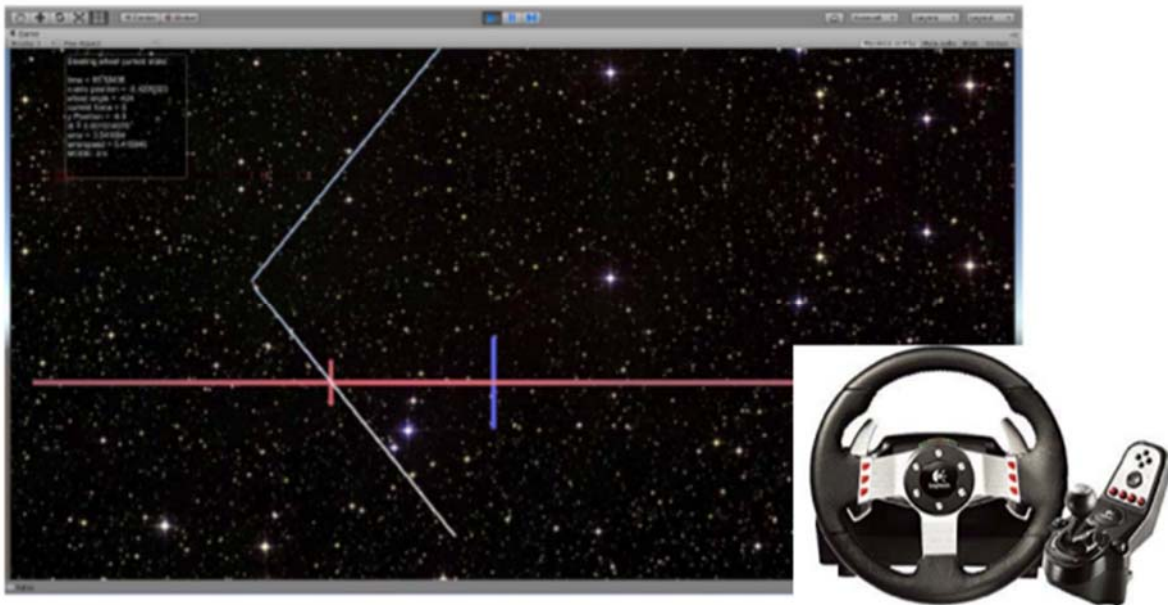


# Analysis of Human Sensorimotor Performance in Challenging Multitasking Control



Sung Hoon Choi  
Fred and Jean Felberg SURF Fellow  
Doris S. Perpall Competition Semi-Finalist  
Mentor: John C. Doyle

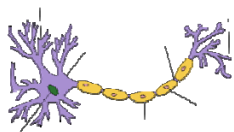
# Analysis of Human Sensorimotor Performance in Challenging Multitasking Control

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## Question about human nervous system

### Human nervous system (sensorimotor control)

#### Hardware level (neurons)



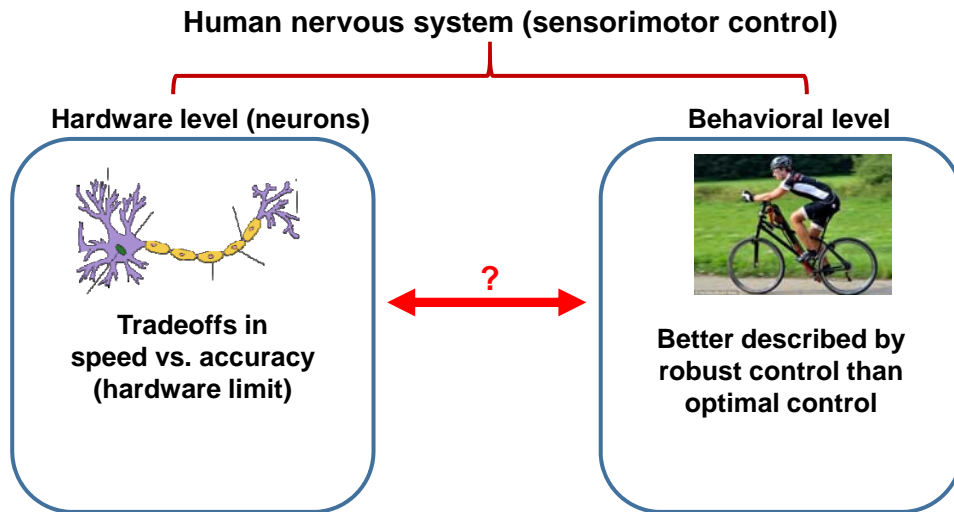
Tradeoffs in  
speed vs. accuracy  
(hardware limit)

#### Behavioral level



Better described by  
robust control than  
optimal control

## Question about human nervous system



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## Behavioral Level

3

## Motion tracking in presence of head motion

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1. Oscillate your hand horizontally back and forth, increasing the frequency until the lines blur
2. Hold your hand still and shake your head horizontally at increasing frequencies until blurring occurs

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## Motion tracking in presence of head motion

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1. Oscillate your hand horizontally back and forth, increasing the frequency until the lines blur  
-> blurs in 1~2 Hz.
2. Hold your hand still and shake your head horizontally at increasing frequencies until blurring occurs  
-> blurs at much higher frequency

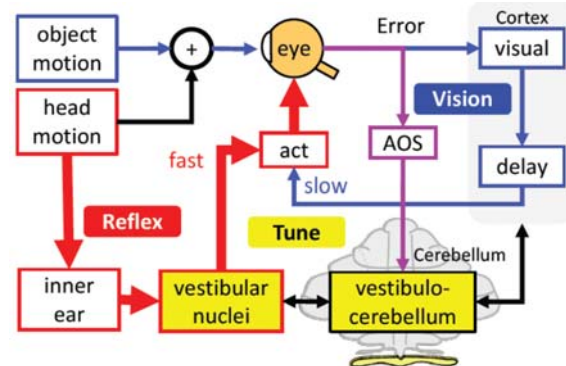
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## Motion tracking in presence of head motion

- ❖ Head motion is compensated via the **fast vestibulo-ocular reflex(VOR)**
- ❖ Object is tracked via the **slow cortical visual feedback**

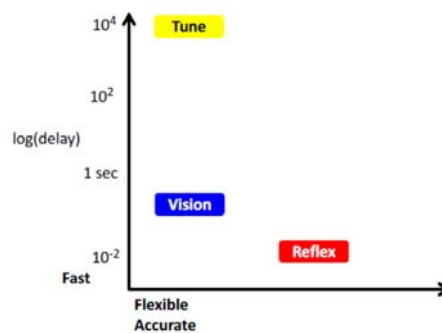
The gains sharing the eye muscle must match. Gains are tuned by cerebellum, vestibular nuclei, and auxiliary optical system



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## Motion tracking in presence of head motion

Fast and accurate visual performance is achieved with parts that are either fast or accurate **but not both!**



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## Layered controllers

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The control system is **layered** by independent vision and reflex layer controllers

Layer 1  
(vision)

Advanced planning: slow and small error



Tuning and learning needed for coordination

Layer 2  
(reflex)

Delayed reflexes: fast and large error

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**Hardware Level  
(neurons)**

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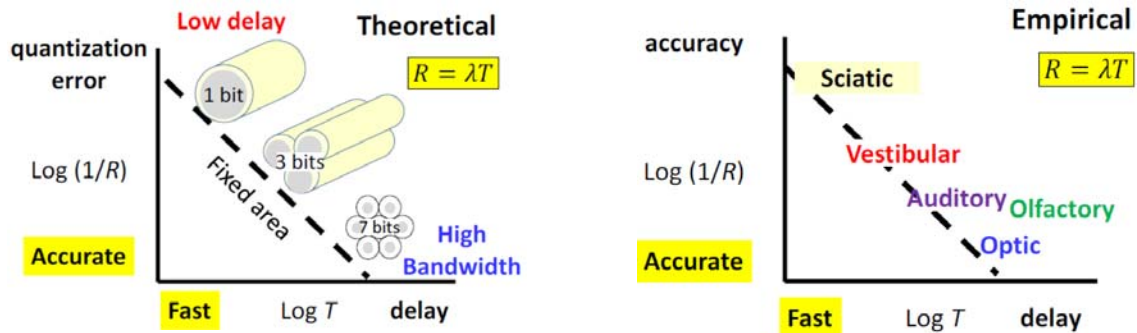
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## Hardware (neurons)

### Heterogeneity in size and number of axons

Propagation **speed** of action potential  $\propto$  axon's **diameter**

Signaling **bandwidth**  $\propto$  **number** of axons



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## Hardware (neurons)

### Heterogeneity in size and number of axons

Propagation **speed** of action potential  $\propto$  axon's **diameter**

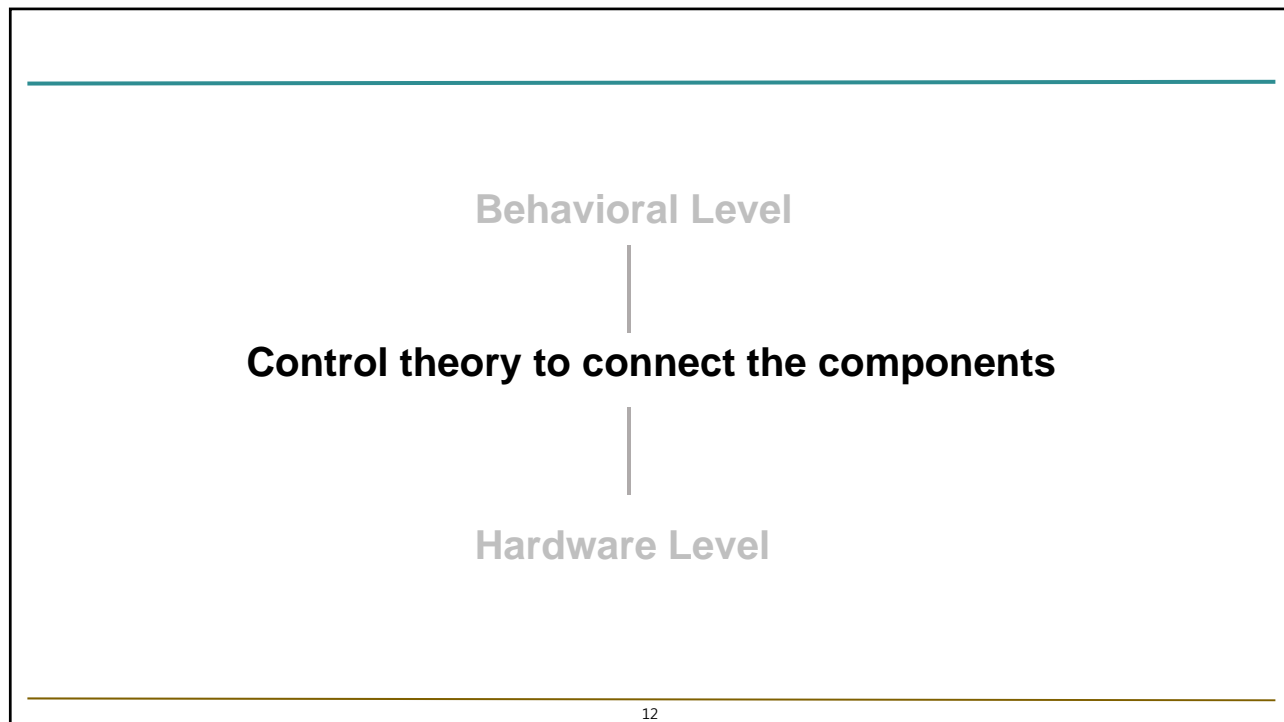
Signaling **bandwidth**  $\propto$  **number** of axons

**Hardware tradeoff between accuracy and speed**

$$R = \lambda T$$

R: number of bits (bandwidth)  
T: signaling delay

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## Control Theory

### Assume

The human sensorimotor composed of

- Sensors (eyes, inner ear)
- Communication Components (cranial and spinal nerves of CNS)
- Controllers (in CNS)
- Actuators (muscle/limb)

### Model

$$P: x(t+1) = ax(t) + w(t - T_w) + R[u(t - T_u)]$$

$$C: u(t) = K(x(0:t), w(0:t), u(0:t-1))$$

$x(t) \in \mathbb{R}$  : a scalar deviation between desired and actual muscle state

$w(t) \in \mathbb{R}$  : a disturbance

$u(t) \in \mathbb{R}$  : a scalar control action aimed to modify the actual muscle state

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Hardware Tradeoff

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## Control Theory

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- Actuators (muscle/limb)

### Optimal cost

$$\begin{cases} \sum_{i=1}^{|\tau|} |a^{i-1}| + |a^{|\tau|}|(2^R - |a|)^{-1} & \text{if } \tau < 0 \text{ (delayed reaction)} \\ (2^R - |a|)^{-1} & \text{if } \tau \geq 0 \text{ (advanced warning)} \end{cases}$$

$\tau := T_w - T_u$  : net warning

$R$  : number of bits (neuron)

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## Control Theory

### Assume

The human sensorimotor composed of

- Sensors (eyes, inner ear)
- Communication Components (cranial and spinal nerves of CNS)
- Controllers (in CNS)
- Actuators (muscle/limb)

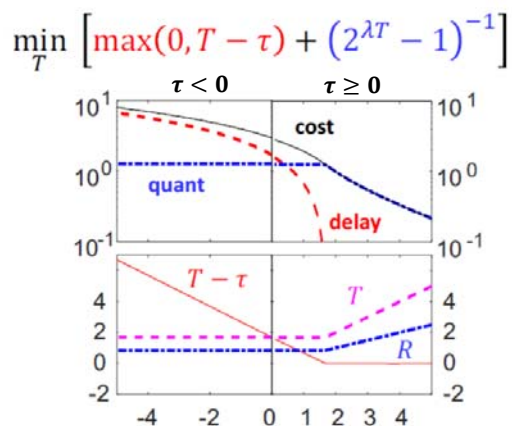
**Optimal cost (Let  $a = 1$ )**

$$\text{Max}[0, T - \tau] + (2^{\lambda T} - 1)^{-1}$$

$T$  : Signaling Delay  
 $\tau$  : Net warning

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## Control Theory



### Delayed reaction ( $\tau < 0$ ) - Reflex

Delay term dominates the overall cost.

Optimal nerve size should  
**sacrifice bandwidth in order to minimize delay!**

### Advanced warning ( $\tau \geq 0$ ) - Vision

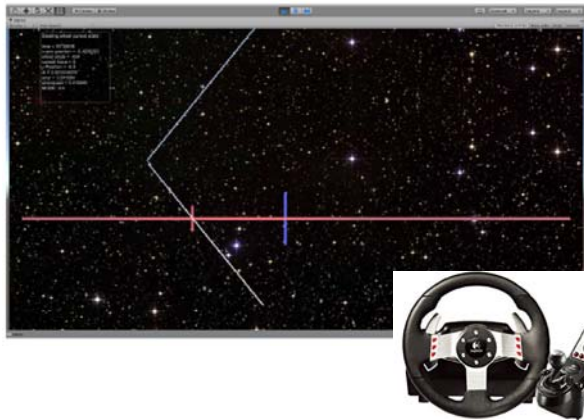
Quantization term dominates the overall cost.

Optimal nerve size should  
**sacrifice speed in order to maximize bandwidth!**

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## Experimental platform

### Experimental video game platform



#### Purposes

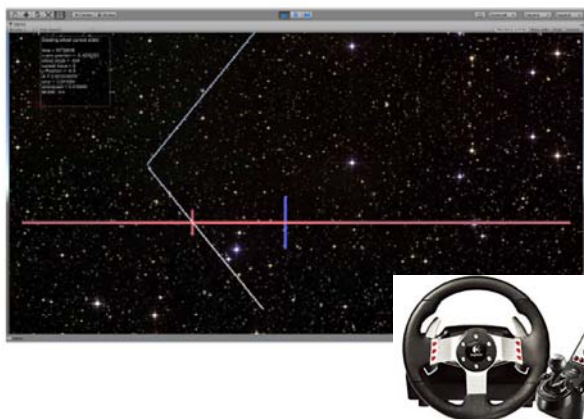
Quantify if the theory correctly predicts planning performance as a function of advanced warning

Quantify how close to optimal are humans in multiplexing planning and reflex tasks

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## Experimental platform

### Experimental video game platform



Experiment goes through three scenarios

**Bumps:** Track a constant track subject to force disturbances on the wheel

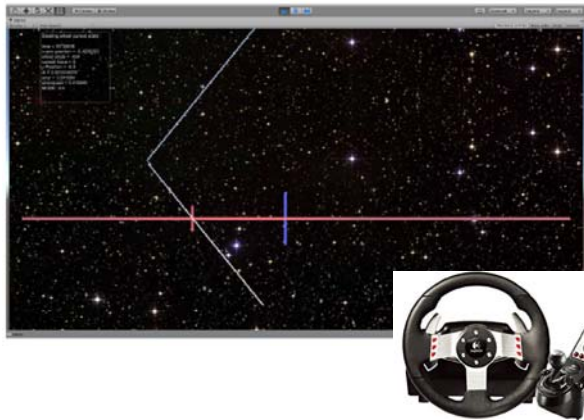
**Trails:** Track moving trail while having look-ahead but no forces

**Trails with Bumps:** Track a moving trail while there are force disturbances on the wheel

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## Experimental platform

### Experimental video game platform



Experiment goes through three scenarios

**Bumps:** Track a constant track subject to force disturbances on the wheel ➡ **Reflex!**

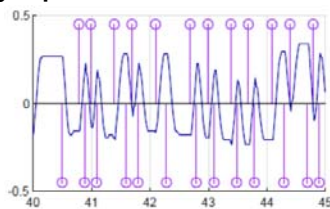
**Trails:** Track moving trail while having look-ahead but no forces ➡ **Vision!**

**Trails with Bumps:** Track a moving trail while there are force disturbances on the wheel ➡ **Multiplex!**

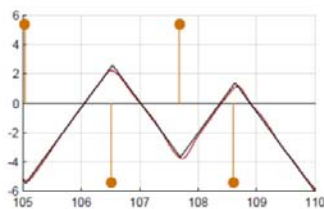
20

## Experimental platform

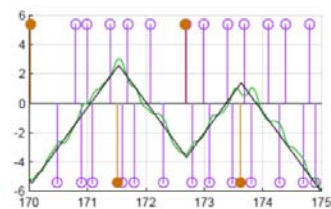
### Player positions



Bump

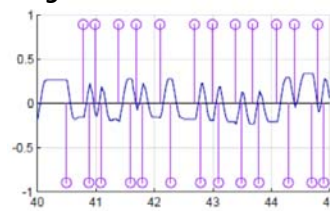


Trail

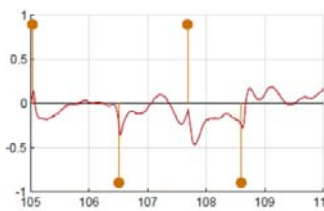


Trail with bumps

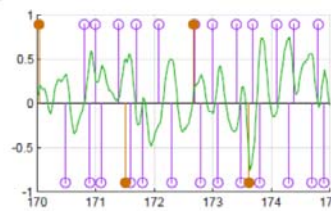
### Tracking error



Bump



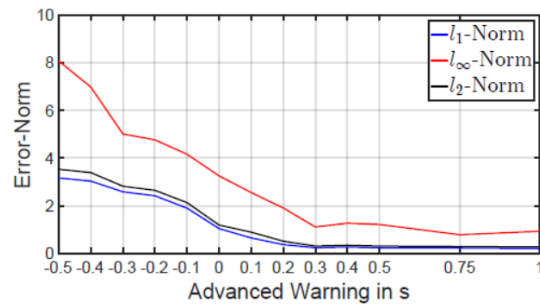
Trail



Trail with bumps

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## Experimental platform



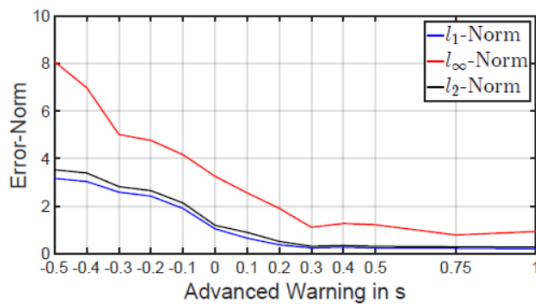
Optimal cost (Let  $\alpha = 1$ )

$$\text{Max}[0, T - \tau] + (2^{\lambda T} - 1)^{-1}$$

$T$  : Signaling Delay  
 $\tau$  : Net warning

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## Experimental platform



**Match strikingly well!**

Optimal cost (Let  $\alpha = 1$ )

$$\text{Max}[0, T - \tau] + (2^{\lambda T} - 1)^{-1}$$

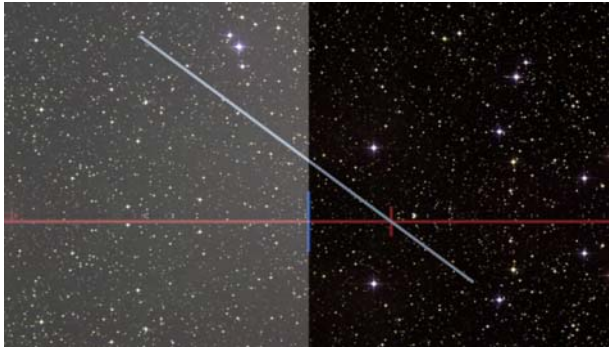
$T$  : Signaling Delay  
 $\tau$  : Net warning

For  $\tau < T$ , the error increase linearly with  $\tau$ .  
 $T \approx 250\text{ms}$  (typical visual delay for humans)

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## Experimental platform - Upgraded

Flash Test



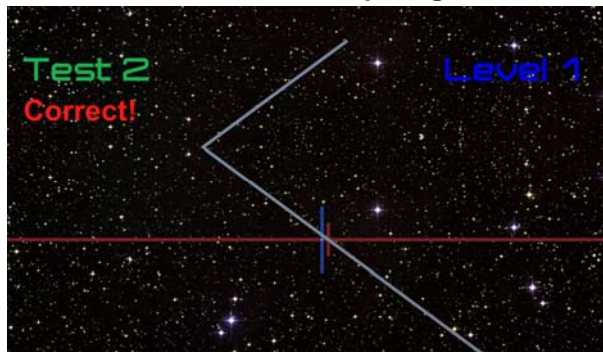
Color Contrast Test



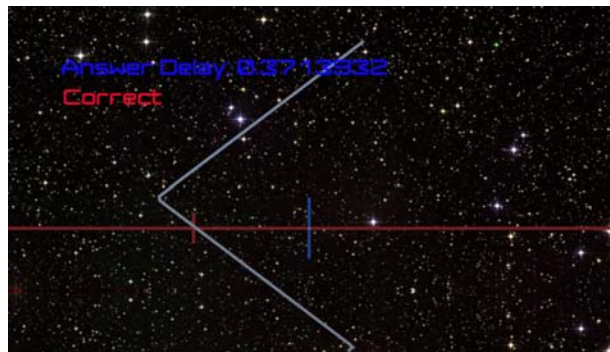
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## Experimental platform - Upgraded

Sound Pitch Comparing Test



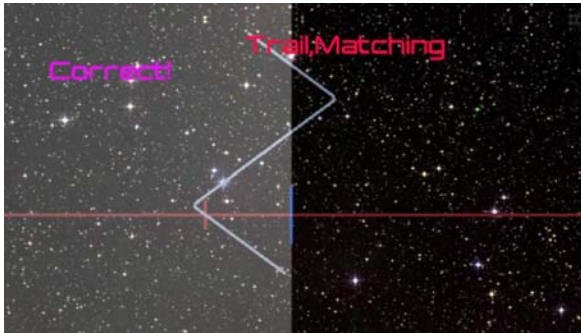
Sound Direction Test



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## Experimental platform - Upgraded

Matching Test = flash + sound test



Are flash and sound coming from same side?

Flash: Left Sound: Left → Press Left button

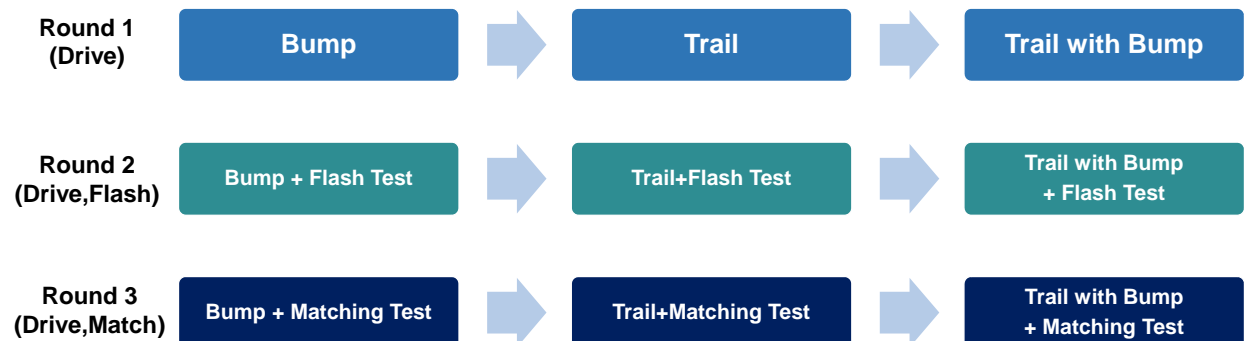
Flash: Right Sound: Right → Press Right button

Flash: Left Sound: Right → Don't press anything  
Flash: Right Sound: Left → Don't press anything

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## Experimental platform - Upgraded

### Upgraded game routine



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## Experimental platform - Upgraded

### First trial



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## Experimental platform - Upgraded

### Second trial



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## Experimental platform - Upgraded

### First trial



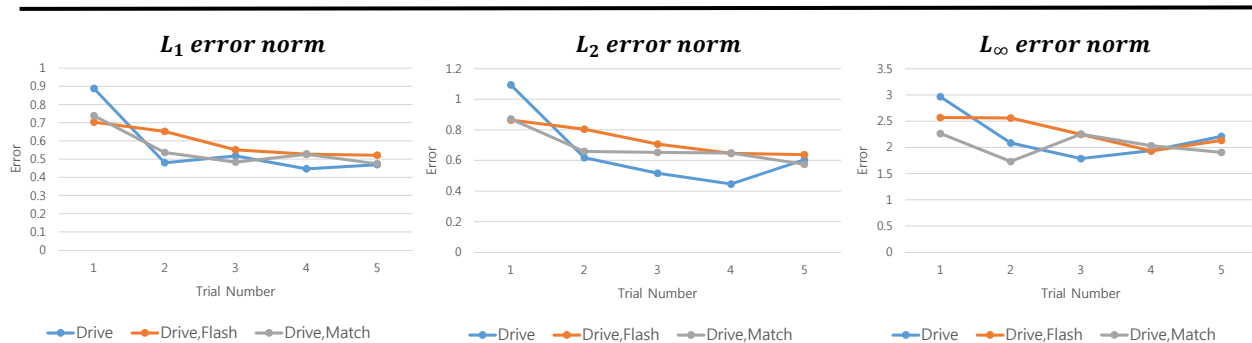
### Second trial



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## Experimental platform - Upgraded

### Error Norms vs Trial Number

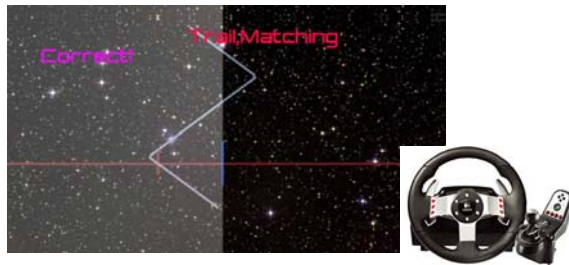


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## Future Goals

Add more basic tasks(visual, auditory) that do not interfere.  
 ➡ Push the multitasking performance to limits.

Do experiments with subjects to study how people learn.  
 ➡ **Come up with a theory to explain human learning.**

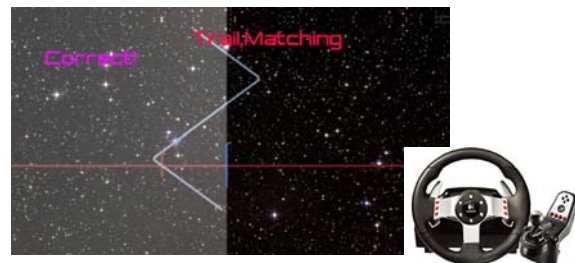
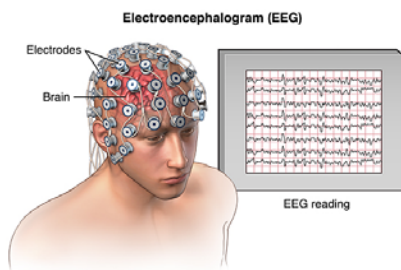


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## Future Goals

**Use the game platform with EEG** to study brain activity as tasks and multitasking changes, and as learning changes.

Identify the cortical sources that are active during different phases of the task.



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## References

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1. Y. Nakahira, N. Matni, and J. C. Doyle, "Hard limits on robust control over delayed and quantized communication channels with applications to sensorimotor control," *2015 IEEE 54th Annual Conference on Decision and Control*.
2. N. Matni and J. C. Doyle, "A theory of dynamics, control and optimization in layered architectures," in *American Control Conference (ACC)*, July 2016.
3. J. C. Doyle, Y. Nakahira, Y. P. Leong, E. Jenson, A. Dai, D. Ho and N. Matni, "Teaching control theory in high school", 2016 IEEE Conference on Decision and Control
4. A. Dai, E. Jensen, D. Ho, J. Doyle, "An experimental video game platform for sensorimotor control," *2016 IEEE Conference on Decision and Control*.