

14.03.18 - PS 12

2.)  $m(t) = e^{-t^2}$

$f_c = 10^4 \text{ kHz}$

$k_f = 6000\pi$

$k_p = 8000\pi$

$B = \sqrt{\frac{1}{2\pi}} \cdot e^{-\frac{\omega^2}{2}}$   
 $\frac{1}{\sigma} = \frac{1}{\sqrt{2\pi}}$

a) Table 3.1.  $\rightarrow e^{-\frac{t^2}{2\sigma^2}} \longleftrightarrow \sigma \sqrt{2\pi} e^{-\frac{\sigma^2 \omega^2}{2}}$   
 $e^{-t^2} \longleftrightarrow \sqrt{\frac{1}{2\pi}} \cdot e^{-\frac{\omega^2}{2} \cdot \frac{1}{2}} = \sqrt{\pi} \cdot e^{-\frac{\omega^2}{4}} = M(\omega)$   
 $\sigma = \sqrt{1/2}$

$M(\omega) = \sqrt{\pi} \cdot e^{-\omega^2/4}$

$m_p = [m(t)]_{\max} = (e^{-t^2})_{t=0} = 1$

$\dot{m}(t) \leftrightarrow j\omega M(\omega)$   
 $= j\sqrt{\pi} \omega e^{-\omega^2/4}$

FM  $\rightarrow \Delta f = \frac{k_f \cdot m_p}{2\pi} = \frac{6000\pi \times 1}{2\pi} = 3000 = 3 \text{ kHz}$

$B_{FM} = 2(B + \Delta f) \approx 2\Delta f = 6 \text{ kHz} \quad (\Delta f \gg B)$

PM  $\rightarrow \Delta f = \frac{k_p \cdot \dot{m}_p}{2\pi} \rightarrow \dot{m}(t) = -2t \cdot e^{-t^2}$

To find  $\dot{m}_p \rightarrow \ddot{m}(t) = 0$

$\ddot{m}(t) = -2 \cdot e^{-t^2} + 2t \cdot 2t \cdot e^{-t^2}$   
 $= -2e^{-t^2/2} + 4t^2 \cdot e^{-t^2} = 0$

$t = 1/\sqrt{2}$



$$\dot{m}\left(\frac{1}{\sqrt{2}}\right) = \dot{m}_p = 0.858$$

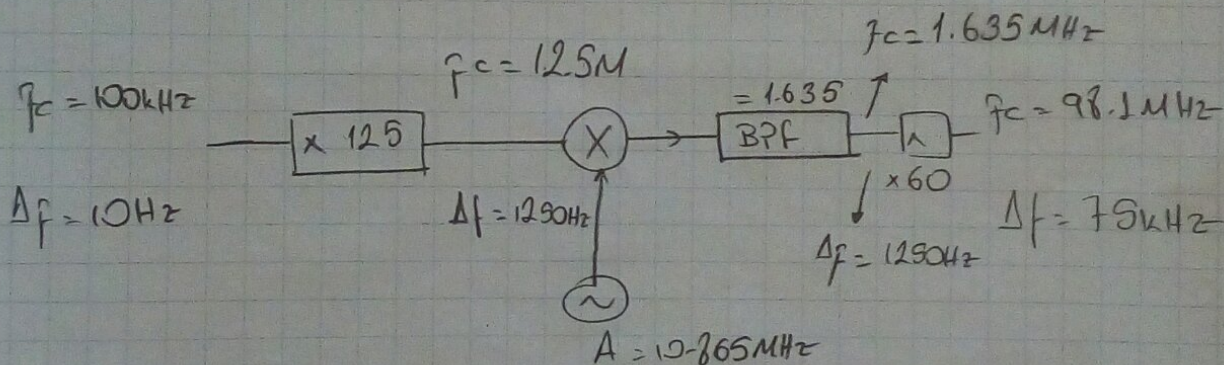
$$\Delta f = \frac{k_f \cdot \dot{m}_p}{2\pi} = \frac{8000\pi \times 0.858}{2\pi} = \underline{\underline{3.432 \text{ kHz}}}$$

$$B_{PM} = 2(B + \Delta f) \approx 2\Delta f = \underline{\underline{6.864 \text{ kHz}}}$$

$\Rightarrow$  Com. freq = 98.1 MHz  
 $\Delta f = 75 \text{ kHz}$

$\textcircled{1} \left\{ \begin{array}{l} \text{FM gen.} = 100 \text{ kHz} \\ \Delta f = 10 \text{ Hz} \end{array} \right.$

Osc. = 10-11 MHz



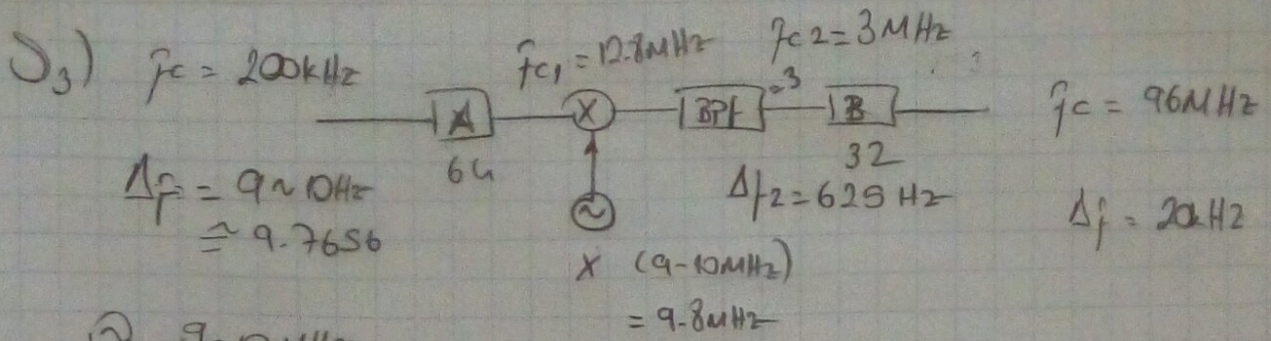
$$\frac{\Delta f_{\text{rest}}}{\Delta f_{\text{fst}}} = \frac{75 \times 10^3 \text{ Hz}}{10 \text{ Hz}} = \frac{7500}{125 \times 60}$$

$$f_c = 12.5 \text{ MHz}$$

$$\rightarrow 12.5 - A = 1.635$$

$$\rightarrow \underline{\underline{A = 10.865 \text{ MHz}}}$$





$$\frac{\Delta f}{\Delta f} = \frac{20000}{9} \approx 2222$$

$$2000 < A \cdot B < 2222$$

$$\text{or } \frac{2000}{10} \approx 2000$$

Only frequency doublers are available:

$$A = 2^{n_1} > 65 \rightarrow n_1 = 6 = 64 \rightarrow A \cdot B = 2048$$

$$B = 2^{n_2} \quad n_2 = 5 = 32$$

$$\left[ \begin{array}{l} f_c \times A > X_{\min} (= 9 \text{ MHz}) \\ 2 \times 10^5 \times A > 9 \cdot 10^6 \\ A > 45 \end{array} \right]$$

$$f_{c1} = 200 \text{ kHz} \times 64 = 12.8 \text{ MHz}$$

$$f_{c2} = \frac{96 \text{ MHz}}{32} = 3 \text{ MHz}$$

$$f_{c1} - X = 3 \text{ MHz}$$

$$12.8 - X = 3$$

$$X = 9.8 \text{ MHz}$$