CMPE 222 Spring 2018

How to prove that a language L is not regular using pumping lemma

We use pumping lemma *only* to prove that a given language is nonregular. We do this by using **proof by contradiction**. Here are the steps:

- 1. Assume that L is regular.
- 2. If L is regular then, according to pumping lemma:

 $\exists p \in \mathbb{Z}^+$ such that, $\forall s \in L$, if $|s| \ge p$ then s can be **pumped**. Remember that if a string s can be **pumped** it means that s can be divided into three segments, i.e. s = xyz such that:

- lyl > 0
- |xy| ≤ p
- $\forall i \ge 0$, $xy^iz \in L$. (See that this is equivalent to xy^*z)
- 3. Find a string s which is longer than p.
- 4. Show that no matter how you segment s such that |y| > 0 and $|xy| \le p$, it is not the case that $\forall i \ge 0$, $xy^iz \in L$.

(If it turns out that s can be indeed pumped, then this particular s is an unlucky choice. In this case, look for another string s).

5. s (which you have shown that it can not be pumped) is a counterexample. I.e. although $s \ge p$, it can not pumped. Thus, our assumption that L is regular is not true. Therefore L is nonregular.

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