

Binary_Simulation_v2

Hun

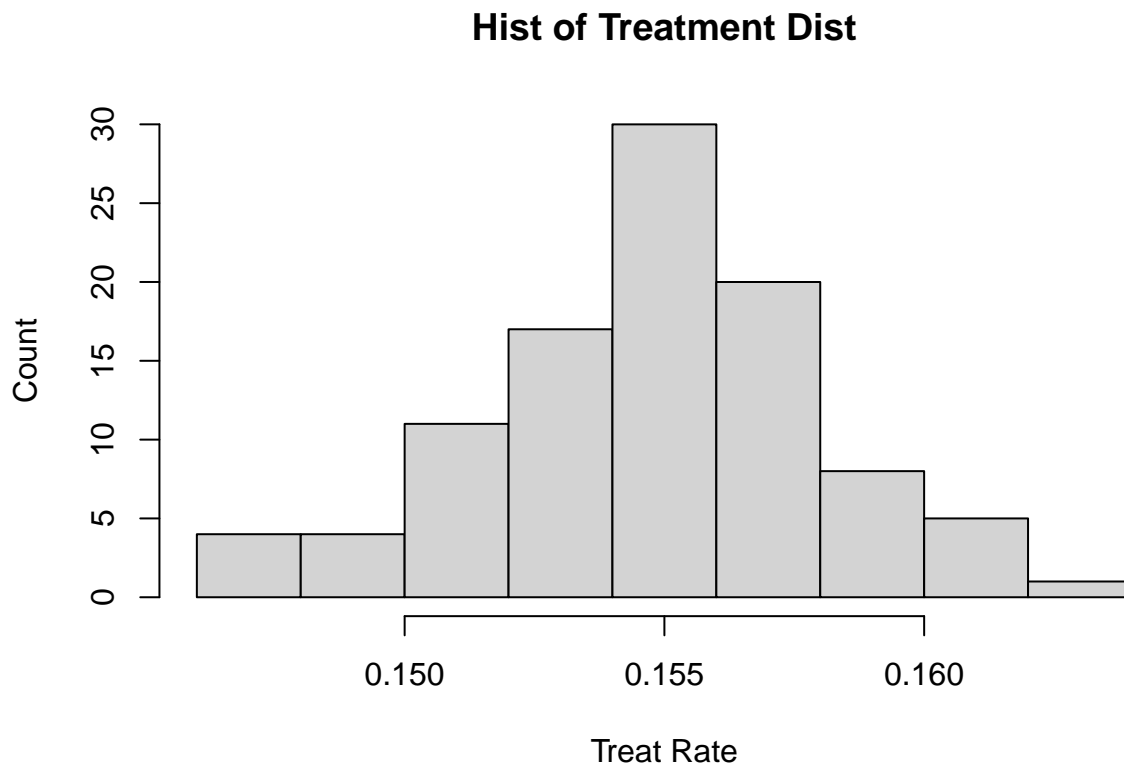
2/15/2022

```
source('./shared_code/data_gen_final_pretty.R')
```

Function for finding the optimal combination of coefficients for covariates to have desired proportion of the treated.

checking dist of treatment rate.

```
hist(map_dbl(1:length(no_boot_list), function(i) mean(no_boot_list[[i]]$A)),  
     main = "Hist of Treatment Dist",  
     xlab = "Treat Rate",  
     ylab = "Count")
```



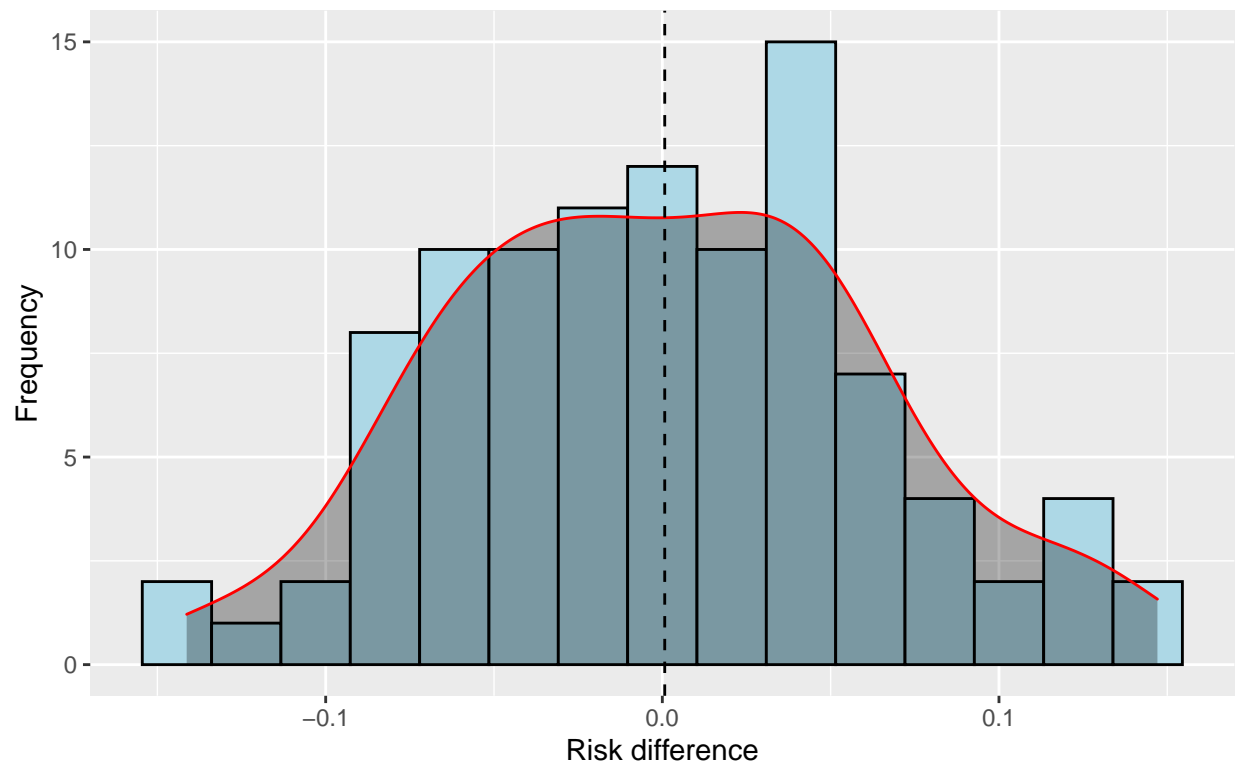
Function for no boot bias distribution

```
no_boot_result <-  
  function(n) {  
    b <- vector()  
    for (i in 1:n) {  
      a <- glm(Y ~ A + L2 + L3, data = no_boot_list[[i]], family = "binomial")  
      b[i] <- summary(a)$coef[2,1]  
    }  
    return(b)  
  }  
  
no_boot_OR <- no_boot_result(100)
```

No boot Bias plot

```
no_boot_bias <-  
  tibble(no_boot_OR = no_boot_OR) %>%  
  summarise(bias = (no_boot_OR - 0.767))  
  
no_boot_bias %>%  
  ggplot(aes(x = bias)) +  
  geom_histogram(fill = "light blue", bins = 15, color = "black") +  
  geom_density(aes(y = ..density..*2), colour = "red",  
               fill = "black", alpha = 0.3) +  
  geom_vline(xintercept = mean(no_boot_bias$bias), linetype = "dashed") +  
  labs(title = "Distribution of no boot ATE bias",  
       caption = "Ideal center: 0", x = "Risk difference", y = "Frequency") +  
  theme(  
    plot.title = element_text(color = "blue", size = 11, face = "bold"),  
    plot.caption = element_text(color = "orange", face = "italic")  
  )
```

Distribution of no boot ATE bias



Ideal center: 0

Implementing nearest-neighbor matching (NNM)

```
df <- no_boot_list
pb4 <- progress_bar$new(format = "bootstrapping... [:bar] :percent eta: :eta",
                        total = length(df))

# could possible turn this into a function later.
matched_df <- list()
# mean_treat_save <- rep(0, length(df))
# match_save <- rep(0, length(df))
for (i in 1:length(df)) {
  pb4$tick()
  matched <- matchit(A ~ L2 + L3,
                    data = df[[i]],
                    distance = "glm",
                    link = "logit",
                    method = "nearest",
                    ratio = 1) # perform NNM

  matched_df[[i]] <- match.data(matched, distance = "ps")
  # mean_treat_save[i] <- (5000*mean(df[[i]]$A)*2)
  # match_save[i] <- (match.data(matched, distance = "ps") %>%
  #   select(subclass) %>% unique() %>% summarize(n=n()) %>% pull(n))*2
}
```

simple Bootstrap

```
# creating the tibble to apply map function
matched_tib <-
  tibble(data = matched_df)

# ### function to iterate glm over a list, to be used in purr:map ###
# returns tibble of parameter estimates and standard errors.

outcome_model_list <- function(list) {
  tib_coef <- tibble()
  boots <- tibble(mean1 = NA,
                  mean0 = NA,
                  difference = NA)
  pb3$tick()
  for (i in 1:length(list)) {
    mod <- glm(Y ~ A + ps,
              data = list[[i]],
              weights = weights,
              family = "binomial")

    sampl_all_treated <- list[[i]] %>%
      mutate(A = 1)

    sampl_all_untreated <- list[[i]] %>%
      mutate(A = 0)

    sampl_all_treated$pred.y <-
      predict(mod, sampl_all_treated, type = "response")

    sampl_all_untreated$pred.y <-
      predict(mod, sampl_all_untreated, type = "response")

    boots[i, "mean1"] <- mean(sampl_all_treated$pred.y)
    boots[i, "mean0"] <- mean(sampl_all_untreated$pred.y)
    boots[i, "difference"] <- boots[i, "mean1"] - boots[i, "mean0"]
    #coefs <- mod$coefficients[2,1:2]
    #tib_coef <- bind_rows(tib_coef, tibble(estimate = coefs[1]))
  }
  return(boots)
}

# ### input matched dataframe, output however many bootstrapped samples you want ###
# first, set seed vector for reproducibility

# now, define function

seed_vec_2 <- rnorm(100000, mean = 0, sd = 10000) %>% round(0) %>% unique()

simple_boot <- function(df, n, size = 500, seeds = seed_vec_2){
  boots <- list()
  pb2$tick()
```

```

for (i in 1:n) {
  set.seed(seeds[i])
  boots[[i]] <-
    df %>%
      filter(subclass %in% sample(levels(subclass),
                                   size,
                                   replace = TRUE))
}
return(boots)
}

# adding progress bars for sanity
pb2 <- progress_bar$new(format = "bootstrapping... [:bar] :percent eta: :eta",
                        total = length(df))
pb3 <- progress_bar$new(format = "bootstrapping... [:bar] :percent eta: :eta",
                        total = length(df))

# creating booted tibbles, applying functions through purr::map.
boot_tib <-
  matched_tib %>%
  mutate(
    boots = map(.x = data, ~simple_boot(.x, n = 100))
  ) %>%
  mutate(ATE = map(.x = boots, ~outcome_model_list(.x)))

```

Unnesting bootstrap coefficients

```

boot_estimates <-
  boot_tib %>%
  mutate(seq = seq(1:nrow(boot_tib))) %>%
  select(ATE, seq) %>% unnest(ATE)

```

Summary of 1000 bootstrap of 100 no boot

```

boot_result <-
  boot_estimates %>%
  group_by(seq) %>%
  summarize(mean_ATE = mean(difference),
            sd_mean_ATE = sd(difference),
            bias = mean_ATE - 0.15)

fig1 <-
  boot_result %>%
  ggplot(aes(x = sd_mean_ATE)) +
  geom_histogram(fill = "light blue", bins = 12, color = "black") +
  geom_density(aes(y = ..density..*0.07), colour = "red",
              fill = "black", alpha = 0.3) +
  geom_vline(xintercept = mean(boot_result$sd_mean_ATE), linetype = "dashed") +

```

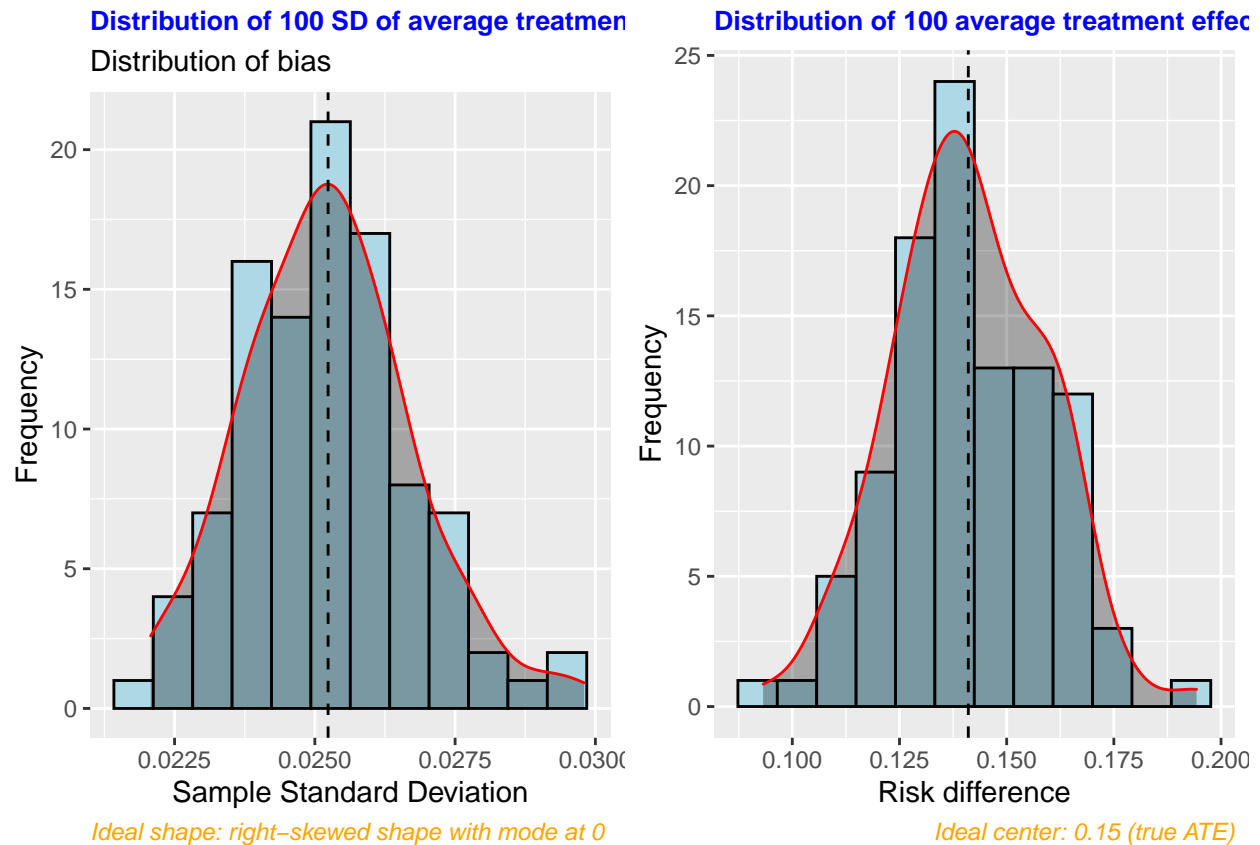
```

labs(title = "Distribution of 100 SD of average treatment effect",
      subtitle = "Distribution of bias",
      x = "Sample Standard Deviation", y = "Frequency",
      caption = "Ideal shape: right-skewed shape with mode at 0 ") +
theme(
plot.title = element_text(color = "blue", size = 10, face = "bold"),
plot.subtitle = element_text(color = "black"),
plot.caption = element_text(color = "orange", face = "italic")
)

fig2 <-
  boot_result %>%
  ggplot(aes(x = mean_ATE)) +
  geom_histogram(fill = "light blue", bins = 12, color = "black") +
  geom_density(aes(y = ..density..*1), colour = "red",
               fill = "black", alpha = 0.3) +
  geom_vline(xintercept = mean(boot_result$mean_ATE), linetype = "dashed") +
  labs(title = "Distribution of 100 average treatment effect",
       caption = "Ideal center: 0.15 (true ATE)",
       x = "Risk difference", y = "Frequency") +
  theme(
plot.title = element_text(color = "blue", size = 10, face = "bold"),
plot.caption = element_text(color = "orange", face = "italic")
)

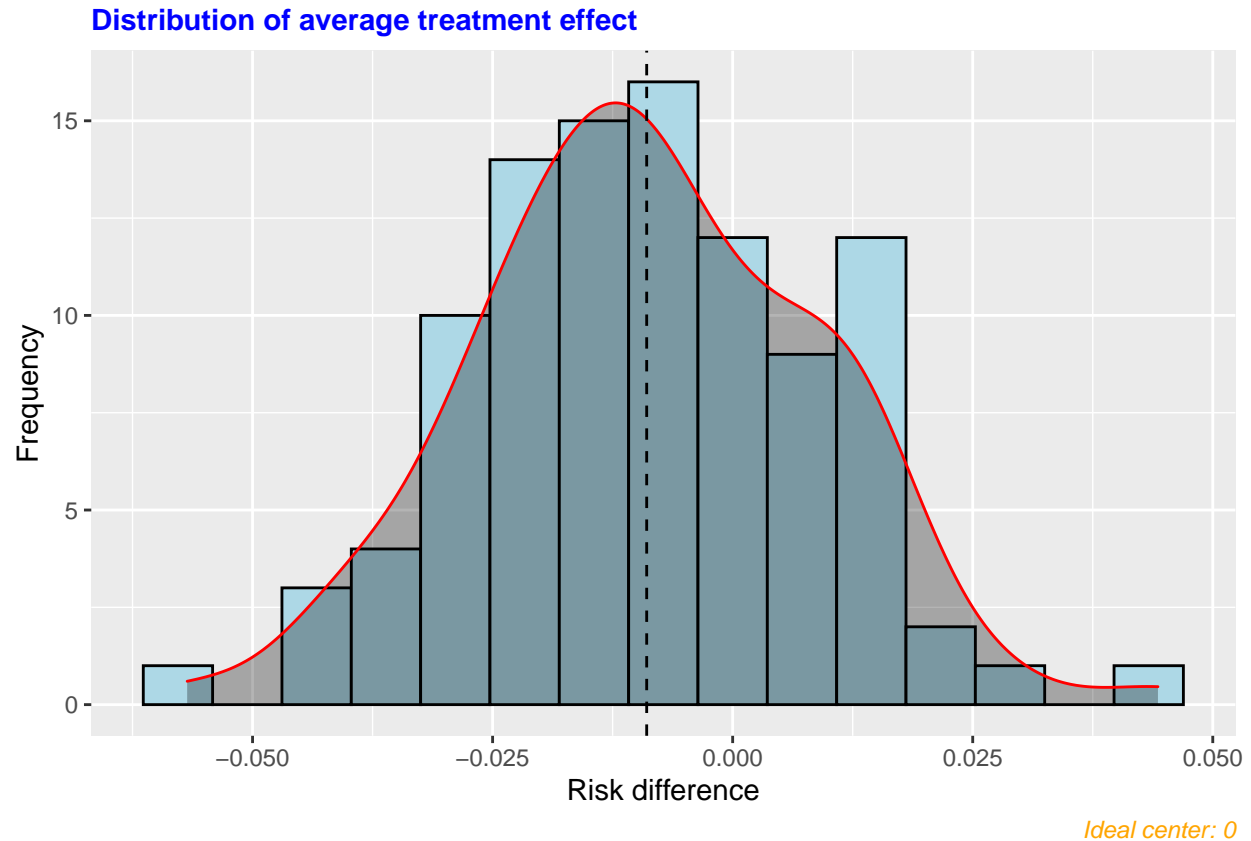
plot_grid(fig1, fig2)

```



```
fig3 <-
  boot_result %>%
  ggplot(aes(x = bias)) +
  geom_histogram(fill = "light blue", bins = 15, color = "black") +
  geom_density(aes(y = ..density..*0.7), colour = "red",
               fill = "black", alpha = 0.3) +
  geom_vline(xintercept = mean(boot_result$bias), linetype = "dashed") +
  labs(title = "Distribution of average treatment effect",
       caption = "Ideal center: 0", x = "Risk difference", y = "Frequency") +
  theme(
    plot.title = element_text(color = "blue", size = 11, face = "bold"),
    plot.caption = element_text(color = "orange", face = "italic")
  )

fig3
```



100 Confidence Intervals Coverage Rate using central limit theorem

```
CI_coverage_rate <- function(nboot){
  boot_CI_ATE <- list()
  count_true <- list()

  for (i in 1:nboot) {
    boot_CI_ATE[[i]] <-
      c(boot_result$mean_ATE[i] + qnorm(0.025)*sd(boot_result$mean_ATE),
        boot_result$mean_ATE[i] + qnorm(0.975)*sd(boot_result$mean_ATE))

    count_true[i] <-
      between(0.15, range(boot_CI_ATE[[i]])[1], range(boot_CI_ATE[[i]])[2])
  }

  result =
    as.vector(unlist(count_true)) %>%
    sum()
  result = paste0("CI coverage rate:", result, "%")

  return(result)
}

CI_coverage_rate(100)
```



```
## [1] "CI coverage rate:92%"
```

Sample mean central limit theorem to build confidence interval

```
(qnorm(0.025) * sd(boot_result$mean_ATE)) + 0.15 #Lower CI range
```

```
## [1] 0.1153242
```

```
(qnorm(0.975) * sd(boot_result$mean_ATE)) + 0.15 #Upper CI range
```

```
## [1] 0.1846758
```