

controls = (dNumber, PNumber) Explicit implementation of "controls"
Easy & recommended (for now)

has assigned = (dNumber, SSN)

is managed by = (dNumber, SSN, startdate)

works = (SSN, PNumber, hour)

supervisor = (SSN-up, SSN-down)

dependent of = (SSN, fname)

Relational Schema

DEPARTMENT = (dNumber, dName)

DEPT-LOC = (dNumber, dloc)

EMPLOYEE = (SSN, ename, address, salary, birthdate, sex)

DEPENDENT = (fname, SSN, relationship, birthdate, sex)

Relational Algebra

Operators

SELECT Symbol = σ (sigma)

syntax = σ

$\langle \text{selection condition} \rangle (R)$

where selection condition is boolean expression on the attributes of R

R = relational algebra expression

EMPLOYEE

<u>e-id</u>	<u>ename</u>	<u>es-ename</u>	<u>sex</u>	<u>salary</u>
e001	Fce	Fce	F	50
e050	Oya	Fce	F	20
e100	Fce	Ece	F	70
e2	Afi	Omer	M	20

Type

attributes

sonradan
extendi

Use relational algebra to select all employees with salary > 30

out of EMPLOYEE relation $R_1 \leftarrow \sigma_{\langle \text{salary} > 30 \rangle} (\text{EMPLOYEE})$

Use RA to select all emp. having name = Ece and salary > 20

$$R_2 \leftarrow \sigma (\text{EMPLOYEE})$$

$$\langle \text{ename} = \text{Ece} \rangle \text{ AND } \langle \text{salary} > 20 \rangle$$

$$R_2 \leftarrow \sigma \left(\begin{array}{l} \sigma (\text{EMPLOYEE}) \\ \langle \text{ename} = \text{Ece} \rangle \quad \langle \text{salary} > 20 \rangle \end{array} \right)$$

Cardinality = number of tuple $| \sigma (R) | \leq | R |$

Degree = number of attribute

$$\text{degree} (\text{EMPLOYEE}) = 4$$

SELECT operator does not change the degree

$$\text{Card} (\text{EMPLOYEE}) = 4 \quad (\text{Tuples, rows})$$

$$| \text{EMPLOYEE} | = 4$$

$$\text{Card} (R_1) = 2$$

$$\text{Card} (R_2) = 1$$

PROJECT symbol = Π

$$\text{syntax} = \Pi (R)$$

list attribute

Use RA to select <e-id, salary> attribute out of EMPLOYEE

$$R_3 \leftarrow \Pi (\text{EMPLOYEE})$$

$$\text{degree} = 2$$

$$\langle \text{e-id, salary} \rangle$$

$$\text{card} = 4$$

Use RA to project EMPLOYEE over salary

$R_4 \leftarrow \pi_{\text{salary}}(\text{EMPLOYEE})$

$\text{degree}(R_4) = 1$

$\text{card}(R_4) = 3$ duplicate sayma

R_4

salary
50
20
70

Use RA to retrieve all info of female employees

$\text{Result} \leftarrow \sigma_{\langle \text{sex} = \text{F} \rangle}(\text{EMPLOYEE})$

$\text{card}(\text{Result}) = 3$

$\text{degree}(\text{Result}) = 5$

Use RA to retrieve all info of employee having frame = Ece

$R_2 \leftarrow \sigma_{\langle \text{frame} = \text{Ece} \rangle}(\text{EMPLOYEE})$

$\text{card}(R_2) = 2$

$\text{degree}(R_2) = 5$

Use RA to retrieve all info of employees having frame = Ece and salary ≥ 50

$R_3 \leftarrow \sigma_{\langle \text{frame} = \text{Ece} \rangle \text{ AND } \langle \text{salary} \geq 50 \rangle}(\text{EMPLOYEE})$

$\text{card}(R_3) = 2$

$\text{degree}(R_3) = 5$

Use RA to retrieve frame and salary of all employees

$R_4 \leftarrow \pi_{\langle \text{frame}, \text{salary} \rangle}(\text{EMPLOYEE})$

$\text{degree}(R_4) = 2$

$\text{card}(R_4) = 4$

Use RA to retrieve frame and salary of female employees

$Temp1 \leftarrow \sigma (EMPLOYEE)$ degree = 5
 $\langle sex = F \rangle$ card = 3

$R_5 \leftarrow \pi (Temp1)$ degree = 2
 $\langle frame, salary \rangle$ card = 3

$R_5 \leftarrow \pi (\sigma (EMPLOYEE))$
 $\langle sex = F, frame, salary \rangle$

UNION, INTERSECTION and MINUS Syntax: $R \cup S$, $R \cap S$, $R - S$

R and S must be union compatible. They must have same number of attribute.

$$\left. \begin{array}{l} R(A_1, A_2, \dots, A_n) \\ S(B_1, B_2, \dots, B_n) \end{array} \right\} \begin{array}{l} n = m \\ \forall i = 1 \dots n \end{array} \quad \begin{array}{l} \text{dom}(A_i) = \text{dom}(B_i) \end{array}$$

Kıtaptaki örnek

degree (STUDENT) = 2 degree (INSTRUCTOR) = 2

card (STUDENT) = 7 card (INSTRUCTOR) = 5

$T = \text{STUDENT} \cup \text{INSTRUCTOR}$

degree (T) = 2

card (T) = 10

Company Database örneği

Retrieve the SSN of all employees who either work in DNOS or directly supervise an employee from DNOS

$DEPTS_EMP \leftarrow \sigma (EMPLOYEE)$ degree (DEPTS_EMP) = 10
 $\langle DNO = 5 \rangle$ card (DEPTS_EMP) = 4

$SSN_DEPTS_EMP \leftarrow \pi_{\langle SSN \rangle} (DEPTS_EMP)$ degree = 1
 card = 4

$SSN_SUPERVISE \leftarrow \pi_{\langle super_ssn \rangle} (DEPTS_EMP)$ degree = 1
 card = 2

$R = SSN_DEPTS_EMP \cup SSN_SUPERVISE$

Cartesian Product

Syntax: $R \times S$

Semantic: $Q = R(A_1, A_2, \dots, A_n) \times S(B_1, B_2, \dots, B_n)$

$Q(A_1, A_2, \dots, A_n, B_1, B_2, \dots, B_n)$

degree(Q) = degree(R) + degree(S)

If $|R| = n_r$ and $|S| = n_s$ then $|Q| = n_r \times n_s$

Use RA to retrieve the name of the female dependent of each employee together with "frame" and "lname" of employee

$FEM_DEP \leftarrow \pi_{\langle ESSN, Dependent-name \rangle} (\sigma_{\langle sex=F \rangle} (DEPENDENT))$ degree = 2
 card = 4

$Temp \leftarrow FEM_DEP \times EMPLOYEE$ degree = $10 + 2 = 12$
 card = 8×4

$Result \leftarrow \pi_{\langle Frame, Lname, Dependent-name \rangle} (\sigma_{\langle ESSN=SSN \rangle} (TEMP))$ degree = 3
 card = 4

Reflexive relationship = (SSN, SuperSSN)

Date

No

Use RA query to retrieve the LName of all employees working in DNO = 5.

$TEMP \leftarrow \sigma_{DNO=5}(EMPLOYEE)$ degree(TEMP) = 10
card(TEMP) = 4

$R \leftarrow \pi_{LName}(TEMP)$ degree = 1
card = 4

Use RA query to retrieve PName of all project located in Stafford

$R \leftarrow \pi_{PName}(\sigma_{PLocation=Stafford}(PROJECT))$ degree = 1
card = 2

Use RA query to retrieve the SSN of the manager of the Research Department.

$Temp \leftarrow \sigma_{Dname=Research}(DEPARTMENT)$ degree = 4
card = 1

$R \leftarrow \pi_{Mgr-SSN}(Temp)$ degree = 1
card = 1

Use RA query to retrieve the FName of the manager of the Research Department.

$SSN_Mgr_Res \leftarrow \pi_{Mgr-SSN}(Temp)$

$All \leftarrow EMPLOYEE \times SSN_Mgr_Res$ degree(All) = 11

card(All) = $8 \times 1 = 8$

Interesting-All $\leftarrow \sigma$ (All)
 SSN = Mgr-SSN

All & Interesting-All
 \downarrow

Result $\leftarrow \pi$ (Interesting-All)
 FName

Interesting-All \leftarrow EMP \bowtie SSN
 SSN = Mgr-SSN

Use RA to retrieve the FName of employees who works less than 30 hours in at least 1 project.

less-than-30 $\leftarrow \sigma$ (WORKS-ON)
 Hrs < 30

degree (less-than-30) = 3

card (less-than-30) = 12

ESSN-less-30 $\leftarrow \pi$ (less-than-30)
 ESSN

degree (ESSN-less-30) = 1

card (ESSN-less-30) = 7

Temp1 \leftarrow EMPLOYEE \times ESSN-less-30 degree (Temp1) = 11

card (Temp1) = 56

Temp2 $\leftarrow \sigma$ (Temp1)
 ESSN = SSN

degree (Temp2) = 11

card (Temp2) = 7

Result $\leftarrow \pi$ (Temp2)
 FName

degree (Result) = 1

card (Result) = 6

EMPLOYEE \bowtie ESSN-less-30
 ESSN = SSN

Functional Dependency: It is a constraint between 2 sets of attributes.

Ex: $R(A_1, A_2, \dots, A_n)$

$X = \{A_1, A_2\}$ $Y = \{A_3, A_4\}$

fd: $X \rightarrow Y$

for every 2 tuples, t_1 and t_2 in the snapshot

$t_1[X] = t_2[X] \xrightarrow{\text{then}} t_1[Y] = t_2[Y]$

Ex:

In EMPLOYEE $X = \{SSN\}$ $Y = \{Bdate\}$

fd1: $X \rightarrow Y$ It is correct because if

$t_1[X] = t_2[X]$ I have 2 rows with the same SSN
 $t_1[Y] = t_2[Y]$

Ex: WORKS_ON fd2: $X \rightarrow Y$ $X = \{ESSN\}$ $Y = \{Hours\}$

If $t_1[X] = t_2[X] \rightarrow t_1[Y] = t_2[Y]$ wrong
 32.5 7.5

Ex:

EMPLOYEE + PROJECT + WORKS ON

SSN	PNumber	Hours	Ename	Pname	Plocation
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fd1 = $\{SSN\} \rightarrow \{Ename\}$

<u>SSN</u>	<u>PNumber</u>	Hours
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fd2 = $\{Pnumber\} \rightarrow \{Pname, Plocation\}$

fd3 = $\{SSN, Pnumber\} \rightarrow \{Hours\}$

<u>SSN</u>	<u>Ename</u>
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Partial Dependency \Rightarrow ~~2NF~~

<u>Pnumber</u>	<u>Pname</u>	<u>Plocation</u>
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Diagram illustrating a record structure with fields: Fname, SSN, Bdate, Address, Number, Dname, and DUGSSN. Red arrows point to Fname, SSN, Bdate, and Address. Blue arrows point to Dname and DUGSSN. A 'Date' label is above the Bdate field, and an 'ID' label is above the Dname field.

$$fd1 = \{SSN\} \rightarrow \{Ename, Bdate, Address, DNumber\}$$

$$fd2 = \{ DNumber \} \rightarrow \{ DName, DMGSSN \}$$

Transitive Dependency \Rightarrow ~~3NF~~

SSN	Ename	Bdate	Address	Number
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ΔNumber	ΔName	ΔMSSN
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