## **Pixelwise Gaussian Entropy**

## Deriving our approximation of the entropy for the observations resulting from acquiring line $\ell$

We want to compute the entropy of  $p(y_t \mid A^{\ell}, y_{< t})$ 

We can choose to model  $p(x_t \mid y_{< t})$  as a pixelwise independent Gaussian, so that  $p(x_t \mid y_{< t}) = \mathcal{N}(x_t; \bar{x}_t, S_{x_t})$  where  $\bar{x}_t$  is the sample mean of the belief distribution (samples  $x_t \mid y_{< t}$ ), and  $S_{x_t}$  is the sample pixelwise variance, i.e. a diagonal covariance with entries  $\sigma^2_{x_t,i}$  for pixels i.

Given that the measurement model  $y_t = U(A^{\ell})x_t$  is linear (where  $U(A^{\ell})$  makes a matrix with 1s on the diagonal at indices contained in  $A^{\ell}$ ), we get that  $p(y_t \mid A^{\ell}, y_{< t})$  is a simple transformation of  $p(x_t \mid y_{< t})$ :

$$p(y_t \mid A^\ell, y_{< t}) = \mathcal{N}(y_t; U(A^\ell) ar{x}_t, U(A^\ell) S_{x_t} U(A^\ell)^ op)$$

The entropy of this distribution is then:

$$H(y_t \mid A^\ell, y_{< t}) = rac{1}{2} ext{log}((2\pi e)^M | U(A^\ell) S_{x_t} U(A^\ell)^ op |)$$

The matrix multiplications of  $S_{x_t}$  have the effect of selecting only the variances of the pixels revealed by  $A^{\ell}$ . Given that the determinant of a diagonal matrix is just the product of its diagonal, the entropy simplifies to:

$$H(y_t \mid A^\ell, y_{< t}) = rac{1}{2} \mathrm{log}((2\pi e)^M \prod_{i \in A^\ell} \sigma_{x_t, i}^2).$$

Bringing the product outside of the log to become a sum, we get finally:

$$H(y_t \mid A^\ell, y_{< t}) = \sum_{i \in A^\ell} rac{1}{2} \mathrm{log}((2\pi e)^{|A^\ell|} \sigma^2_{x_t, i})$$

In other words, the entropy of the measurement  $y_t$  observed by acquiring line  $\ell$  is equal to the sum of pixelwise entropies of the pixels revealed by  $\ell$ .