27 pm 25

Def (G,) set GxG—G (a,b)—a,b=ab

(a) assoc. (ab) c=a(bc)

(b) therexists ell sit, al=ea-a frallalli.

(c) foresten at of their exists of st. a. a. a. a. e.

It a.b=b.a frale a,be6, we say that Gis commulative (abelian).

Examples (Z,+), (Zn,+), (R\*,·) (+ ´E)

(0)/b

(B) = ((a) b) | ad-bc = by

(Gholk),) group (not abelian).

Ex G1, G2 graps. Define GxG2= ((a,b)/at6, 3

f(xy) = f(x).f(x) frales f: 6, -> 62 st. (a, b). (c, d) - (ac, bd) Thun (G, x Bz), ) is a group. Signe homomorphisms Gi, Gz gramps

bipechir homm. Kerf = {x66, | f(x) = egg} Inf = 4 fro) 1 oc esty. Switzelite Morning. unjective hormm. mondamonam. · epimorphism 1 so mus phism

f mono (=) Ker f = {eg,} G, - G homm. Nun fisom == 5-7 (som

"== " Let on E ker f Thun f(x) = e2 = f(ea,) Writ Hu same operation, Equivalently, Hsahsfria.

(a) x,y CH => 2cy CH

(b) xcH => 2cy CH

(c) xcH => 2cy CH Ggramp, HCG, H+A St. HISaging Thus f(x,y) = f(x), f(y)) = f(x). f(y) & 27 E Kerf= {es,} , Then 2y = Es,) <= " f(x) = f(x) fr xy (e) But f mono, 80 2 = Co1 · + - 2 · 2 · ) Starten of Proof (1) Sampoduc

Hi & G frollier \*/hat is the smallest Subgrich 6 that · John R Tr nAM Mary () H! suppose of O Ggrap JHiljier even permutatins tons OUX エンリハメン (2) A S Sn NZ 52 (+ Z) (1) sydward S C I Xe CX

Need to prove: subgrape [ ] (X) (dear) Thus  $\langle X \rangle = \langle q_1, q_2, q_k | \alpha, \in X, k \in \mathbb{N}$ Front Pay pier, exercise (x) 15 a subgrate. that contrains X ( the subgr. gen. by X). Det It & H=< {at ..., any > We sou that Tun (X) is the smallest subgr. of 6 X X= 423 Q Thun (125) - 22 + 1 15 finitely generated. THE SUPSET

Flist, chuck that HIS a Bulgary. Bay Need to prove Subaki. School