Semiparametric robust mean estimations based on the orderliness of quantile averages

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- As one of the most fundamental problems in statistics, robust location
- estimation has many prominent solutions, such as the trimmed mean,
- 3 Winsorized mean, Hodges-Lehmann estimator, Huber M-estimator,
- and median of means. Recent studies suggest that their maximum
- biases concerning the mean can be quite different, but the under-
- 6 lying mechanisms remain largely unclear. In this article, similar to
- 7 the mean-median-mode inequality, it is proven that in the context
- 8 of nearly all common unimodal distributions, there exists an orderli-
- ness of symmetric quantile averages with different breakdown points.
 Further deductions explain why the Winsorized mean and median
- of means generally have smaller biases compared to the trimmed
- The state of the s
- 12 mean. Building on the U-orderliness, the superiority of the median
- 13 Hodges-Lehmann mean is discussed.

semiparametric | mean-median-mode inequality | asymptotic | unimodal | Hodges—Lehmann estimator

- Data Availability. Data for Figure ?? are given in SI Dataset
- 2 S1. All codes have been deposited in GitHub.
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- 5 and merit of this paper.