CMPS 6610 Extra Credit

In this extra credit assignment, we will test and review concepts you have learned since the midter exam. Please add your written answers to answers.md which you can convert to a PDF using convert.sh. Alternatively, you may scan and upload written answers to a file named answers.pdf.

1. Algorithmic Paradigms

- 1a. In learning about algorithmic paradigms, you encountered the unit weight scheduling problem. Given n tasks, what is the work and span of solving the unit-weight task scheduling problem by brute force?
- 1b. Now suppose we generalize this task scheduling problem by giving each task a weight. The goal is now to schedule a set of non-overlapping tasks with maximum weight. Does the greedy algorithm still work? If so, provide a new proof. If not, provide a counterexample.
- 1c. State the optimal substructure property for the weighted task scheduling problem, and give the work and span of the resulting dynamic programming algorithm.

2. Graphs

- 2a. We learned that we could use breadth-first search to solve the shortest path problem in an unweighted graph. Why doesn't it work for weighted graphs? Give a high-level reason as well as a counterexample.
- 2b. For the shortest path problem, is the Bellman-Ford algorithm superior to Dijkstra's algorithm? Compare and contrast these two approaches.
- 2c. You learned the cut property for minimum spanning trees. There is another useful fact called the cycle property for minimum spanning trees which states the following:

Given a graph G that contains a cycle, then the largest weight cycle in that graph **cannot** be contained in any minimum spanning tree.

Prove the cycle property.

3. Randomization

• 5a. In the last problem set you were asked to use Markov's inequality in Problem 1. Prove Markov's inequality by using the definition of the expected value of a random variable.