## Semiparametric robust mean estimations based on the orderliness of quantile averages

## **Tuban Lee**

This manuscript was compiled on June 6, 2023

- As one of the most fundamental problems in statistics, robust loca-
- 2 tion estimation has many prominent solutions, such as the symmetric
- 3 trimmed mean, symmetric Winsorized mean, Hodges-Lehmann es-
- 4 timator, Huber M-estimator, and median of means. Recent studies
- suggest that their biases concerning the mean can be quite different
- 6 in asymmetric distributions, but the underlying mechanisms largely
- 7 remain unclear. This study establishes two forms of orderliness within
- 8 a wide range of semiparametric distributions. Further deductions ex-
- plain why the Winsorized mean typically has smaller biases compared
  to the trimmed mean; two sequences of semiparametric robust mean
- estimators emerge. Building on the  $\gamma$ -U-orderliness, the superiority
- estimators emerge. Building on the  $\gamma$ - $\delta$ -orderimess, the superior of the median Hodges–Lehmann mean is discussed.

semiparametric | mean-median-mode inequality | asymptotic | unimodal | Hodges–Lehmann estimator