EEEN 352 System Dynamics and Control

Homework 03

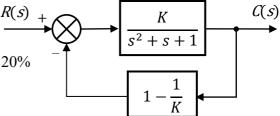
Due: 01-May-2020 Friday 23:59

Problem 1) For the unity-feedback system given, where

$$G(s) = \frac{K}{s(s+10)}$$

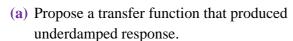
- R(s) + G(s)
- (a) Obtain the closed-loop transfer function and calculate the value of gain *K* in order to obtain a 12% overshoot to a unit step input
- (b) Propose a new underdamped system to produce unit step response with the same percent overshoot and steady-state value but two times faster in terms of settling time.
- (c) Write the unit step response in a general form.
- (d) Sketch the time responses for (a) and (b) on the dame plane.

Problem 2) For the system given in the figure on the right-hand side, where the input is unit step.

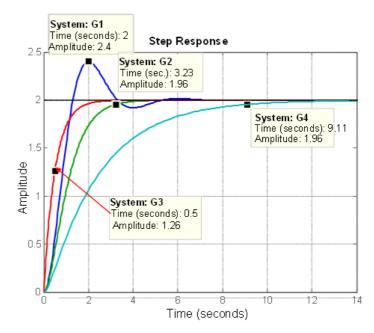


- (a) Find the value of gain *K* that yields maximum 20% overshoot,
- (b) Find the peak time for this gain,
- (c) Find the settling time for this gain,
- (d) Find the value of gain K to obtain the fastest response without any oscillation.

Problem 3) Considering the four different unit step responses plotted on the right-hand side.



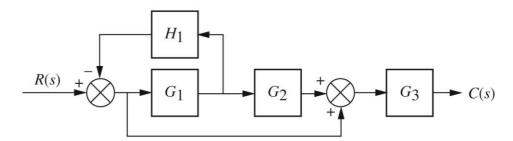
- (b) Write a general expression for the response of G1.
- (c) What would be the order of the system G3? Why? Propose a transfer function.
- (d) Which system would be critically damped? Why? Write its transfer function with the same ω_n of G1.



$$T_p = \frac{\pi}{\omega_n \sqrt{1-\zeta^2}}, T_s \cong \frac{4}{\zeta \omega_n}, \%OS = 100. e^{-\zeta \pi/\sqrt{1-\zeta^2}}, \zeta = \frac{-\ln(\%OS/100)}{\sqrt{\pi^2 + \ln^2(\%OS/100)}}, \lim_{t \to \infty} f(t) = \lim_{s \to 0} sF(s), p. 1 \text{ of } 2$$

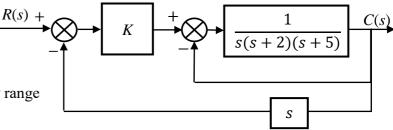
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Problem 4) Find the closed-loop transfer function, T(s) = C(s)/R(s) for the system presented below.



Problem 5) For the feedback control system given in the figure below,

- (a) Find the closed-loop transfer function, T(s) = C(s)/R(s),
- **(b)** Determine the system's stability range for gain *K* using Routh-Hurwitz criterion,



- (c) The system type for K=20 (convert the system to a simple unity feedback),
- (d) The steady-state error for an input step of 5u(t) for this gain,
- (e) The steady-state error for an input ramp of 5tu(t) for this gain.

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