attribute on the right side.



We need to decompose the relation in order to have a relation in 2NF.

## Second Normal Form

A table must satisfy the following to be in a second normal form:

- Table is in 1NF and
- there is no partial functional dependencies

| mID | mName  | eID | eName   | eSkill |
|-----|--------|-----|---------|--------|
| 1   | Newton | 1   | Cayley  | C++    |
| 1   | Newton | 1   | Cayley  | Python |
| 1   | Newton | 2   | Laplace | C++    |
| 1   | Newton | 2   | Laplace | Java   |

$mID \rightarrow mName$

$eID \rightarrow eName$  mld

## Second Normal Form

A table must satisfy the following to be in a second normal form:

- Table is in 1NF and
- there is no partial functional dependencies

| mID | mName  | eID | eName   | eSkill |
|-----|--------|-----|---------|--------|
| 1   | Newton | 1   | Cayley  | C++    |
| 1   | Newton | 1   | Cayley  | Python |
| 1   | Newton | 2   | Laplace | C++    |
| 1   | Newton | 2   | Laplace | Java   |

mID → mName

eID → eName mID

→

| mID | mName  | eID | eName   |
|-----|--------|-----|---------|
| 1   | Newton | 1   | Cayley  |
| 1   | Newton | 2   | Laplace |

| eID | eSkill |
|-----|--------|
| 1   | C++    |
| 1   | Python |
| 2   | C++    |
| 2   | Java   |

## Third Normal Form

A table must satisfy the following to be in a third normal form:

- Table is in 2NF and
- No non-key attributes are transitively dependent

## Third Normal Form

A table must satisfy the following to be in a third normal form:

- Table is in 2NF and
- No non-key attributes are transitively dependent

| mID | mName  | eID | eName   |
|-----|--------|-----|---------|
| 1   | Newton | 1   | Cayley  |
| 1   | Newton | 2   | Laplace |

$mID \rightarrow mName$

$eID \rightarrow eName$  mld

Is this relation in 3NF?

## Third Normal Form

A table must satisfy the following to be in a third normal form:

- Table is in 2NF and
- No non-key attributes are transitively dependent

| mID | mName  | eID | eName   |
|-----|--------|-----|---------|
| 1   | Newton | 1   | Cayley  |
| 1   | Newton | 2   | Laplace |

$mID \rightarrow mName$

$eID \rightarrow eName$   $mID$

No, there is a transitive relationship, we need to decompose it



## Third Normal Form

A table must satisfy the following to be in a third normal form:

- Table is in 2NF and
- No non-key attributes are transitively dependent

| <b>mID</b> | <b>mName</b> | <b>eID</b> | <b>eName</b> |
|------------|--------------|------------|--------------|
| 1          | Newton       | 1          | Cayley       |
| 1          | Newton       | 2          | Laplace      |

→

| <b>mID</b> | <b>mName</b> |
|------------|--------------|
| 1          | Newton       |

| <b>eID</b> | <b>eName</b> | <b>mID</b> |
|------------|--------------|------------|
| 1          | Cayley       | 1          |
| 2          | Laplace      | 1          |

# Boyce-Codd Normal Form

A table must satisfy the following to be in a Boyce-Codd normal form (BCNF):

- Table is in 3NF and
- every functional dependency must have a key on the left side

Sometimes it is not possible to achieve the BCNF and we are satisfied with 3NF

# Boyce-Codd Normal Form

A table must satisfy the following to be in a Boyce-Codd normal form (BCNF):

- Table is in 3NF and
- every functional dependency must have a key on the left side

Sometimes it is not possible to achieve the BCNF and we are satisfied with 3NF

## BCNF Problem

- A relational scheme  $R$  with a set of FDs is in BCNF if for every FD  $\overline{A} \rightarrow \overline{B}$  it holds that  $\overline{A}$  is a key
- However, there are cases when the BCNF condition cannot be satisfied
- Consider  $R(J, K, L)$  and  $FDs = \{JK \rightarrow L, L \rightarrow K\}$ 
  - There are two candidates for a key:  $JK$  and  $JL$
  - $R$  is not in BCNF and none of its decompositions will satisfy the  $JK \rightarrow L$  dependency!
  - There is no decomposition which would be in BCNF and all the dependencies would be satisfied

## One decomposition step

- One decomposition step decomposes an original table into two
- Every decomposition of a relational scheme  $R(\overline{A})$  into two relational schemes  $R_1(\overline{B})$  and  $R_2(\overline{C})$  with a minimal cover  $F$  has to satisfy the following rules:
  - $\overline{B} \cup \overline{C} = \overline{A}$
  - We try to keep all functional dependencies, i.e. it is not necessary to join  $R_1$  and  $R_2$  to check a FD.
  - $R_1 \bowtie R_2 = R$  (lossless join)

## One decomposition step

- One decomposition step decomposes an original table into two
- Every decomposition of a relational scheme  $R(\overline{A})$  into two relational schemes  $R_1(\overline{B})$  and  $R_2(\overline{C})$  with a minimal cover  $F$  has to satisfy the following rules:
  - $\overline{B} \cup \overline{C} = \overline{A}$
  - We try to keep all functional dependencies, i.e. it is not necessary to join  $R_1$  and  $R_2$  to check a FD.
  - $R_1 \bowtie R_2 = R$  (lossless join)

## One decomposition step

- One decomposition step decomposes an original table into two
- Every decomposition of a relational scheme  $R(\overline{A})$  into two relational schemes  $R_1(\overline{B})$  and  $R_2(\overline{C})$  with a minimal cover  $F$  has to satisfy the following rules:
  - $\overline{B} \cup \overline{C} = \overline{A}$
  - We try to keep all functional dependencies, i.e. it is not necessary to join  $R_1$  and  $R_2$  to check a FD.
  - $R_1 \bowtie R_2 = R$  (lossless join)

## One decomposition step

- One decomposition step decomposes an original table into two
- Every decomposition of a relational scheme  $R(\overline{A})$  into two relational schemes  $R_1(\overline{B})$  and  $R_2(\overline{C})$  with a minimal cover  $F$  has to satisfy the following rules:
  - $\overline{B} \cup \overline{C} = \overline{A}$
  - We try to keep all functional dependencies, i.e. it is not necessary to join  $R_1$  and  $R_2$  to check a FD.
  - $R_1 \bowtie R_2 = R$  (lossless join)



## Example - Lossless decomposition

- `Purchase(cName, email, pID, pCategory, pLabel, when, price)`

**Purchase**

| zName | email           | pID | pCath.    | pLabel     | when      | price |
|-------|-----------------|-----|-----------|------------|-----------|-------|
| Radim | Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim | R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li    | Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

- We perform the scheme decomposition

**Customer**

| zName | email           |
|-------|-----------------|
| Radim | Radim.B@vsb.cz  |
| Radim | R_Moskva@a.cz   |
| Li    | Jet.li@email.hk |

**ProductPurchase**

| email           | pID | pCath.    | pLabel     | when      | price |
|-----------------|-----|-----------|------------|-----------|-------|
| Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

## Example - Lossless decomposition

- `Purchase(cName, email, pID, pCategory, pLabel, when, price)`

**Purchase**

| zName | email           | pID | pCath.    | pLabel     | when      | price |
|-------|-----------------|-----|-----------|------------|-----------|-------|
| Radim | Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim | R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li    | Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

- We perform the scheme decomposition

**Customer**

| zName | email           |
|-------|-----------------|
| Radim | Radim.B@vsb.cz  |
| Radim | R_Moskva@a.cz   |
| Li    | Jet.li@email.hk |

**ProductPurchase**

| email           | pID | pCath.    | pLabel     | when      | price |
|-----------------|-----|-----------|------------|-----------|-------|
| Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

## Example - Lossless decomposition

- `Purchase(cName, email, pID, pCathegy, pLabel, when, price)`

Purchase

| zName | email           | pID | pCath.    | pLabel     | when      | price |
|-------|-----------------|-----|-----------|------------|-----------|-------|
| Radim | Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim | R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li    | Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

- We perform the scheme decomposition

| Customer |                 | ProductPurchase |     |           |            |           |       |
|----------|-----------------|-----------------|-----|-----------|------------|-----------|-------|
| zName    | email           | email           | pID | pCath.    | pLabel     | when      | price |
| Radim    | Radim.B@vsb.cz  | Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim    | R_Moskva@a.cz   | R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li       | Jet.li@email.hk | Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

- After joining the `Customer` and `ProductPurchase` relations, we get the original relation `Purchase`

## Example - Lossy decomposition

- Purchase(cName, email, pID, pCategory, pLabel, when, price)

Purchase

| zName | email           | pID | pCath.    | pLabel     | when      | price |
|-------|-----------------|-----|-----------|------------|-----------|-------|
| Radim | Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim | R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li    | Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

- We perform **another** decomposition of the scheme

Customer

| zName | email           |
|-------|-----------------|
| Radim | Radim.B@vsb.cz  |
| Radim | R_Moskva@a.cz   |
| Li    | Jet.li@email.hk |

ProductPurchase

| zName | pID | pCath.    | pLabel     | when      | price |
|-------|-----|-----------|------------|-----------|-------|
| Radim | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li    | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

## Example - Lossy decomposition

- Purchase(cName, email, pID, pCategory, pLabel, when, price)

Purchase

| zName | email           | pID | pCath.    | pLabel     | when      | price |
|-------|-----------------|-----|-----------|------------|-----------|-------|
| Radim | Radim.B@vsb.cz  | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim | R_Moskva@a.cz   | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li    | Jet.li@email.hk | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

- We may test a **different** decomposition of the scheme

| Customer |                 |   | ProductPurchase |     |           |            |           |       |
|----------|-----------------|---|-----------------|-----|-----------|------------|-----------|-------|
| zName    | email           |   | zName           | pID | pCath.    | pLabel     | when      | price |
| Radim    | Radim.B@vsb.cz  | ⋈ | Radim           | 1   | hairdryer | Electrolux | 1.8.2012  | 520   |
| Radim    | R_Moskva@a.cz   |   | Radim           | 2   | vacuum    | Hoover     | 3.9.2012  | 3500  |
| Li       | Jet.li@email.hk |   | Li              | 5   | toothpick | WoodOva    | 1.10.2012 | 5     |

- After joining the **Customer** and **ProductPurchase** relations, we do **NOT** get the original **Purchase** relation!

## Lossless join

- There exists a simple criterion  $R(\overline{A})$  to  $R_1(\overline{B})$  and  $R_2(\overline{C})$  is lossless if one of the following FD is satisfied:
  - $\overline{B} \cap \overline{C} \rightarrow \overline{B}$
  - $\overline{B} \cap \overline{C} \rightarrow \overline{C}$

# Decomposition

- A correct decomposition is based on functional dependencies (FDs) above a relational scheme
- Having an FD picked, one from the resulting relational schemes has to have only this FD's attributes and common attributes of the resulting schemes have to be on the left hand side of this FD

# Decomposition - Flashback Example

- *For the Purchase scheme, consider this set of FDs:*

*email*  $\rightarrow$  *cName*

*pID*  $\rightarrow$  *pCategory*, *pLabel*

*email*, *pID*, *when*  $\rightarrow$  *price*

*Why has the first decomposition been correct?*

- In the first example, the decomposition was done with respect to the rule *email*  $\rightarrow$  *cName*
- The *Customer* scheme consists of the attributes {*email*, *cName*}
- The common attribute is *email*



## Decomposition - Flashback Example

- *For the Purchase scheme, consider this set of FDs:*

*email  $\rightarrow$  cName*

*pID  $\rightarrow$  pCategory, pLabel*

*email, pID, when  $\rightarrow$  price*

*Why has the first decomposition been correct?*

- In the first example, the decomposition was done with respect to the rule  $\text{email} \rightarrow \text{cName}$
- The Customer scheme consists of the attributes {email, cName}
- The common attribute is email

# Algorithm of a Scheme Decomposition into BCNF

We find keys for an original relational scheme  $R$ ;

$D = \{R\}$ ;

**while** *there exists a scheme  $R' \in D$  not being in BCNF* **do**

    We choose  $\overline{A} \rightarrow \overline{B}$  for  $R'$  not satisfying the BCNF condition;

    We decompose  $R'$  into  $R_1(\overline{A}, \overline{B})$  and  $R_2(\overline{A}, \text{remaining attributes})$ ;

    We assign FDs to the new schemes  $R_1$  and  $R_2$ ;

    We find keys for  $R_1$  and  $R_2$ ;

    We remove  $R'$  from the  $D$  set and add  $R_1$  and  $R_2$  there;

**end**

# Algorithm of a Scheme Decomposition into BCNF

We find keys for an original relational scheme  $R$ ;

$D = \{R\}$ ;

**while** *there exists a scheme  $R' \in D$  not being in BCNF* **do**

    We choose  $\overline{A} \rightarrow \overline{B}$  for  $R'$  not satisfying the BCNF condition;

    We decompose  $R'$  into  $R_1(\overline{A}, \overline{B})$  and  $R_2(\overline{A}, \text{remaining attributes})$ ;

    We assign FDs to the new schemes  $R_1$  and  $R_2$ ;

    We find keys for  $R_1$  and  $R_2$ ;

    We remove  $R'$  from the  $D$  set and add  $R_1$  and  $R_2$  there;

**end**

## Algorithm of a Scheme Decomposition into BCNF

We find keys for an original relational scheme  $R$ ;

$D = \{R\}$ ;

**while** *there exists a scheme  $R' \in D$  not being in BCNF* **do**

    We choose  $\overline{A} \rightarrow \overline{B}$  for  $R'$  not satisfying the BCNF condition;

    We decompose  $R'$  into  $R_1(\overline{A}, \overline{B})$  and  $R_2(\overline{A}, \text{remaining attributes})$ ;

    We assign FDs to the new schemes  $R_1$  and  $R_2$ ;

    We find keys for  $R_1$  and  $R_2$ ;

    We remove  $R'$  from the  $D$  set and add  $R_1$  and  $R_2$  there;

**end**

## Algorithm of a Scheme Decomposition into BCNF

We find keys for an original relational scheme  $R$ ;

$D = \{R\}$ ;

**while** *there exists a scheme  $R' \in D$  not being in BCNF* **do**

    We choose  $\overline{A} \rightarrow \overline{B}$  for  $R'$  not satisfying the BCNF condition;

    We decompose  $R'$  into  $R_1(\overline{A}, \overline{B})$  and  $R_2(\overline{A}, \text{remaining attributes})$ ;

    We assign FDs to the new schemes  $R_1$  and  $R_2$ ;

    We find keys for  $R_1$  and  $R_2$ ;

    We remove  $R'$  from the  $D$  set and add  $R_1$  and  $R_2$  there;

**end**

## Algorithm of a Scheme Decomposition into BCNF

We find keys for an original relational scheme  $R$ ;

$D = \{R\}$ ;

**while** *there exists a scheme  $R' \in D$  not being in BCNF* **do**

    We choose  $\overline{A} \rightarrow \overline{B}$  for  $R'$  not satisfying the BCNF condition;

    We decompose  $R'$  into  $R_1(\overline{A}, \overline{B})$  and  $R_2(\overline{A}, \text{remaining attributes})$ ;

    We assign FDs to the new schemes  $R_1$  and  $R_2$ ;

    We find keys for  $R_1$  and  $R_2$ ;

    We remove  $R'$  from the  $D$  set and add  $R_1$  and  $R_2$  there;

**end**

## Algorithm of a Scheme Decomposition into BCNF

We find keys for an original relational scheme  $R$ ;

$D = \{R\}$ ;

**while** *there exists a scheme  $R' \in D$  not being in BCNF* **do**

    We choose  $\overline{A} \rightarrow \overline{B}$  for  $R'$  not satisfying the BCNF condition;

    We decompose  $R'$  into  $R_1(\overline{A}, \overline{B})$  and  $R_2(\overline{A}, \text{remaining attributes})$ ;

    We assign FDs to the new schemes  $R_1$  and  $R_2$ ;

    We find keys for  $R_1$  and  $R_2$ ;

    We remove  $R'$  from the  $D$  set and add  $R_1$  and  $R_2$  there;

**end**

## Decomposition into BCNF - Example

- *Purchase(cName, email, pID, pCategory, pLabel, when, price)*  
 $\{email \rightarrow cName; pID \rightarrow pCategory, pLabel;$   
 $email, pID, when \rightarrow price\}$
- $\{email, pID, when\}$  is the key



## Decomposition into BCNF - Example

- *Purchase(cName, email, pID, pCategory, pLabel, when, price)*  
 $\{email \rightarrow cName; pID \rightarrow pCategory, pLabel;$   
 $email, pID, when \rightarrow price\}$
- $\{email, pID, when\}$  is the key

## Decomposition into BCNF - Example

- *Purchase*(*cName*, *email*, *pID*, *pCategory*, *pLabel*, *when*, *price*)  
 $\{email \rightarrow cName; pID \rightarrow pCategory, pLabel; email, pID, when \rightarrow price\}$
- $\{email, pID, when\}$  is the key
- There are two FDs violating the BCNF condition;  
 let us choose, e.g.,  $email \rightarrow cName$
- We decompose the original *Purchase* scheme into two:
  - *Customer*(*email*, *cName*)
  - *Purchase*(*email*, *pID*, *pCategory*, *pLabel*, *when*, *price*)

## Decomposition into BCNF - Example

- *Purchase*(*cName*, *email*, *pID*, *pCategory*, *pLabel*,  
*when*, *price*)  
 $\{email \rightarrow cName; pID \rightarrow pCategory, pLabel;$   
 $email, pID, when \rightarrow price\}$
- $\{email, pID, when\}$  is the key
- There are two FDs violating the BCNF condition;  
let us choose, e.g.,  $email \rightarrow cName$
- We decompose the original *Purchase* scheme into two:
  - *Customer*(*email*, *cName*)
  - *Purchase*(*email*, *pID*, *pCategory*, *pLabel*,  
*when*, *price*)

## Decomposition into BCNF - Example

- We decompose the original `Purchase` scheme into two:
  - `Customer(email, cName)`
  - `Purchase(email, pID, pCategory, pLabel, when, price)`
- The attributes `{email, pID, when}` are still the key of the `Purchase` scheme

## Decomposition into BCNF - Example

- We decompose the original `Purchase` scheme into two:
  - `Customer(email, cName)`
  - `Purchase(email, pID, pCategory, pLabel, when, price)`
- The attributes `{email, pID, when}` are still the key of the `Purchase` scheme
- `pID → pCategory, pLabel` violates the BCNF condition
- We decompose the new `Purchase` scheme:
  - `Product(pID, pCategory, pLabel)`
  - `Purchase(email, pID, when, price)`

## Decomposition into BCNF - Example

- We decompose the original `Purchase` scheme into two:
  - `Customer(email, cName)`
  - `Purchase(email, pID, pCategory, pLabel, when, price)`
- The attributes `{email, pID, when}` are still the key of the `Purchase` scheme
- `pID → pCategory, pLabel` violates the BCNF condition
- We decompose the new `Purchase` scheme:
  - `Product(pID, pCategory, pLabel)`
  - `Purchase(email, pID, when, price)`

## Decomposition into BCNF - Example

- We decompose the original `Purchase` scheme into two:
  - `Customer(email, cName)`
  - ~~`Purchase(email, pID, pCategory, pLabel, when, price)`~~
- The attributes `{email, pID, when}` are still the key of the `Purchase` scheme
- `pID → pCategory, pLabel` violates the BCNF condition
- We decompose the new `Purchase` scheme:
  - `Product(pID, pCategory, pLabel)`
  - `Purchase(email, pID, when, price)`

# Decomposition into BCNF - Properties

- Please recall that there are two requirements:
  - The decomposition satisfies the requirement on lossless join (i.e.,  $R_1 \bowtie R_2 \bowtie \dots \bowtie R_n = R$ )
  - All functional dependencies has to be satisfied
- The first requirement is always satisfied if we use the decomposition to BCNF
- The resulting scheme produced by the algorithm is dependent on an order in which we pick FDs
- We start with FD where attributes on the right side never occur on the left side in any other FD
- The problem is that sometimes we can not perform a decomposition to BCNF and keep all FDs



## Decomposition into BCNF - Properties

- Please recall that there are two requirements:
  - The decomposition satisfies the requirement on lossless join (i.e.,  $R_1 \bowtie R_2 \bowtie \dots \bowtie R_n = R$ )
  - All functional dependencies has to be satisfied
- The first requirement is always satisfied if we use the decomposition to BCNF
- The resulting scheme produced by the algorithm is dependent on an order in which we pick FDs
- We start with FD where attributes on the right side never occur on the left side in any other FD
- The problem is that sometimes we can not perform a decomposition to BCNF and keep all FDs

## Decomposition into BCNF - Properties

- Please recall that there are two requirements:
  - The decomposition satisfies the requirement on lossless join (i.e.,  $R_1 \bowtie R_2 \bowtie \dots \bowtie R_n = R$ )
  - All functional dependencies has to be satisfied
- The first requirement is always satisfied if we use the decomposition to BCNF
- The resulting scheme produced by the algorithm is dependent on an order in which we pick FDs
- We start with FD where attributes on the right side never occur on the left side in any other FD
- The problem is that sometimes we can not perform a decomposition to BCNF and keep all FDs

## Decomposition into BCNF - Properties

- Please recall that there are two requirements:
  - The decomposition satisfies the requirement on lossless join (i.e.,  $R_1 \bowtie R_2 \bowtie \dots \bowtie R_n = R$ )
  - All functional dependencies has to be satisfied
- The first requirement is always satisfied if we use the decomposition to BCNF
- The resulting scheme produced by the algorithm is dependent on an order in which we pick FDs
- We start with FD where attributes on the right side never occur on the left side in any other FD
- The problem is that sometimes we can not perform a decomposition to BCNF and keep all FDs

## Decomposition into BCNF - Properties

- Please recall that there are two requirements:
  - The decomposition satisfies the requirement on lossless join (i.e.,  $R_1 \bowtie R_2 \bowtie \dots \bowtie R_n = R$ )
  - All functional dependencies has to be satisfied
- The first requirement is always satisfied if we use the decomposition to BCNF
- The resulting scheme produced by the algorithm is dependent on an order in which we pick FDs
- We start with FD where attributes on the right side never occur on the left side in any other FD
- The problem is that sometimes we can not perform a decomposition to BCNF and keep all FDs

# Summary

- Functional dependencies (FDs)
  - represent a relationship among attributes, which can cause redundancy in data
  - By using FDs, we find a closure for some attributes and also a key of a scheme
- Optimization of a set of FDs
- 1NF, 2NF, 3NF, BCNF
- Relational scheme decomposition
- BCNF:
  - form of relational scheme that is lossless
  - decomposition into BCNF with respect to FDs

# Summary

- Functional dependencies (FDs)
  - represent a relationship among attributes, which can cause redundancy in data
  - By using FDs, we find a closure for some attributes and also a key of a scheme
- Optimization of a set of FDs
- 1NF, 2NF, 3NF, BCNF
- Relational scheme decomposition
- BCNF:
  - form of relational scheme that is lossless
  - decomposition into BCNF with respect to FDs

## Summary

- Functional dependencies (FDs)
  - represent a relationship among attributes, which can cause redundancy in data
  - By using FDs, we find a closure for some attributes and also a key of a scheme
- Optimization of a set of FDs
- 1NF, 2NF, 3NF, BCNF
- Relational scheme decomposition
- BCNF:
  - form of relational scheme that is lossless
  - decomposition into BCNF with respect to FDs

## Summary

- Functional dependencies (FDs)
  - represent a relationship among attributes, which can cause redundancy in data
  - By using FDs, we find a closure for some attributes and also a key of a scheme
- Optimization of a set of FDs
- 1NF, 2NF, 3NF, BCNF
- Relational scheme decomposition
- BCNF:
  - form of relational scheme that is lossless
  - decomposition into BCNF with respect to FDs



# Summary

- Functional dependencies (FDs)
  - represent a relationship among attributes, which can cause redundancy in data
  - By using FDs, we find a closure for some attributes and also a key of a scheme
- Optimization of a set of FDs
- 1NF, 2NF, 3NF, BCNF
- Relational scheme decomposition
- BCNF:
  - form of relational scheme that is lossless
  - decomposition into BCNF with respect to FDs

# Summary

- Functional dependencies (FDs)
  - represent a relationship among attributes, which can cause redundancy in data
  - By using FDs, we find a closure for some attributes and also a key of a scheme
- Optimization of a set of FDs
- 1NF, 2NF, 3NF, BCNF
- Relational scheme decomposition
- BCNF:
  - form of relational scheme that is lossless
  - decomposition into BCNF with respect to FDs

## References

- Jennifer Widom. Introduction to Databases.  
<https://www.coursera.org/course/db>
- Course home pages <http://dbedu.cs.vsb.cz>