

We define the following raw variables over each region of land  $\lambda_i \in \lambda$  in some region of land in Minnesota where  $\lambda$  is a land partition of Minnesota according to some rule (street, neighborhood, ..., city, county, district, ...) and  $i \in [1, |\lambda|] \cap \mathbb{N}$ . ex.)  $\lambda = \{\text{Ramsey, Anoka, St. Louis, ...}\}$  is a partition of Minnesota into counties.

$E_i :=$  average energy cost

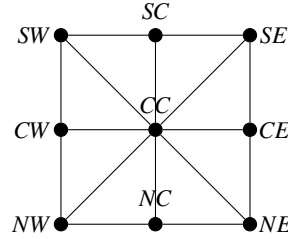
$T_i :=$  road density (number of roads per acre)

$Y_i :=$  average yield of corn ,sugarbeets ,soy, other grains (bushels/acre)

$N_i := \frac{\text{Nitrogen needed}}{\text{Crop Production Index}} \text{ (N/cpi)}$

Normalized Variables:

We translate the Minnesota district map; Minnesota partitioned by districts, to the graph  $G = (\lambda, E)$  below, where the vertices  $\lambda_i \in \lambda$  are districts and the edges represent a shared border or corner between vertices:



$$\lambda = \{\lambda_i \in \lambda \mid i \in [1, |\lambda|] \cap \mathbb{N}\} = \{SW, SC, SE, CW, CC, CE, NW, NC, NE\}.$$

Now, let  $f : \lambda \rightarrow \mathbb{R}^4$  be defined by  $f(\lambda_i) = \begin{pmatrix} \hat{E}_i \\ \hat{T}_i \\ \hat{Y}_i \\ \hat{N}_i \end{pmatrix}$ .  $f$  produces a tuple containing the normalized variables

for each of our districts  $\lambda_i \in \lambda$ . We now define our weight row vector as follows  $w = (16, 20, 24, 40)$  which scales  $\hat{E}_i, \hat{T}_i, \hat{Y}_i, \hat{N}_i$ , respectively, which are ranked in order from most to least important out of 100%. These weights are ordered according to most significant with respect to economic feasibility. Finally, we multiply  $f(\lambda_i)$  by  $w$  from the left in order to produce a linear combination for each district, once again centered around economic feasibility, which we call its rank  $R$ :

$$R(\lambda_i) = w f(\lambda_i) w$$

Finally, we select