Semiparametric robust mean estimations based on the orderliness of quantile averages

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- As one of the most fundamental problems in statistics, robust loca-
- 2 tion estimation has many prominent solutions, such as the symmetric
- 3 trimmed mean, symmetric Winsorized mean, Hodges-Lehmann es-
- 4 timator, Huber M-estimator, and median of means. Recent studies
- suggest that their biases concerning the mean can be quite different
- 6 in asymmetric distributions, but the underlying mechanisms largely
- remain unclear. This study establishes two forms of orderliness within
 a wide range of semiparametric distributions. Further deductions ex-
- 9 plain why the Winsorized mean typically has smaller biases compared
- to the trimmed mean; two sequences of semiparametric robust mean
- estimators emerge. Building on the γ -U-orderliness, the superiority
- of the median Hodges-Lehmann mean is discussed.

semiparametric | mean-median-mode inequality | asymptotic | unimodal | Hodges—Lehmann estimator

Classifying Distributions by the Signs of Derivatives

- Let $\mathcal{P}_{\mathbb{R}}$ denote the set of all continuous distributions over
- $_{3}$ $\,$ \mathbb{R} and $\mathcal{P}_{\mathbb{X}}$ denote the set of all discrete distributions over a
- 4 countable set X.
- 5 Data Availability. Data for Figure ?? are given in SI Dataset
- 6 S1. All codes have been deposited in GitHub.
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