

# Python Performance for Plants and Profit

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# About me

PhD in computational physics

Former projects: Minix68k (68k FP Emulation), Linux libm.so.5 (High Precision FP), perl and python for epoc, flightgear, msktutil...

Member Apache Software Foundation

Backend Software Architect at Bosch eBike



# LUGT Mailinglist

Ein längeres Programm braucht bei meinem Kollegen 5 h und 10 Minuten, bei mir über 13 h.

# LUGT Mailinglist

Simulation Pflanzenbewegungen

# Inner Loop

```
for t in range(0,N):
    for ring in range(0,rings):
        for cell in range(0,ringsize):

            flux = .....

            # Perform Runge-Kutta integration on current cell
            x = X[t][ring][cell]
            y = Y[t][ring][cell]
            k11 = h*dXdt(x,y,flux)
            k12 = h*dYdt(x,y)

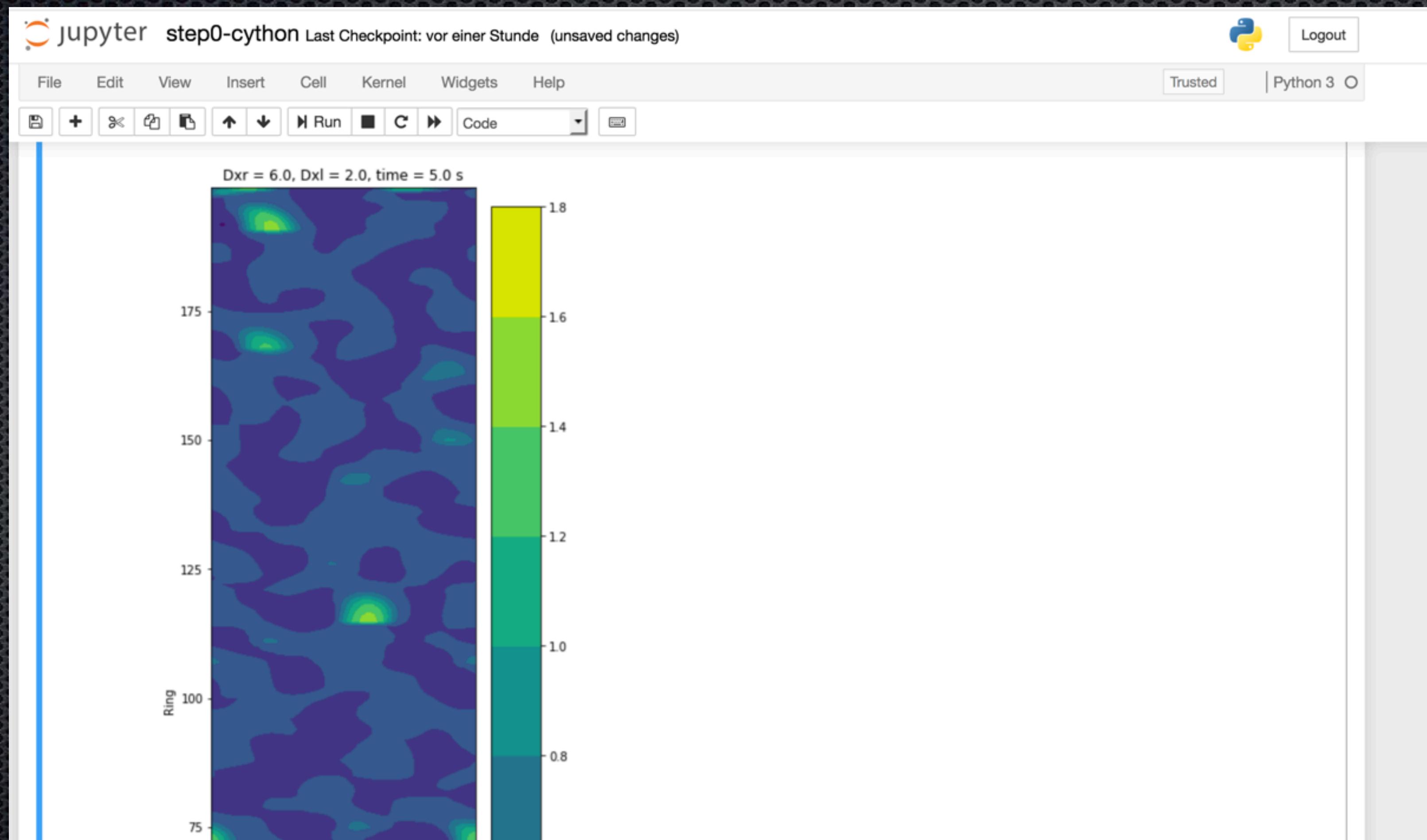
            k21 = h*dXdt(x+0.5*k11, y+0.5*k12,flux)
            k22 = h*dYdt(x+0.5*k11, y+0.5*k12)

            k31 = h*dXdt(x+0.5*k21, y+0.5*k22,flux)
            k32 = h*dYdt(x+0.5*k21, y+0.5*k22)

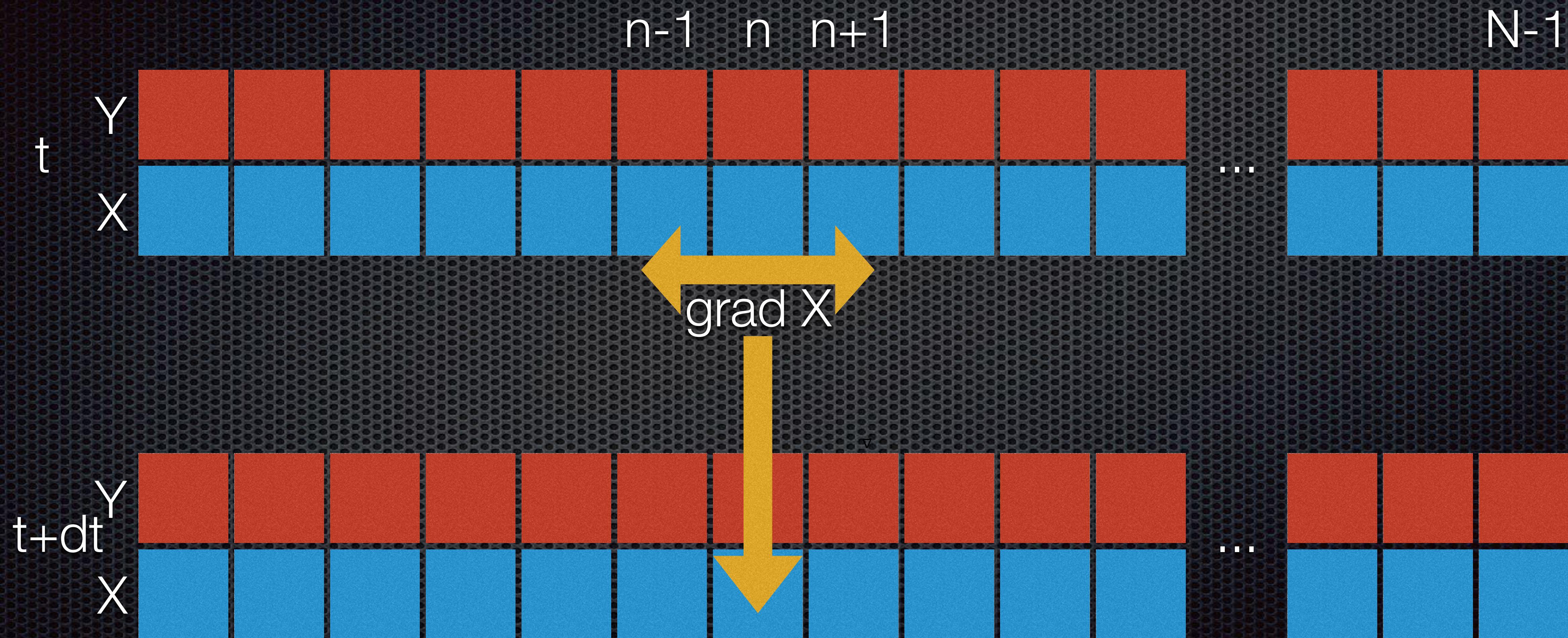
            k41 = h*dXdt(x+k31, y+k32,flux)
            k42 = h*dYdt(x+k31, y+k32)

            X[t+1][ring][cell] = x + (k11 + 2*k21 + 2*k31 + k41)/6
            Y[t+1][ring][cell] = y + (k12 + 2*k22 + 2*k32 + k42)/6
```

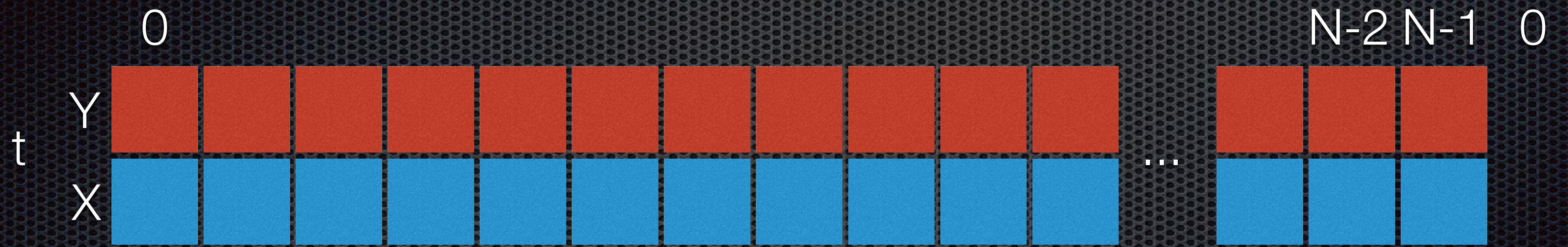
# Running in jupyter



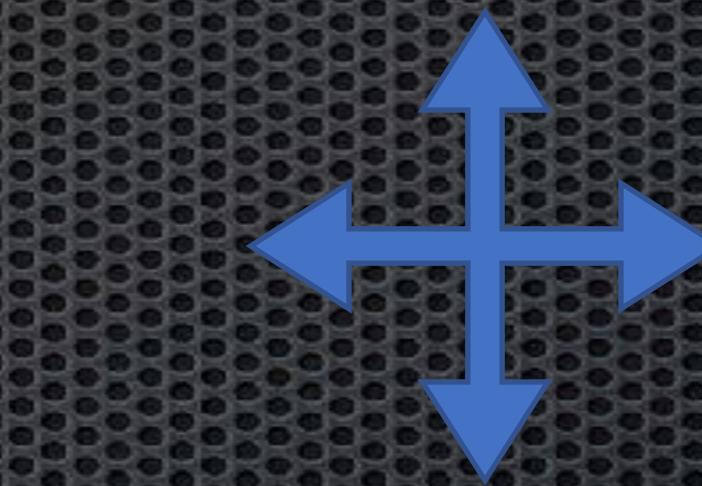
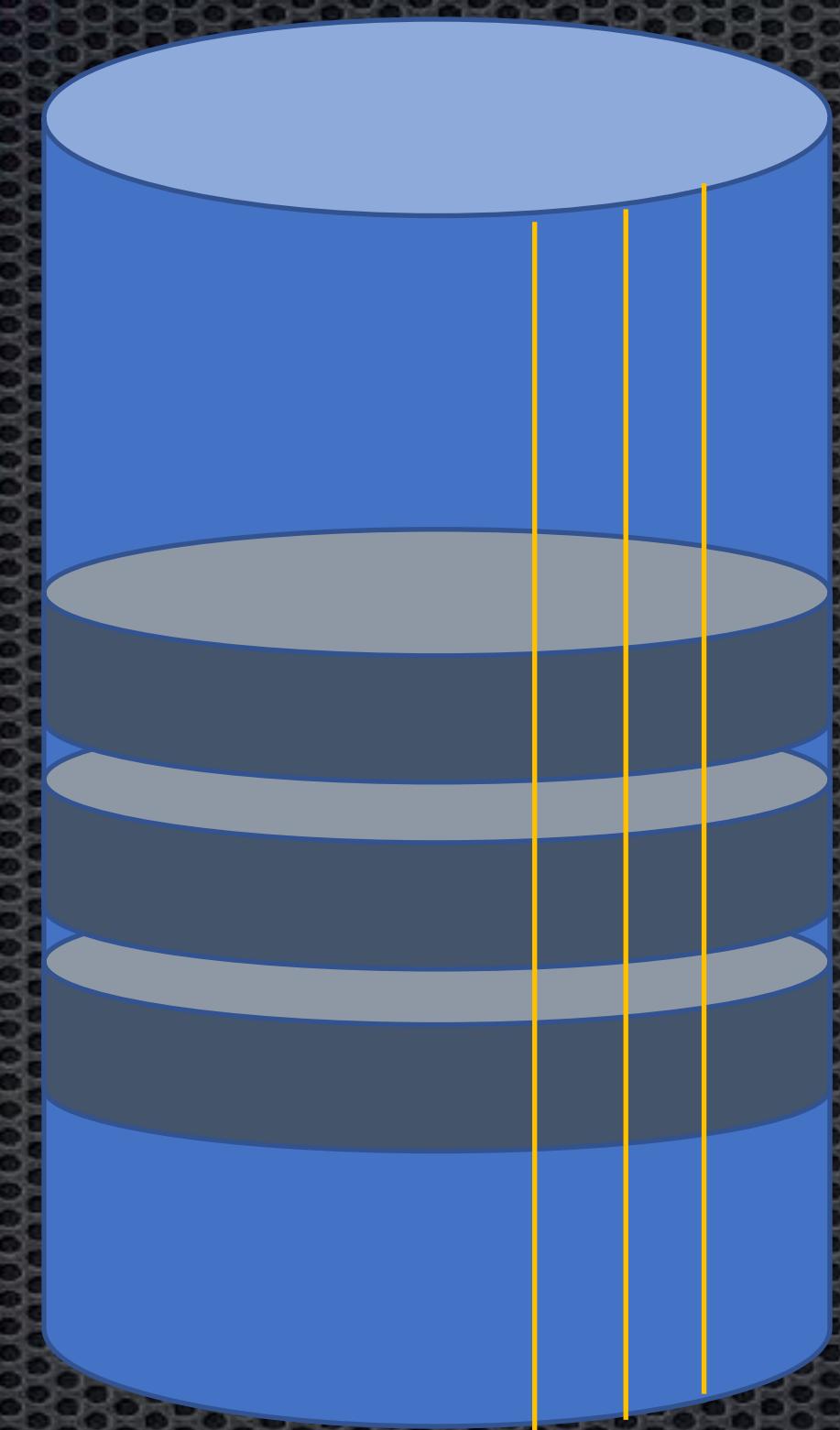
# Diskretisierte DGL



# Randbedingung : Ring



# Netztopologie



Horizontaler Gradient

Vertikaler Gradient wenn Richtung stimmt

# NumPy // python dynamische Typen

```
A = 1
```

```
A + 2 # 3
```

```
A = np.arange(3) # [0, 1, 2]
```

```
B = A + 1      # [1, 2, 3] elementwise
```

```
A + B          # [1, 3, 5] elementwise
```

```
A * B          # [0, 2, 6] elementwise
```

```
A ** 2         # [0, 1, 4] elementwise
```

# NumPy // python dynamic types

```
np.sin(A)          # elementwise sin  
np.greater(A,B)  # elementwise true/false if A[i] > B[i]  
  
A = np.arange(3)  
  
#example functions work both with scalar and vector  
  
def f(x) :  
    return x**2  
  
  
  
  
for i in range(0,3):          # b = f(a)  
    b[i] = f(a[i])
```

# Grundsätzliche Schleife

```
for t in range(0,N):  
    for ring in range(0,rings):  
        for cell in range(0,ringsize):
```

flux = ....

# Perform Runge-Kutta integration on current cell

x = X[t][ring][cell]

y = Y[t][ring][cell]

k11 = h\*dXdt(x,y,flux)

k12 = h\*dYdt(x,y)

k21 = h\*dXdt(x+0.5\*k11, y+0.5\*k12, flux)

k22 = h\*dYdt(x+0.5\*k11, y+0.5\*k12)

k31 = h\*dXdt(x+0.5\*k21, y+0.5\*k22, flux)

k32 = h\*dYdt(x+0.5\*k21, y+0.5\*k22)

k41 = h\*dXdt(x+k31, y+k32, flux)

k42 = h\*dYdt(x+k31, y+k32)

X[t+1][ring][cell] = x + (k11 + 2\*k21 + 2\*k31 + k41)/6

Y[t+1][ring][cell] = y + (k12 + 2\*k22 + 2\*k32 + k42)/6

Idee: Vectorisieren, viele voneinander  
unabhängige Gleichartige Berechnungen

# Profit

The tight internal loop is now done by numpy

Numpy uses optimized routines for vectors, matrices

BLAS (Basic Linear Algebra System)

These may be hand optimized to match processor

# Vectorisieren

SIMD: Single Instruction, Multiple Data

Voraussetzung: Keine Datenabhängigkeiten

Intel/AMD: AVX/AVX2, ... spezielle Register die mehrere FP aufnehmen können.

ARM: "Neon"

Dazu muss man den Code attributieren.

# Boundary conditions

```
flux = 0.0
```

```
# horizontal diffusion
```

```
if cell == 0:  
    flux = Dxr*(X[index][ring][ringsize-1] - X[index][ring][cell]) \  
        + DxI*(X[index][ring][1] - X[index][ring][cell])  
elif cell==ringsize-1:  
    flux = Dxr*(X[index][ring][cell-1] - X[index][ring][cell]) \  
        + DxI*(X[index][ring][0] - X[index][ring][cell])  
else:  
    flux = Dxr*(X[index][ring][cell-1] - X[index][ring][cell]) \  
        + DxI*(X[index][ring][cell+1] - X[index][ring][cell])
```

# Nachbarschaftsbeziehungen

```
# Boundary conditions will be handled automatically
```

```
xr = np.roll(X[index][ring], 1)
```

```
xl = np.roll(X[index][ring], -1)
```

```
flux = Dxr * (xr - X[index][ring]) + DxI * (xl - X[index][ring])
```

# boolean Indices

```
# vertical diffusion
    if X[index][ring-1][cell] > X[index][ring][cell]:
        flux += Dxd*(X[index][ring-1][cell] - X[index][ring][cell])
    if X[index][ring][cell] > X[index][ring+1][cell]:
        flux -= Dxd*(X[index][ring][cell] - X[index][ring+1][cell])

# Boolean indices !
d = np.greater(X[index][ring - 1], X[index][ring])

# d == True calc/do not calc corresponding value

# Array Access by Array of bools == Boolean index

flux[d] += Dxd * (X[index][ring - 1][d] - X[index][ring][d])
d = np.greater(X[index][ring], X[index][ring + 1])
flux[d] -= Dxd * (X[index][ring][d] - X[index][ring + 1][d])
```

# Problem numpy

- Viel mehr geht nicht...

# cython.org

**Cython** is an **optimising static compiler** for both the **Python** programming language and the extended Cython programming language (based on **Pyrex**). It makes writing C extensions for Python as easy as Python itself.

Cython gives you the combined power of Python and C to let you

- write Python code that calls back and forth from and to C or C++ code natively at any point.
- easily tune readable Python code into plain C performance by adding static type declarations.
- use combined source code level debugging to find bugs in your Python, Cython and C code.
- interact efficiently with large data sets, e.g. using multi-dimensional NumPy arrays.
- quickly build your applications within the large, mature and widely used CPython ecosystem.
- integrate natively with existing code and data from legacy, low-level or high-performance libraries and applications.

# Cython: Loop

Idee: Den Rechenkern von Cython optimieren lassen

```
for t in range(0,N):
    for ring in range(0,rings):
        timestep(X, Y, cylinderConcPerCell, index, ring, t, tau, omega, Am)
```

# Cython: timestep.pyx

```
cpdef timestep(X, Y, cylinderConcPerCell, index, ring, t, tau, omega, Am):  
    for cell in range(0,ringsize):  
        flux = ....  
  
        # Perform Runge-Kutta integration on current cell  
        x = X[t][ring][cell]  
        y = Y[t][ring][cell]  
        k11 = h*dXdt(x,y,flux)  
        k12 = h*dYdt(x,y)  
  
        k21 = h*dXdt(x+0.5*k11, y+0.5*k12,flux)  
        k22 = h*dYdt(x+0.5*k11, y+0.5*k12)  
  
        k31 = h*dXdt(x+0.5*k21, y+0.5*k22,flux)  
        k32 = h*dYdt(x+0.5*k21, y+0.5*k22)  
  
        k41 = h*dXdt(x+k31, y+k32,flux)  
        k42 = h*dYdt(x+k31, y+k32)  
  
        X[t+1][ring][cell] = x + (k11 + 2*k21 + 2*k31 + k41)/6  
        Y[t+1][ring][cell] = y + (k12 + 2*k22 + 2*k32 + k42)/6
```

Idee: Vectorisieren, viele voneinander unabhängige Gleichartige Berechnung

# Cython: optimize timestep.pyx

```
@cython.boundscheck(False)
cpdef timestep(double[:, :, :] X, double[:, :, :] Y, double[:, :] cylinderConcPerCell, int index,
              int ring, int t, int tau, double omega, double Am):
    cdef double flux
    cdef double x, y
    cdef double k11, k12, k21, k22, k31, k32, k41, k42
    cdef int cell
    flux = .....

    # Perform Runge-Kutta integration on current cell
    x = X[t][ring][cell]
    y = Y[t][ring][cell]
    k11 = h*dXdt(x,y,flux)
    k12 = h*dYdt(x,y)

    k21 = h*dXdt(x+0.5*k11, y+0.5*k12, flux)
    k22 = h*dYdt(x+0.5*k11, y+0.5*k12)

    k31 = h*dXdt(x+0.5*k21, y+0.5*k22, flux)
    k32 = h*dYdt(x+0.5*k21, y+0.5*k22)

    k41 = h*dXdt(x+k31, y+k32, flux)
    k42 = h*dYdt(x+k31, y+k32)

    X[t+1][ring][cell] = x + (k11 + 2*k21 + 2*k31 + k41)/6
    Y[t+1][ring][cell] = y + (k12 + 2*k22 + 2*k32 + k42)/6
```

Idee: typed memoryviews  
Schneller geht's nicht...

Leider funktioniert das nicht für  
Scalar \* Vector...

Deswegen ausgangsbasis ursprünglicher Code  
Step0

# Cython: Auszug aus timestep.c

```
/* "timestep.pyx":121
*
*      k42 = h*dYdt(x+k31, y+k32)
*
*
*      Xret = x + (k11 + 2*k21 + 2*k31 + k41)/6      # <<<<<<<<<
*      Yret = y + (k12 + 2*k22 + 2*k32 + k42)/6
*      X[(index+1)%tau][ring][cell] = Xret
*/
__pyx_v_Xret = (__pyx_v_x + (((__pyx_v_k11 + (2.0 * __pyx_v_k21)) + (2.0 * __pyx_v_k31)) + __pyx_v_k41) / 6.0);

/* "timestep.pyx":122
*
*
*      Xret = x + (k11 + 2*k21 + 2*k31 + k41)/6
*      Yret = y + (k12 + 2*k22 + 2*k32 + k42)/6      # <<<<<<<<
*      X[(index+1)%tau][ring][cell] = Xret
*      Y[(index+1)%tau][ring][cell] = Yret
*/
__pyx_v_Yret = (__pyx_v_y + (((__pyx_v_k12 + (2.0 * __pyx_v_k22)) + (2.0 * __pyx_v_k32)) + __pyx_v_k42) / 6.0);
```

# Bewertung

- Aufwändig:
  - Typdefinitionen
  - Keine Operationen scalar mit vector (Broadcasting)
- Raum für weitere Optimierungen (Compiler)
- Weit verbreitet

[numba.pydata.org](https://numba.pydata.org)

- JIT (Just in time) compiler für python, aufbauend auf LLVM
- Benötigt sehr viel Infrastruktur
- (Anaconda bringt alles mit)
- Integriert mit numpy (!)

# Logic from Numba

```
@njit(cache = True)
def ringdynamics( X, Y, cylinderConcPerCell, index, t, tau, h, omega, Am):
```

```
    for ring in range(rings):
        flux = ....
```

```
# Perform Runge-Kutta integration on current cell
```

```
x = X[index][ring]
y = Y[index][ring]
k11 = h * dXdt(x, y, flux)
k12 = h * dYdt(x, y)
k21 = h * dXdt(x + 0.5 * k11, y + 0.5 * k12, flux)
k22 = h * dYdt(x + 0.5 * k11, y + 0.5 * k12)
k31 = h * dXdt(x + 0.5 * k21, y + 0.5 * k22, flux)
k32 = h * dYdt(x + 0.5 * k21, y + 0.5 * k22)
k41 = h * dXdt(x + k31, y + k32, flux)
k42 = h * dYdt(x + k31, y + k32)
```

```
X[(index + 1) % tau][ring] = x + (k11 + 2 * k21 + 2 * k31 + k41) / 6
Y[(index + 1) % tau][ring] = y + (k12 + 2 * k22 + 2 * k32 + k42) / 6
```

Idee: Vectorcode als Funktion damit dieser annotiert werden kann

@njit: Fehler, wenn Optimierung nicht durchgeführt werden

# numba Bewertung:

- Sehr einfaches Handling
- Geht oder Geht nicht.
- Kann nicht komplettes numpy
- np.roll musste ersetzt werden durch "kompatible" Implementierung
- Verfügbarkeit eingeschränkt

# Was geht noch?

- Step 0 in "C" mit fixen Adresse

C

```
for (int ring = 0; ring < RINGS; ring++) {
    for (int cell = 0; cell < RINGSIZE; cell++) {
        double flux = 0.;

        double flux = ....
        float x = X[index][ring][cell];
        float y = Y[index][ring][cell];
        double k11 = h * dXdt(x, y, flux);
        double k12 = h * dYdt(x, y);

        double k21 = h * dXdt(x + 0.5 * k11, y + 0.5 * k12, flux);
        double k22 = h * dYdt(x + 0.5 * k11, y + 0.5 * k12);

        double k31 = h * dXdt(x + 0.5 * k21, y + 0.5 * k22, flux);
        double k32 = h * dYdt(x + 0.5 * k21, y + 0.5 * k22);

        double k41 = h * dXdt(x + k31, y + k32, flux);
        double k42 = h * dYdt(x + k31, y + k32);
        X[(index + 1) % TAU][ring][cell] = x + (k11 + 2 * k21 + 2 * k31 + k41) / 6;
        Y[(index + 1) % TAU][ring][cell] = y + (k12 + 2 * k22 + 2 * k32 + k42) / 6;
```

# Bewertung C

- Fixe Arrays sehr unflexibel
- Mehrdimensionale Dynamische Arrays sehr fehlerträchtig
- Binding über cython sehr einfach möglich
- Viel weiteres Optimierungspotential

# Resultate

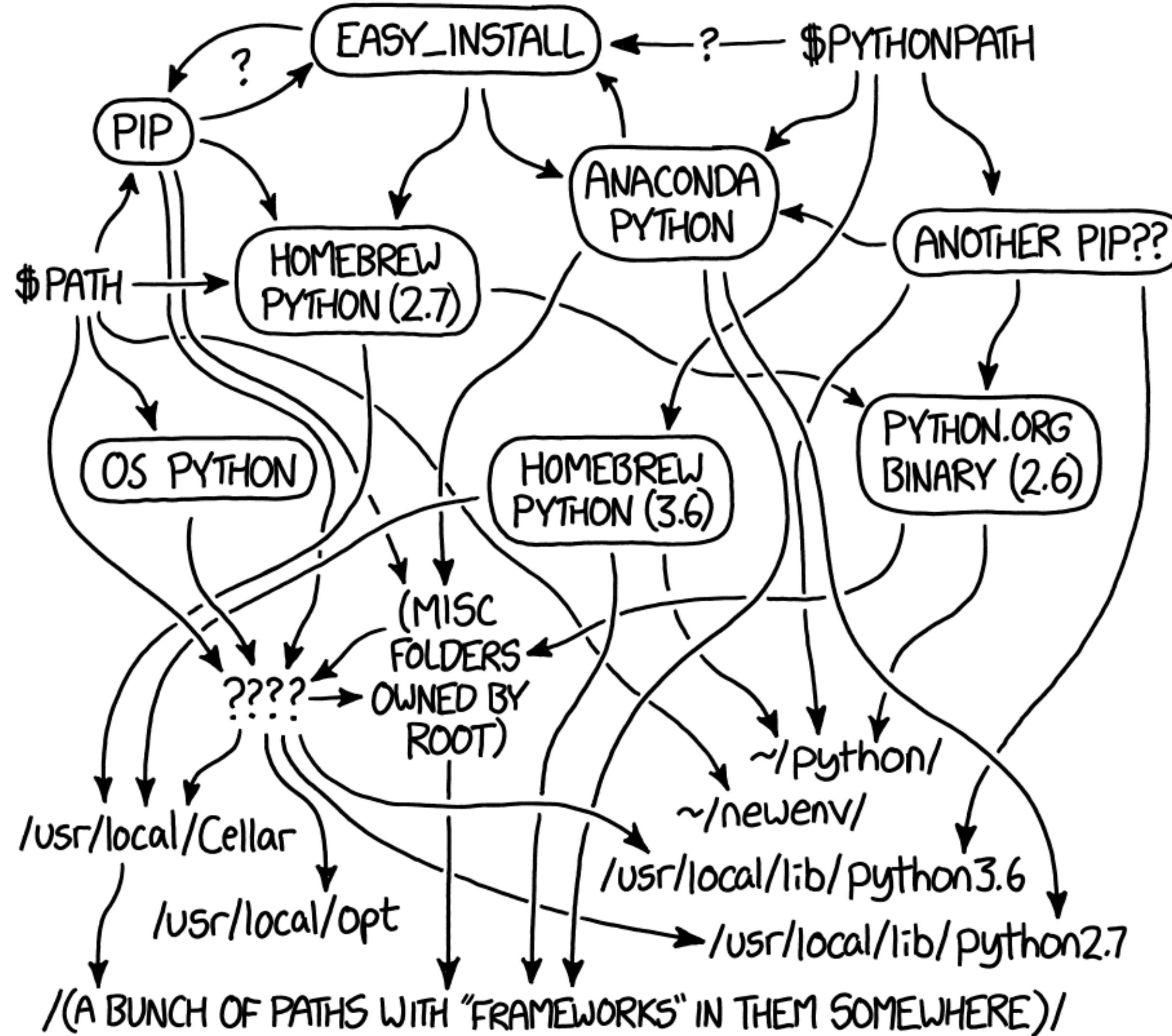
- step0: 125 sec
- step1/step2: 12sec
- step0 + optimites cython: 2sec
- step2 + optimiertes numba: 2sec
- step0 in C ohne matplotlib: 0.2sec

# Ergebnis

- Python ist langsam
- Numpy ist schneller
- Cython ist aufwändig, sehr schnell
- Numba ist sehr einfach && sehr schnell, Verfügbarkeit eingeschränkt
- Sowohl cython als auch numba integrieren gut in jupyter!
- C ist weiterhin am schnellsten.

# Zum Mitnehmen

- jupyter + matplotlib ist geil zum explorativen Arbeiten.
- numba ist der Star, wenn es funktioniert.
- C ist und bleibt: Ressourcenschonend, schnell, aber fehlerträchtig und aufwändig.
- C++ ist schwierig den richtigen Stil zu finden
- Virtual environments verwenden!



MY PYTHON ENVIRONMENT HAS BECOME SO DEGRADED  
THAT MY LAPTOP HAS BEEN DECLARED A SUPERFUND SITE.



Danke!

[github.com/oflebbe/pp4pp](https://github.com/oflebbe/pp4pp)  
of ät oflebbe dot de