

Centroiding Point-Objects with Event Cameras

Dr. Scott McCloskey

Presentation Outline: EBS-base Centroiding

- ◆ Problem definition
- ◆ Motivating applications of EBS-based centroiding
- ◆ Analytical model and theoretical bounds
- ◆ Dataset collection
- ◆ LSTM-based Centroiding approach
- ◆ Experimental results
- ◆ Summary & conclusions

Technology: Event-Based Sensors

Advantages

- Low latency ($<100\mu\text{s}$)
- Low power consumption/less wasted energy
- High dynamic range

Challenges:

- Sparse/few events in small time batches
- Non-Gaussian spatial event distribution
- Event distribution depends on object brightness and velocity

Image Frame



Intensity

Event "Frame"



Positive Events
Negative Events

Technology: Event-Based Sensors

Advantages

- Low latency ($<100\mu s$)

Approach: Estimate an unresolved object's **centroid and velocity** in **$<20ms$** by leveraging the **spatial cues** in the event distribution

1. Develop an analytical model of event distributions
2. Create centroiding dataset from a high-speed monitor
3. Train a SOTA centroiding model for 5ms and 20ms time batches
4. Compare performance against theoretical bounds

and velocity

Image Frame

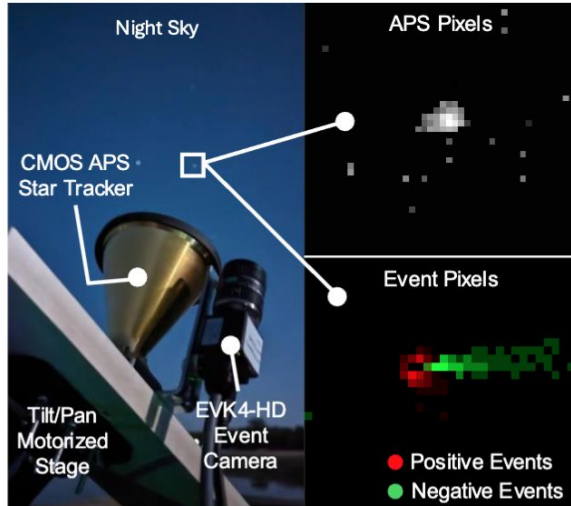
Intensity

Positive Events

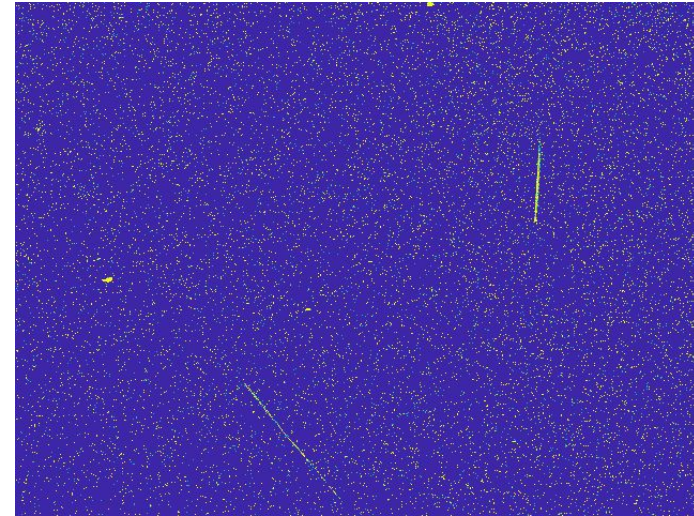
Negative Events

Kitware's EBS Work & Motivating Applications

Event-based star tracking Poster #108, Friday afternoon



Meteor detection and classification [1]



Closed-Form Event Distribution Model

- In low-light, each EBS pixel acts as a low-pass filter (LPF) [3]:

“Event Likelihood”

LPF Cutoff Frequency

Pixel Voltage

$$E_{LL}(\mathbf{x}, t) = 2\pi \cdot f_c(\tilde{I}(\mathbf{x}, t)) \cdot [\tilde{I}(\mathbf{x}, t) - V(\mathbf{x}, t)]$$

Pixel Time

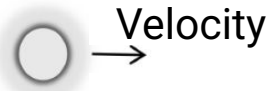
Intensity on Image Plane

The diagram shows the equation $E_{LL}(\mathbf{x}, t) = 2\pi \cdot f_c(\tilde{I}(\mathbf{x}, t)) \cdot [\tilde{I}(\mathbf{x}, t) - V(\mathbf{x}, t)]$ with several annotations. A red dashed box around $E_{LL}(\mathbf{x}, t)$ is labeled “Event Likelihood” with a red arrow. An orange dashed box around $f_c(\tilde{I}(\mathbf{x}, t))$ is labeled “LPF Cutoff Frequency” with an orange arrow. A green dashed box around $V(\mathbf{x}, t)$ is labeled “Pixel Voltage” with a green arrow. A blue dashed box around $\tilde{I}(\mathbf{x}, t)$ is labeled “Intensity on Image Plane” with a blue arrow. Below the equation, the terms “Pixel” and “Time” are written, with blue arrows pointing to \mathbf{x} and t respectively.

- With some simple assumptions, we can achieve a **closed-form solution** that **facilitates advanced analysis**

Event Distribution Comparisons

Unresolved
Object



Conventional
Models

Spatial
Derivative of Log



Spatial
Derivative



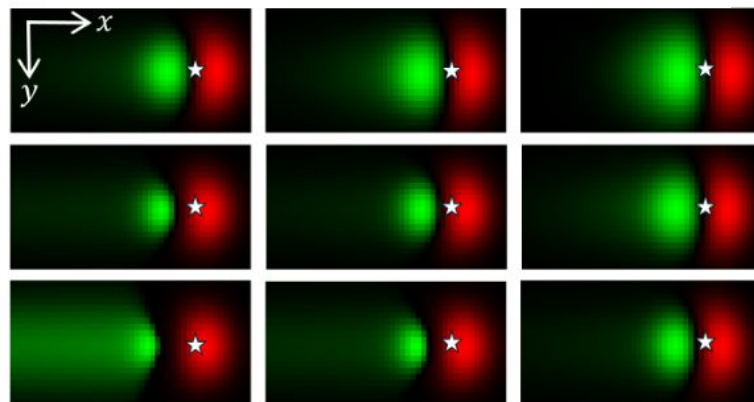
☆ True
Centroid

● Pos
Events

● Neg
Events

- Speed, position, and intensity are all **spatially coupled**
- Therefore, **spatial cues** lend important information
- Analytical results align with captured dataset

Proposed Closed-Form Solution



Low
Speed

High
Speed

Dim

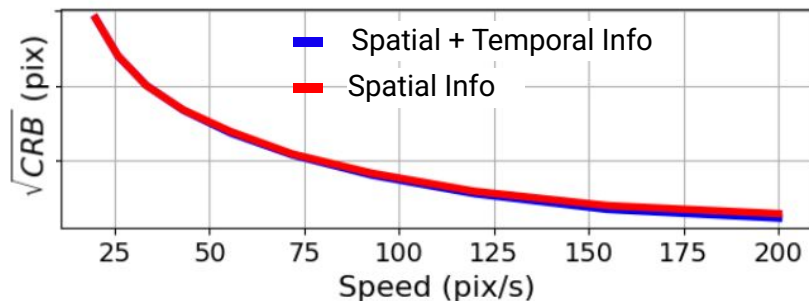
Bright

Cramér-Rao Bounds (CRB)

[4] Shah, Sachin, et al. "Codeevents: optimal point-spread-function engineering for 3d-tracking with event cameras." Proceedings of the IEEE/CVF conference on computer vision and pattern recognition. 2024.

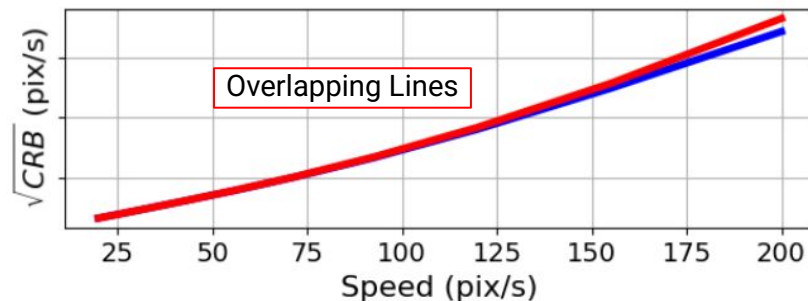
- Sample-normalized CRB can be analytically calculated with the closed-form model

Object Centroid Sample-Normalized CRB



(lower CRB = more accurate estimator)

Object Speed Sample-Normalized CRB



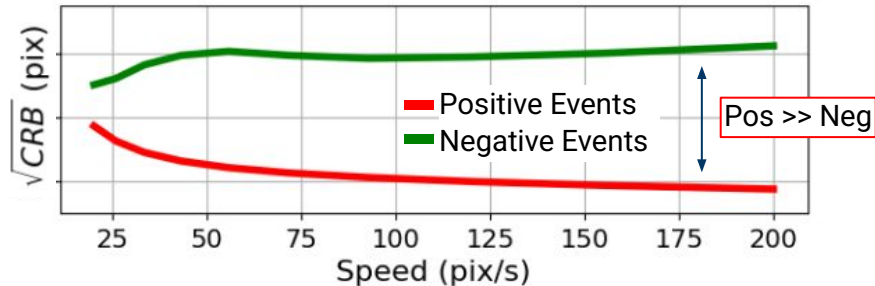
Two main takeaways:

- Temporal information is **not as important** for small time batches

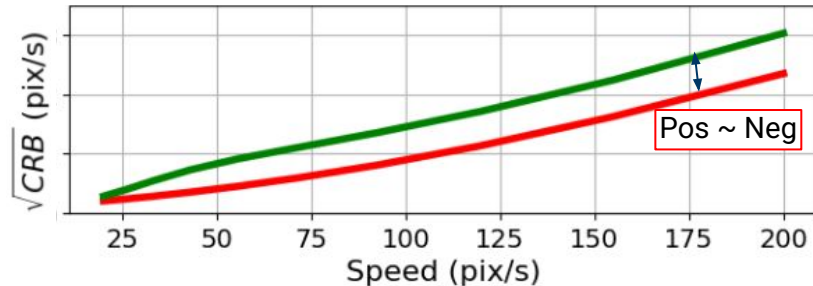
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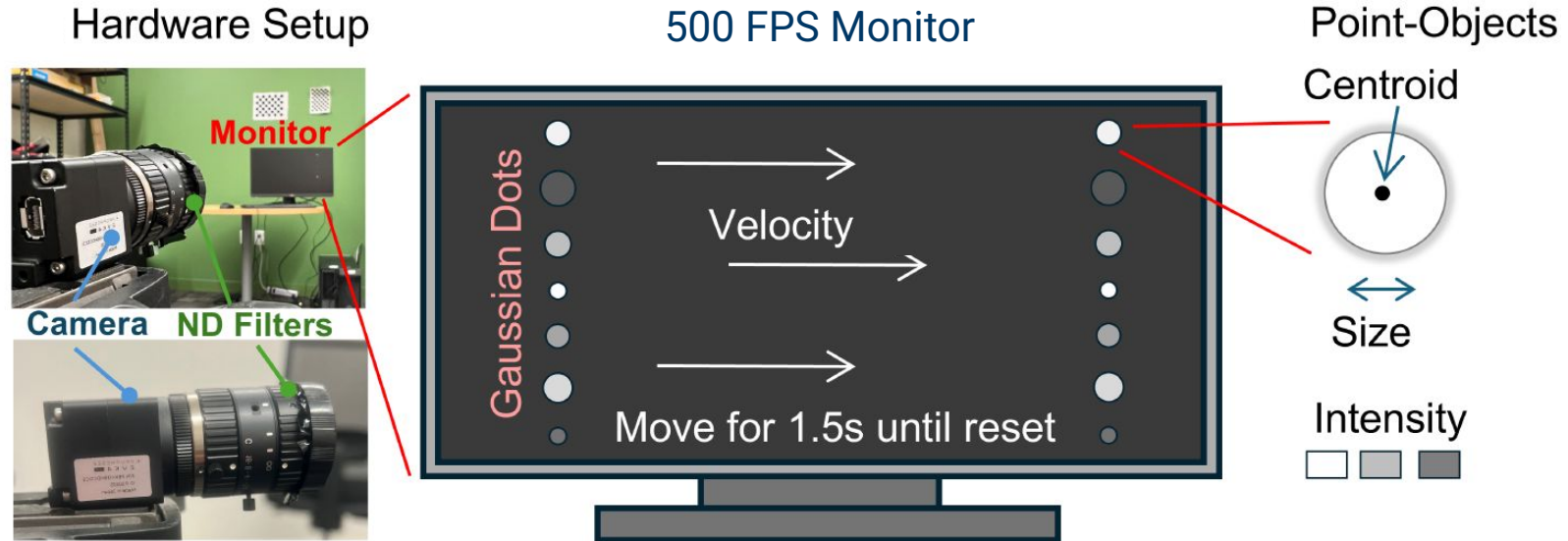
(lower CRB = more accurate estimator)

Two large takeaways:

- Temporal information is **not as important** for small time batches
- Negative events are useful** in estimating velocity

Centroiding Dataset

- ◆ To train a model to leverage these spatial cues, we collect a point-object centroiding dataset



Prophesee EVK4-HD

Centroiding Dataset

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Camera Resolution	Length (time)	# Unique Objects	# Unique 5ms Event Streams
1280x720	3 hours	10,588	2,117,600

Calibration Error	Obj Event Rates	Obj Inten Range	Obj Size Range	Obj Vel Range
~0.2 pixels	2 to 20kHz	8 to 300 μ lux	1 to 8 pixels	15 to 350 pix/s

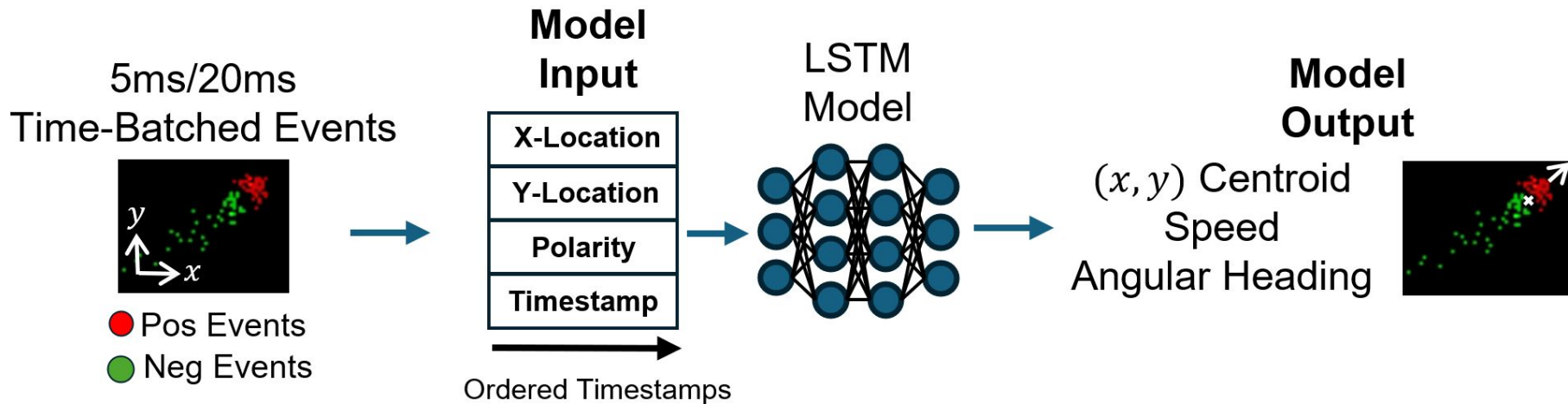
Examples of Dataset Capture

Monitor Video

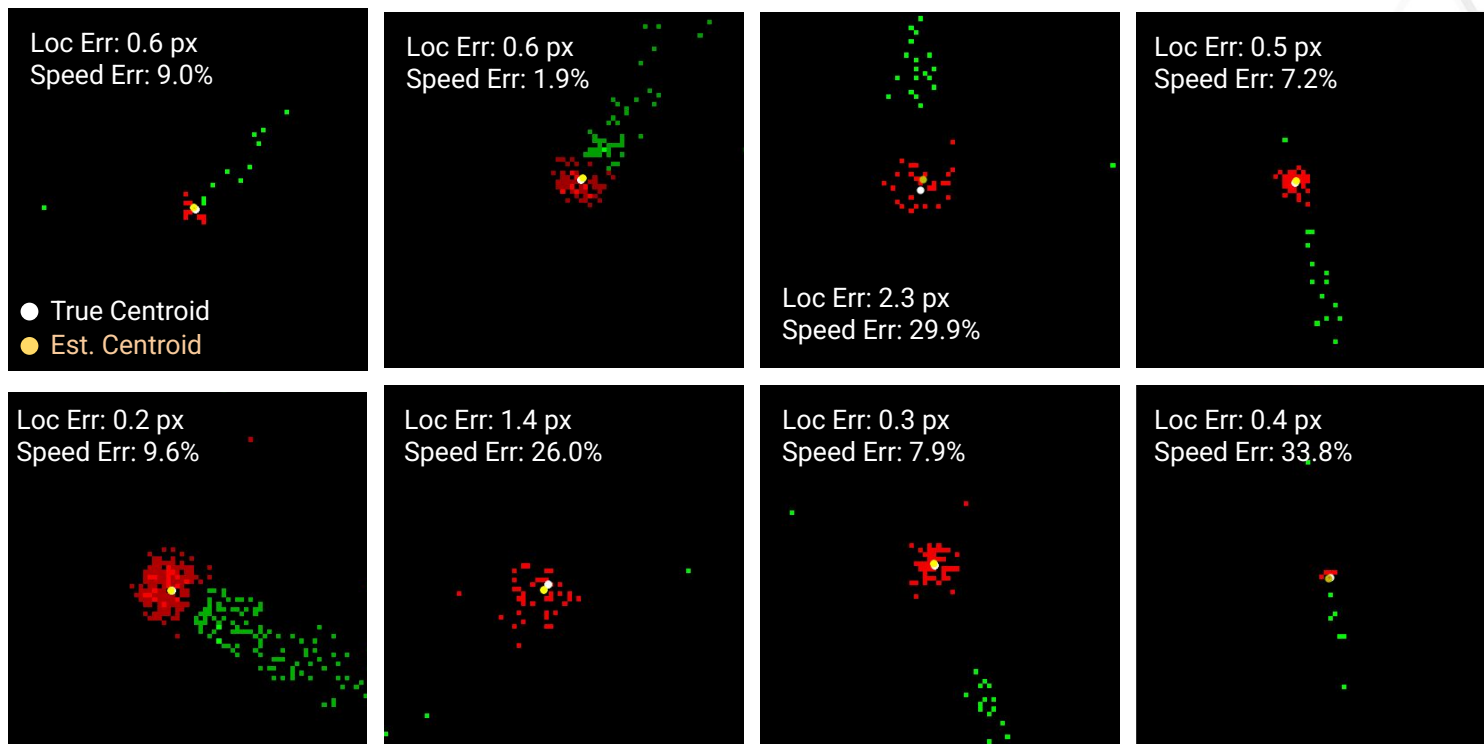
Resulting Events

LSTM-based EBS Centroiding Approach

- **Model:** 3-layer LSTM, 500k total parameters
- Feed each event in one at a time, observe the output after the last event



Centroiding Results



Centroiding Results

Tested on 85,000 5ms and 20ms event streams
Best results **bolded**, second-best underlined

- Centroiding Results:
Compared to previous
methods, the proposed
model has...

- ~2x location accuracy
- ~5x speed accuracy

(a) 5ms time batch

Method	Events Used	Location Error (pix)	SMAPE Speed Error (%)	Angular Error (deg)
Mean Cent.	Pos	<u>1.74 ± 1.45</u>	112.30 ± 56.60	72.42 ± 48.89
Mean Cent.	Pos, Neg	6.60 ± 3.00	136.82 ± 51.08	<u>15.91 ± 36.80</u>
Inten. Recon.	Pos, Neg	1.76 ± 1.47	111.27 ± 56.31	72.23 ± 48.76
Gauss MLE	Pos	2.34 ± 2.00	<u>102.34 ± 57.13</u>	67.93 ± 48.74
LSTM Model	Pos, Neg	0.95 ± 0.70	17.75 ± 17.10	15.54 ± 30.60

(b) 20ms time batch

Mean Cent.	Pos	2.19 ± 1.36	42.04 ± 44.62	28.59 ± 35.87
Mean Cent.	Pos, Neg	7.51 ± 2.68	64.47 ± 48.53	<u>12.94 ± 35.25</u>
Inten. Recon.	Pos, Neg	<u>1.68 ± 1.33</u>	41.77 ± 44.34	28.56 ± 35.91
Gauss MLE	Pos	1.76 ± 1.38	<u>36.79 ± 41.38</u>	26.01 ± 34.80
LSTM Model	Pos, Neg	0.76 ± 0.54	10.66 ± 10.35	6.27 ± 10.48

5ms Time-Batch Centroiding Ablation Study

Event Information			Metrics		
Pos Events	Neg Events	Event Order	Loc Err (pix)	Speed Err (%)	Angular Err (deg)
✓	✓	✓	0.95	17.7	15.5
✓	✓	X	0.95	17.4	15.5
✓	X	✓	1.08	37.3	45.4
X	✓	✓	2.81	25.9	17.8

- Removing timestamps/event order *does not* affect model accuracy
 - **Majority of information is in the spatial distribution** for small time batches
- **Positive** events are important for *location estimation*
- **Negative** events are important for *velocity estimation*

5ms Time-Batch Centroiding Ablation Study

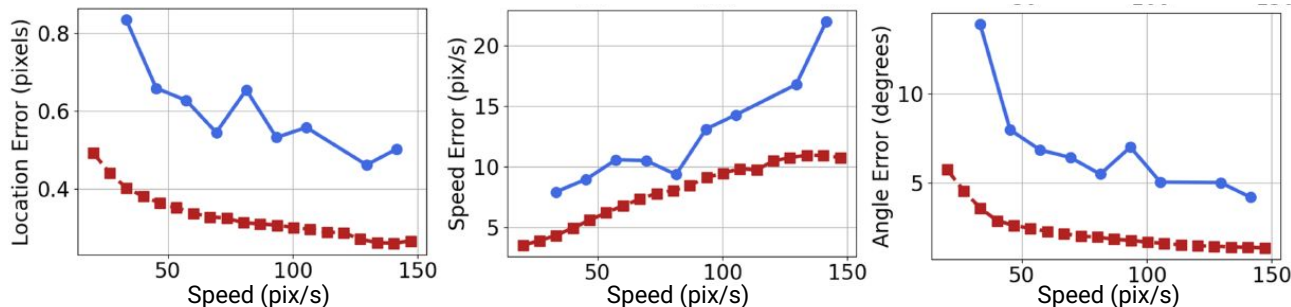
Object Priors		Metrics		
Size + Inten Info	Vel Info	Loc Err (pix)	Speed Err (%)	Angular Err (deg)
✓	✓	0.81	NA	NA
✓	X	0.88	16.0	16.3
X	X	0.95	17.7	15.5

- Priors (size, intensity, and velocity) only offer minor improvement
- This suggests that the network can **successfully decorrelate these effects**

Cramér-Rao Bounds (CRB)

Constant object size, intensity

LSTM
Model
CRB



- ◆ We can compare the model's accuracy to CRB limitations
- ◆ Unlike previous analytical CRB, this is empirically calculated via the dataset
- ◆ Our model's accuracy approaches that limit or at least adopts a similar shape

Summary

- **Objective:** leverage the spatiotemporal distribution of events to better localize unresolved objects in $<20\text{ms}$

Image Frame



● Intensity

Event "Frame"



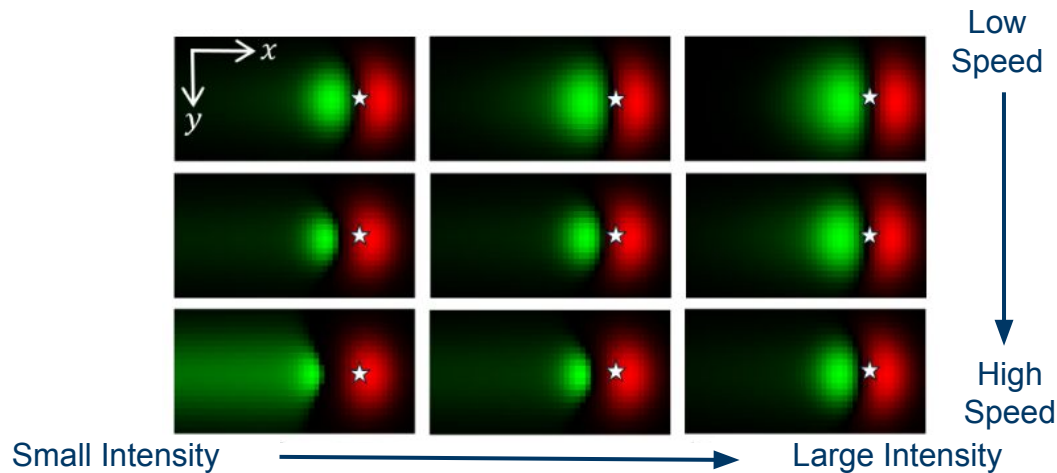
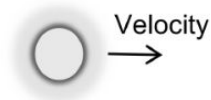
● Positive Events

● Negative Events

Summary

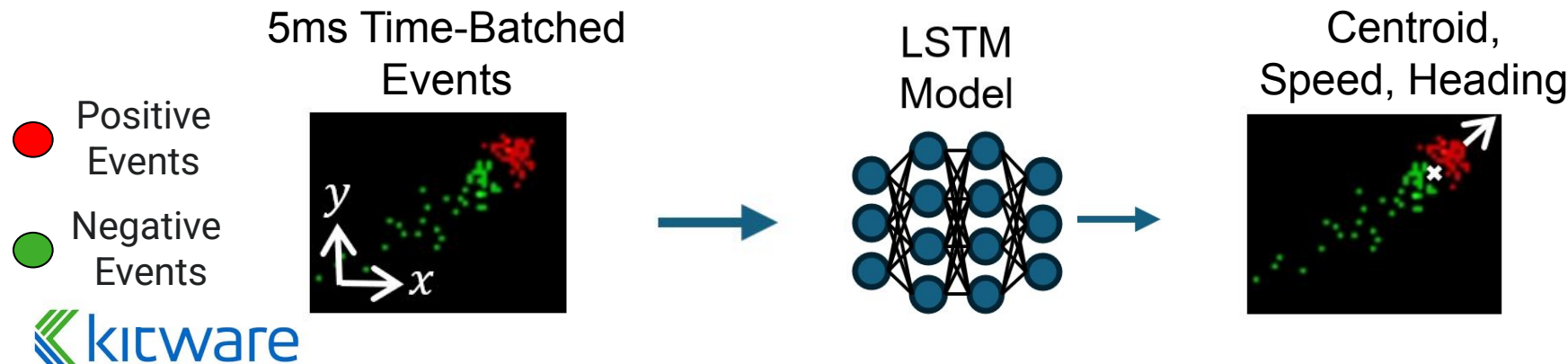
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Unresolved
Object



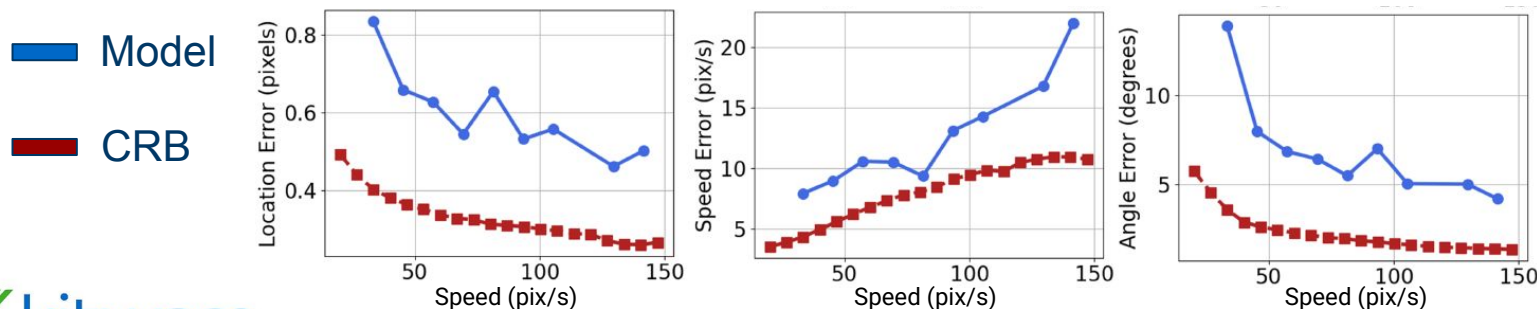
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- Our model's performance can be compared to the Cramér-Rao Bounds (CRB)
- Additional results include more ablation studies, additional analysis, and performance on star tracking
- Dataset/code: <https://gitlab.kitware.com/nest-public/ebs-datadriven-centroiding>