## Near-consistent robust estimations of moments for unimodal distributions

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This manuscript was compiled on June 8, 2023

orderliness | invariant | unimodal | adaptive estimation | U-statistics

- **A. Congruent distribution.** In the realm of nonparametric
- 2 statistics, the relative differences, or orders, of robust esti-
- 3 mators are of primary importance. Deducting from this prin-
- $^{4}$  ciple, it is natural to assume that when there is a shift in the
- 5 parameters of the underlying distribution, all nonparametric
- 6 estimates should asymptotically change in the same direction,
- $_{7}$  if they are estimating the same attribute of the distribution.
- $_{8}\,\,$  Otherwise, if the mean indicates an increase in the location
- 9 of the distribution, but the median indicates a decrease, a
- 10 contradiction arises.
- Data Availability. Data for Table ?? are given in SI Dataset S1.
- 12 All codes are attached.
- 13 ACKNOWLEDGMENTS. I gratefully acknowledge the construc-
- tive comments made by the editor which substantially improved
- the clarity and quality of this paper.