Semiparametric robust mean estimations based on the orderliness of quantile averages

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semiparametric | mean-median-mode inequality | asymptotic | unimodal | Hodges—Lehmann estimator

Inequalities related to weighted averages

- 2 So far, it seems plausible that the bias of a reasonable weighted
- 3 average should be monotonically related to its degree of robust-
- 4 ness in a semiparametric distribution, since it is a linear com-
- bination of quantile averages. Analogous to the γ -orderliness,
- 6 the γ -trimming inequality for a right-skewed distribution is
- 7 defined as $\forall 0 \leq \epsilon_1 \leq \epsilon_2 \leq \frac{1}{1+\gamma}, \gamma \geq 0, TM_{\epsilon_1, \gamma} \geq TM_{\epsilon_2, \gamma}$.
- 8 γ -orderliness is a sufficient condition for the γ -trimming in-
- 9 equality, as proven in the SI Text. The next theorem shows
- another relation between quantile average and trimmed mean.
- Theorem .1. For a distribution that is right-skewed and
- follows the γ -trimming inequality, it is asymptotically true
- 3 that the quantile average is always greater or equal to the
- 14 corresponding trimmed mean with the same ϵ and γ .
- Data Availability. Data for Figure ?? are given in SI Dataset
- 16 S1. All codes have been deposited in GitHub.
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