## **EEEN 322 Communication Engineering** Homework 2

Due: 20.05.2019

## Problem 1 (30 points)

Suppose that  $m(t) = 5\cos 3000\pi t$  is the message signal to be frequency-modulated.

- a) Calculate the bandwidth of the modulated signal, if the modulation is NBFM.
- b) For WBFM with bandwidth  $B_{FM} \approx 2\Delta f$ , find the smallest value of  $k_f$ . (Let << and >> mean "at least ten times" smaller and greater, respectively).
- c) For the value of  $k_f$  found in (b), what is the bandwidth of the modulated signal?

## Problem 2 (30 points)

Suppose that the message signal is  $m(t) = 6\cos 2000\pi t - 2\sin 4000\pi t$ ,  $\omega_c = 10^6$  rad/s, A = 5, and  $k_f = 10^5 \pi$ .

- a) Write the expression of  $\varphi_{FM}(t)$  (use the indefinite integral of m(t)).
- b) Calculate the bandwidth of  $\varphi_{FM}(t)$ .
- c) What should be the value of  $k_p$  for  $\varphi_{PM}(t)$  to have the same bandwidth as that of  $\varphi_{FM}(t)$ ?
- d) Write the expression of  $\varphi_{PM}(t)$  by using the  $k_p$  value you have found in (c).

## Problem 3 (40 points)

Suppose that we perform FM and PM modulations with  $\,k_{_f} = 20000\pi\,$  and  $\,k_{_p} = 10\pi\,$ . The following information are given for m(t):

- (i)  $m_p = 2$
- (ii)  $m'_p = 4000$
- (iii) Bandwidth is 2500 Hz.
  - a) Calculate the bandwidths of FM and PM modulated signals obtained using m(t)as the message signal.
  - b) Calculate the bandwidths of FM and PM modulated signals obtained using  $m^2(t)$ as the message signal.
  - c) Comment on the differences of the bandwidths you have calculated in (a) and (b) referring to the differences in FM and PM modulations.