

**Lecture Notes on
Pattern Recognition**

**Session 07: Data Science -
The Risk of Privacy Compromise**

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Unit Learning Outcomes

- ULO1:**
 - Develop knowledge of and discuss new and *emerging fields* in data science.
 - Why there is the risk of privacy compromise
 - What are the current method to preserve the privacy?
 - How to manipulate textual data?
- ULO2:**
 - Describe advanced constituents and underlying *theoretical foundation* of data science.
 - The principle of differential privacy

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Road map

```

graph LR
    BD[Big Data] --> BI[Behaviour Informatics]
    BD --> PC[Privacy Concerns]
    BI --> GPP[GeoTagged Photo]
    BI --> CDD[Check-in Data]
    BI --> PPT[Periodic Pattern]
    BI --> PCP[Privacy Compromise]
    PC --> DP[Differential Privacy]
    PC --> S[Sensitivity]
    DP --> LEM[Lap/Exp Mechanisms]
  
```

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Research Themes @ TULIP Lab

(Team for Universal Learning and Intelligent Processing)

- Research Themes**
 - Behavior Informatics**
 - Periodic Behavior Mining
 - Behavior Prediction
 - Information Abuse Prevention**
 - Privacy Preserving Data Mining
 - Information Releasing Compliance Checking
 - Business Intelligence Applications**
 - Recommender System
 - Tourism/Hospitality Management

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Behavior Informatics

- Geotagged Photo
- Check-in Data
- What can be discovered?

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Behavior Informatics

- People share **news**, **interests** and **ideas** in OSNs,
– **though** these platforms also spread **email malware**, **rumours**,
gossips and **malicious links**, and also leak our **privacy**.

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Tourist Movement Analysis

- **Tourism Managers** need to obtain a comprehensive understanding about tourist behaviour:
 - Where and when visited?
 - What are participated activities and events?
 - What are tourist preferences and perceptions toward tourism products and service?
 -



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Tourist Movement Analysis

- **Existing Approaches in Travel Behavior:**
 - Survey and opinion polls are popular methods.
 - Time consuming and limited in the number of responses and scale of surveyed areas.
- **Challenges:**
 - How to capture comprehensive information about tourist travel behavior at large scales?
 - How to extract meaningful insights about tourist travel behavior?

**SOCIAL MEDIA ANALYTICS**

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Geotagged Photos

- Many photo-capturing devices now have built-in global positioning systems (GPS) technology
 
- **Geotagged photos** are shared on social website
 - Flickr (www.flickr.com)
 - Panoramio (www.panoramio.com)
 - 29,443 photos collected from 2,100 HK inbound tourists



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Geotagged Photos Visualization



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Geotagged Photos Visualization



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Hot Spots

Popularity of Areas of Interest.

Group	Area of Interest	Percentage (%)	Popularity Rank
Asian Tourist	Hong Kong Central	40.35	1
	Tsim Sha Tsui Area	38.80	2
	Times Square Towers	20.08	3
	Hong Kong International Airport	18.34	4
	The Peak Tower	14.19	5
	Center Mong Kok	10.52	6
Western Tourist	Hong Kong Central	47.92	1
	Tsim Sha Tsui Area	44.64	2
	The Peak Tower	19.74	3
	Center Mong Kok	13.14	4
	Times Square Towers	12.22	5
	Hong Kong International Airport	10.99	6
	Tian Tan Buddha Statue	10.43	7



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Temporal Analysis

- Tourist Present based on time stamp of the photos

(A) Hong Kong International Airport
 (B) Hong Kong Central

Hong Kong International Airport: Asian Tourist (red line), Western Tourist (blue line)

Hong Kong Central: Asian Tourist (red line), Western Tourist (blue line)

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Tourist Movement Analysis

(A) Asian Tourist
 (B) Western Tourist

Tourist Traffic Flow in Hong Kong Metropolitan Area.

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Tourist Movement Analysis

Huy Quan Vu, Gang Li, Rob Law, Ben Haobin Ye. Exploring the travel behaviors of inbound tourists to Hong Kong using Geotagged photos. *Tourism Management*.

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What is more?

- Geotagged Photos cannot provide detailed contextual information on tourists' activities for further analysis

(a) Without Activity Information
 (b) With Activity Information

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Venue Check-ins

- Location-aware mobile social applications, including
 - Foursquare (www.foursquare.com)
 - Ubersocial (www.ubersocial.com)
 - Yelp (www.yelp.com)
- Available on mobile devices
 - Allow users to explicitly share their current location in the form of venue check-ins,
 - With metadata such as *venue name*, *categories*, and *subcategories*.
 - Allows for **inferring tourist activities** (*dining, shopping, sightseeing, entertainment, etc.*)

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Venue Check-ins

- One Example
 - <https://www.swarmapp.com/c/8tfAWSjlQjU>

Ken Kobayashi at Hong Kong International Airport
 (+40 check-ins)
 Hong Kong | May 19, 2016 via Swarm for iOS
 Coins
 40 check-ins at Hong Kong International Airport +7
 Sharing is caring! +2

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Foursquare Venues

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Activity category (Label)	Example of Venue Type
Art & Entertainment (Ar)	Arcade, Art Gallery, Casino, Circus, Concert Hall, Exhibit, Historic Site, Movie Theater, Museum, Stadium, Theme Park, Zoo
College & University (Co)	College Academic Building, College Bookstore, College Library, College Lab, Student Center
Event (Ev)	Christmas Market, Conference, Convention, Festival, Parade
Food (Fo)	American Restaurant, Asian Restaurant, Italian Restaurant, Seafood Restaurant, Fast Food Restaurant, Burger Joint, Food Court, Coffee Shop, Dessert Shop
Nightlife Spot (Ni)	Bar, Lounge, Night Market, Nightclub
Outdoors & Recreation (Ou)	Athletics & Sports, Bay, Beach, Bike Trail, Botanical Garden, Bridge, Campground, Harbor / Marina
Professional & Other Places (Pr)	Animal Shelter, Auditorium, Ballroom, Building, Community Center, Convention Center, Cultural Center, Factory, Spiritual Center
Residence (Re)	Assisted Living, Home, Housing Development, Residential Building, Trailer Park
Shop & Service (Sh)	ATM, Antique Shop, Business Service, Flower Shop, Food & Drink Shop, Gaming Cafe
Travel & Transport (Tr)	Airport, Boat or Ferry, Bus Station, Cable Car, Cruise, Hotel, Metro Station, Pier, Taxi Stand

<https://developer.foursquare.com/categoriestree>

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Check-in Data

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- Check-in Record of a Tourist during a trip in Hong Kong

ID	Date	Time	Venue Name	Venue Type	Category	Latitude	Longitude
C1	5-Jun-16	13:10	Hong Kong International Airport	Airport	Ar	22.3091	114.1748
C2	4-Jun-16	23:25	Des Chai Daeng	Neighborhood	Ou	22.3001	114.1726
C3	4-Jun-16	22:41	KFC	Fried Chicken Joint	Fo	22.2989	114.1728
C4	5-Jun-16	17:17	Ngong Ping	Neighborhood	Ou	22.2550	113.9069
C5	5-Jun-16	17:18	Ngong Ping 360 Station	Cable Car	Tr	22.2568	113.9014
C6	5-Jun-16	17:18	Walking with Buddha	General Entertainment	Ar	22.2564	113.9031
C7	5-Jun-16	19:26	Ting Chau Tsai	City	Ou	22.3060	114.0255
C8	5-Jun-16	21:55	The Spaghetti House	Italian Restaurant	Fo	22.2962	114.1714
C9	5-Jun-16	21:55	Victoria Peak, Hong Kong	Theme Park	Ar	22.2962	114.1740
C10	6-Jun-16	11:38	Giant Panda Adventure	Zoo	Ar	22.2453	114.1754
C11	6-Jun-16	11:39	Panda Village	Zoo	Ar	22.2461	114.1762
C12	6-Jun-16	19:47	Spoon by Alain Ducasse	French Restaurant	Fo	22.2932	114.1741
C13	6-Jun-16	21:18	Sheraton Hong Kong Hotel	Hotel	Tr	22.2953	114.1726
C14	6-Jun-16	22:18	McDonald	Fast Food Restaurant	Fo	22.2964	114.1711
C15	7-Jun-16	12:46	MTR Tung Chung Station	Metro Station	Tr	22.2892	113.9413
C16	7-Jun-16	14:24	Chocolate Shop	Fo	22.2892	113.9407	
C17	7-Jun-16	19:28	Cross-Harbour Tunnel	Tunnel	Tr	22.2955	114.1817
C18	7-Jun-16	20:36	The Peak Galleria	Shopping Mall	Sh	22.2703	114.1500
C19	7-Jun-16	20:37	Victoria Peak	Mountain	Ou	22.2708	114.1496
C20	8-Jun-16	9:01	Hong Kong International Airport	Airport	Tr	22.3153	113.9348

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Check-in Data

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Venue Check-in Data in Hong Kong

Group	# of Tourist	# of Check-ins	Average
Asian	467	12,836	27.49
Western	333	4,519	33.98
Total:	800	17,355	

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Activity Preference Analysis

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Activity Preferences of Asian and Western tourists

Venue Type	Proportion (%)	Asian	Western	Difference	Z-test	p-value*
Arts & Entertainment						
Theme Park	27.74	8.27	19.47	4.655	0.000	
Food						
Hong Kong Restaurant	19.14	9.77	9.37	2.514	0.012	
Steakhouse	2.58	9.02	6.44	-3.350	0.011	
Nightlife Spot						
Bar	4.73	14.29	9.55	-3.860	0.000	
Lounge	1.29	8.27	6.98	-4.283	0.000	
Pub	0.22	6.77	6.55	-5.207	0.000	
Hostel Bar	3.23	8.27	5.04	-2.527	0.011	
Cocktail Bar	1.51	6.02	4.51	-2.943	0.003	
Outdoors & Recreation						
Neighborhood	30.32	18.80	11.53	2.591	0.010	
City	11.40	20.30	8.90	-2.679	0.007	
Shop & Service						
Shopping Mall	40.22	27.07	13.15	2.731	0.006	
Travel & Transport						
Metro Station	14.84	3.76	11.08	3.408	0.001	
Bus Station	12.90	4.51	8.39	2.710	0.007	
Bus Stop	5.16	0.00	5.16	2.668	0.008	

*Significant at p≤0.05

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Activity Categories Distribution

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Distribution of Check-ins

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Temporal Analysis

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- Tourism Spots

a) Airport

b) Shopping Mall

c) Park

d) Spiritual Center

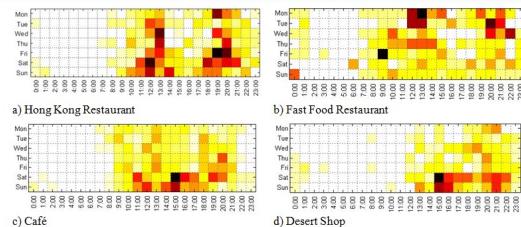
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Temporal Analysis

- Dinning Behavior



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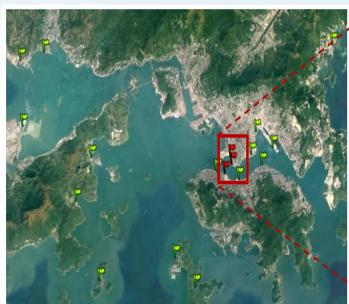
Train Station Visits



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Ferry Pier Visits



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Tourists' Behavior Mining



Huy Quan Vu, Gang Li, Rob Law, Yanchun Zhang, [Travel Diaries Analysis by Sequential Rule Mining](#), Journal of Travel Research, 2017, 57(3): 399-413.

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Periodic Behavior Mining



- Observed Check-in Data is usually a mixed events from different periodic behaviors
 - What are regular behavior patterns?
 - What are their periods for each?
 - Predict the Behavior on a particular day



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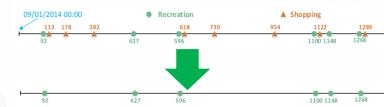
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Periodic Behavior Mining



- Observed Check-in Data is usually a mixed events from different periodic behaviors
 - What are Periodic?
 - What is the period?
 - Predict the Behavior on a particular day

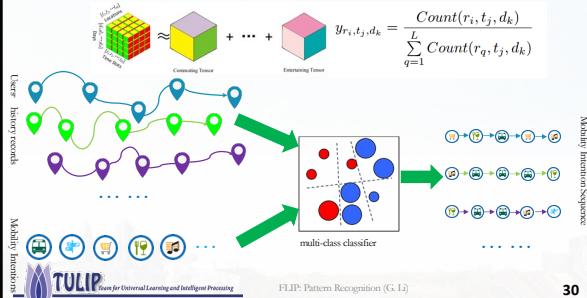


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Periodic Behavior Mining Mobility Intentions

- CP Decomposition

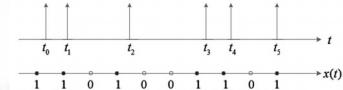


Periodic Behavior Mining Periodicity Detection

Definition 1 (Human Periodic Behavior). Suppose $T_0 > 1$ and $0 \leq t_0 < T_0$, for any $0 \leq t^* < T_0$

$$I(t^*) = \begin{cases} 1, & t^* = t_0 \\ 0, & \text{otherwise} \end{cases} \quad (1)$$

If there is one and only one timestamp $t' \in [t_0 - \delta + kT_0, t_0 + \delta + kT_0]$ of X which satisfies $I(t') = I(t_0)$ for $k = 0, 1, \dots, \text{mod}(n-1, T_0)$, the binary sequence X is a periodic behavior binary sequence with the period T_0 .



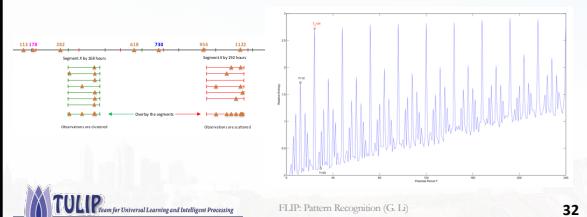
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Periodic Behavior Mining Periodicity Detection

Lemma 1. If a binary sequence X is periodically generated according to a categorical distribution μ_0' for some period T_0 , then for any $T \geq 2, T \in \mathbb{N}$, we have

$$\lim_{n \rightarrow \infty} KL(T_0) \geq \lim_{n \rightarrow \infty} KL(T) \quad (5)$$



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Periodic Behavior Mining Applications

- Applications of Periodic Behavior Mining
 - What is the schedule of a person on a particular day/time?
 - Where to find the person on a particular day/time?
 - Police applications
 - Scheduled “Encountering” for match making
 - Timely Recommendation Systems
 - Now it is the time for you to stock rice, cooking oil, or ice cream!

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Privacy Breach

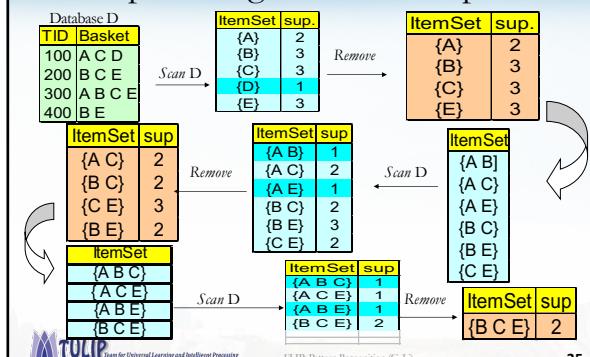
- Privacy Breach in Data Release/Sharing:
 - Adversary with background information, may re-identify the user or confirm the relationship between users from the aggregated information of the dataset.
 - Adversary observes the aggregated information of the dataset, removing a particular user will change the statistical information.



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Apriori Algorithm: Example



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Privacy Breach Example (1)

TABLE 5. Privacy breach of international visitors

ID	User(Gender)	Location of Origin	Venue	Date	Time
R ₁	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	Rendezvous Hotel Singapore	31-Dec-2015	10:24
R ₂	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	Plaza Singapura	31-Dec-2016	17:22
R ₃	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	Gardens by the Bay	31-Dec-2016	20:58
R ₄	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	The Cathay Cineplex	1-Jan-2017	14:15
R ₅	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	Sentosa Island	1-Jan-2017	16:01
R ₆	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	Siloso Beach	1-Jan-2017	17:10
R ₇	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	FashionTV Singapore Night Club	2-Jan-2017	02:14
R ₈	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	MA Deen Bissa Restaurant	2-Jan-2017	04:27
R ₉	U ₁ (M)-U ₂ (F)	Kuala Lumpur, Malaysia	Merlion Park	2-Jan-2017	18:09



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Privacy Breach Example (2)

TABLE 6. Privacy breach of Singapore residents traveling overseas.

ID	User(Gender)	Visited Destination	Venue	Date	Time
L ₁	U ₅ (M)-U ₆ (F)	Shanghai, China	UNCO Lounge	25-May-2015	20:17
L ₂	U ₅ (M)-U ₆ (F)	Shanghai, China	TS Restaurant and Bar	26-May-2015	17:35
L ₃	U ₅ (M)-U ₆ (F)	Cannes, France	Villa Mystique Resort	25-Jun-2015	11:03
L ₄	U ₅ (M)-U ₆ (F)	Paris, France	Derson Restaurant	27-Jun-2015	19:58
L ₅	U ₅ (M)-U ₆ (F)	Paris, France	Ladure Pastry Shop	28-Jun-2015	14:48
L ₆	U ₅ (M)-U ₆ (F)	London, United Kingdom	L'ETO Caff	10-Oct-2015	11:01
L ₇	U ₅ (M)-U ₆ (F)	Hong Kong	The Ocean Club Bar	31-Oct-2015	18:47
L ₈	U ₅ (M)-U ₆ (F)	Hanoi, Vietnam	HOME Hanoi Restaurant	01-Jan-2016	19:04
L ₉	U ₅ (M)-U ₆ (F)	Ho Chi Minh, Vietnam	MGallery Hotel des Art	30-Jun-2016	19:54
L ₁₀	U ₅ (M)-U ₆ (F)	Ho Chi Minh, Vietnam	L'Usine: Cafe	01-Jul-2016	10:55
L ₁₁	U ₅ (M)-U ₆ (F)	Ho Chi Minh, Vietnam	Social Club @ Hotel Des Arts	01-Jul-2016	17:04



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Privacy Breach Example (3)

TABLE 7. Privacy breach of local resident in Singapore.

ID	User(Gender)	Venue	Date	Time
S ₁	U ₇ (M)-U ₈ (F)	Club Myst	01-May-2017	01:56
S ₂	U ₇ (M)-U ₈ (F)	Strker Signature Bar	10-May-2017	21:16
S ₃	U ₇ (M)-U ₈ (F)	Club Hollywood	13-May-2017	00:20
S ₄	U ₇ (M)-U ₈ (F)	Oppa Korean Grill Restaurant	16-May-2017	19:17
S ₅	U ₇ (M)-U ₈ (F)	MANEKINEKO Karaoke Bar	19-May-2017	22:09
S ₆	U ₇ (M)-U ₈ (F)	Hotel G Singapore	10-Jun-2017	11:24
S ₇	U ₇ (M)-U ₈ (F)	Golden Village Multiplex	08-Jul-2017	21:24
S ₈	U ₇ (M)-U ₈ (F)	The Platinum Movie Suites	12-Aug-2017	14:35
S ₉	U ₇ (M)-U ₈ (F)	Joo Bar	12-Aug-2017	19:46



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Privacy Breach Example (4)

TABLE 8. Joint check-in record indicating sensitive contrast relationship.

ID	User(Gender)	Venue	Date	Time
C ₁	U ₉ (M)-U ₁₀ (F)	Zouk Night Club	11-Sep-2015	23:31
C ₂	U ₉ (M)-U ₁₁ (F)	Zouk Night Club	18-Nov-2015	23:50
C ₃	U ₉ (M)-U ₁₁ (F)	Club Luxi	17-Jan-2016	00:30
C ₄	U ₉ (M)-U ₁₁ (F)	Club Hollywood	06-Feb-2016	04:34
C ₅	U ₉ (M)-U ₁₀ (F)	Wave House Sentosa	12-Mar-2016	22:43
C ₆	U ₉ (M)-U ₁₀ (F)	Zouk Night Club	02-Jul-2016	00:25
C ₇	U ₉ (M)-U ₁₀ (F)	Zouk Night Club	07-Aug-2016	06:39



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Concerns on Data Privacy

- Privacy Model
- Differential Privacy



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Special Issues on Privacy

• IEEE Spectrum, Aug.

2014

- On the Internet, nobody knows you are a dog (1993).
- Interested parties not only know you are a dog, but also know the colour of your fur (2014)



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Special Issues on Privacy

- Communication of ACM**

Sept. 2014

- Federal law governing student privacy and the release of student records suggests that anonymizing student data can hardly protect student privacy.

practice



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Special Issues on Privacy

- Science**, Jan. 2015

- Data pour out of us and our devices every second of every day, and people no longer control their personal privacy.



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Information Abuse Prevention

- Information Abuse**

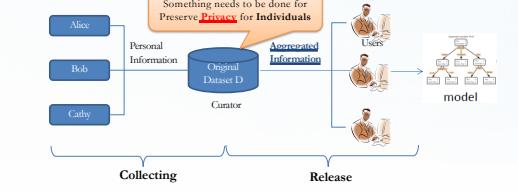
- The compromise of information for which the data stakeholders are not willing to disclose.
- It depends on
 - the nature of the information,
 - the involved internal or external users,
 - and the ways in which the organization grants the access to or releases the information.



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Background



- Data are collected in:
- Medical, Bank, Social Network.....
- Social benefits :
- better services, Finding correlations, Publishing official statistics, Data Mining.....

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Who is an adversary?

- Every user is potentially an adversary
 - After data is released, we cannot prevent any user from performing any type of analysis on the released data
 - Worst case scenario
 - Must account for disclosure risk from all types of analyses



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RR: One Early Trick in Social Science

- Response to embarrassing questions

- How many percentage of researchers are using pirate software?

- Are you using Pirate Software in research?**

- Yes?**
- No?**

- Participants are advised to respond as below

- Flip a coin
 - If **tail**, then response the truth
 - If **head**, flip another coin
 - If **head**, response Yes
 - If **tail**, response No

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RR: One Early Trick in Social Science

- Response to embarrassing questions
 - How many percentage of researchers are using pirate software?
 - Are you using Pirate Software in research?
 - Yes?
 - No?
- Here privacy comes from **a plausible deniability** of any outcome
- Accuracy comes from the understanding of the mechanism
 - expected #Yes is
 - $\frac{1}{4}$ participants who are not Yes +
 - $\frac{3}{4}$ participants who are Yes
 - $P^* = \frac{1}{4}(1-p) + \frac{3}{4} p = \frac{1}{4} + p/2$



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What to promise?

- Respondent will feel safe submitting his data if “If I knew the chance that the privatized **aggregated information** (constructed model or query results) S was **nearly the same**, whether or not I submitted my information”



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What to promise?

- Respondent will feel safe submitting his data if “If I knew the chance that the privatized **aggregated information** (constructed model or query results) S was **nearly the same**, whether or not I submitted my information”



It bounds the ability to infer from any outcome S , whether the input data was D or D' .

From an arbitrary prior $P(D)$ and $P(D')$, we see that

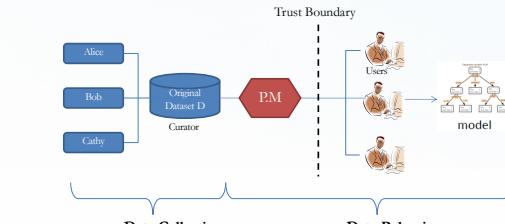
$$\frac{p(D|S)}{p(D'|S)} = \frac{p(D)}{p(D')} \times \frac{p(S|D)}{p(S|D')}$$



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Privacy Model



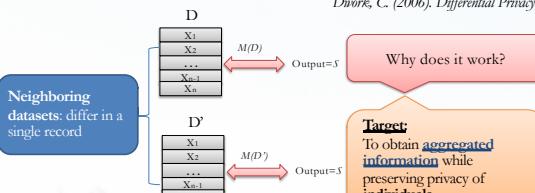
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Differential Privacy

- An individual is **in** or **out** of the database should make **little difference** of the analytical output

Dwork, C. (2006). Differential Privacy



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Differential Privacy

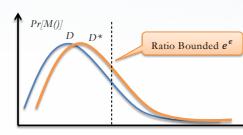
- Definition:

– a **mechanism M** is ϵ -**differential privacy** if for all pairs of neighboring datasets D and D' , and for all possible output S , satisfy with:

ϵ is Privacy Budget

$$e^{-\epsilon} \leq \frac{\Pr[M(D) \in S]}{\Pr[M(D') \in S]} \leq e^{\epsilon}$$

DP-Mechanism



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Privacy Budget

- ϵ controls the privacy guarantee level of mechanism.
 - A smaller ϵ represents a stronger privacy.
 - Normally, it is less than 1.



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Sensitivity: Global Sensitivity

- The **global sensitivity** considers the maximal difference between query results on neighboring datasets
 - indicates how much the **difference** should be hidden in mechanisms
 - Only related to query



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Sensitivity: Example

- Suppose we have a dataset D and two queries:
 $f_1 = \text{Count}(\text{HIV})$, $f_2 = \text{Average}(\text{Age})$.
- Let r represent the record.

	Job	Sex	Age	Disease	Count(HIV)	Average(Age)
	Engineer	Male	35	Hepatitis	$f_1(D)=4$	$f_2(D)=34.3$
	Engineer	Male	50	Hepatitis	$f_1(D-r)=4$	$f_2(D-r)=34.1$
	Lawyer	Male	35	HIV	$f_1(D-r2)=4$	$f_2(D-r2)=31.6$
	Writer	Female	30	Flu	$f_1(D-r3)=3$	$f_2(D-r3)=34.1$
	Writer	Female	30	HIV	$f_1(D-r4)=4$	$f_2(D-r4)=35$
	Dancer	Female	30	HIV	$f_1(D-r5)=3$	$f_2(D-r5)=35$
	Dancer	Female	30	HIV	$f_1(D-r6)=3$	$f_2(D-r6)=35$
					$f_1(D-r7)=3$	$f_2(D-r7)=35$
					$\Delta f_{GS}=4-3=1$	$\Delta f_{GS}=34.3-31.6=2.7$



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Differential Privacy Mechanism

- Laplace Mechanism:**
 - suitable for numeric output
 - How many people in this room have blue eyes?
- Exponential Mechanism:**
 - suitable for non-numeric output
 - What is the most common eye color in this room?

Dwork, C., McSherry, F., Nissim, K., & Smith, A. (2006). Calibrating Noise to Sensitivity in Private Data Analysis. *Theory of Cryptography*, 265-284.

McSherry, F., & Talwar, K. (2007). Mechanism Design via Differential Privacy. *(FOCS'07)*



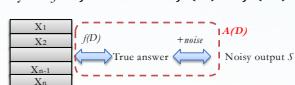
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Laplace Mechanism

- Let $f(D)$ be a numeric query on dataset D
 - How many people in this room have blue eyes?
 - The sensitivity of f : $\Delta f = \max \|f(D) - f(D')\|_1$



- A Laplace Mechanism M is ϵ -differential privacy:

$$M(D) = f(D) + \text{Lap}\left(\frac{\Delta f}{\epsilon}\right)$$

True Answer

Noise

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Laplace Example

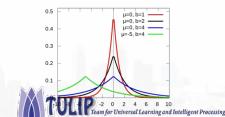
- Query: How many people have HIV?
 - DP answer = True answer + Noise
 - $M(D) = f(D) + \text{Lap}\left(\frac{\Delta f}{\epsilon}\right)$
 - Sensitivity is $\Delta f = 1$, because the answer is changed most at 1 if one user is deleted.
 - If we define $\Delta f = 1$, the noise is sample from:

$$\text{Lap}\left(\frac{1}{\epsilon}\right)$$

- DP answer $M(D)$:

- $4 + 1 = 5$ (higher probability)
- $4 - 1 = 3$ (higher probability)
- $4 - 3 = 1$ (lower probability)

$$\text{Lap}(b) = \frac{1}{2b} \exp\left(-\frac{|x|}{b}\right)$$



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Exponential Mechanism

- Exponential Mechanism is suitable for non-numeric output R
 - What is the most common eye color in this room?
 - i.e. R={Brown, Blue, Black, Green}
- Paired with a quality score q:
 - $q(D, r)$ represents how good an output r is for dataset D
- An exponential Mechanism \mathcal{A} is ϵ -differential privacy if:

$$A(D, q) = \{\text{return } r \text{ with probability } \propto \exp\left(\frac{\epsilon \cdot q(D, r)}{2\Delta q}\right)\}$$

Sensitivity of $q: \Delta q = \max \|q(D) - q(D')\|_1$



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Exponential Example

- What is the most common eye color in this room?

- i.e. R={Brown, Blue, Black, Green}

11.8%, 0.01%, 88%, 0.0001%

$$\Pr(r) \propto \exp\left(\frac{\epsilon \cdot q(D, r)}{2\Delta q}\right)$$

Impact of changing a single record

Option	Score	Sampling Probability		
		$\epsilon = 0$	$\epsilon = 0.1$	$\epsilon = 1$
Brown	23	0.25	0.34	0.12
Blue	9	0.25	0.16	10^4
Black	27	0.25	0.40	0.88
Green	0	0.25	0.10	10^{-6}



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Advantage of DP

	Traditional PM	Differential Privacy
Privacy level can be measured and compared	No	Can be measured by the privacy budget
The privacy guarantee can be proved theoretically	No	DP definition
Resist background attack	No	DP assumes that attackers get to know everyone's information except the one we will protect.



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Challenge: Tradeoff P&U

• Privacy

- bounded by the privacy budget

• Utility

- diverse measurements according to different application requirements
 - Recommendation system: similarity covariance
 - Classification: misclassified rate

• Privacy vs. Utility

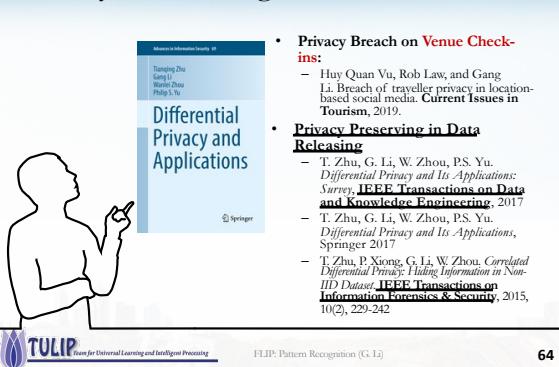
- Both mechanisms sacrifice utility to gain privacy
- Tradeoff:** To get the maximal utility in a fixed



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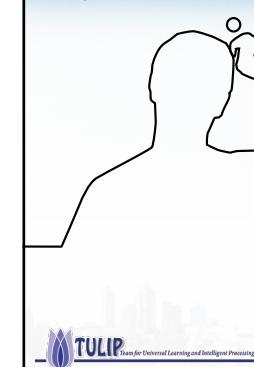
Privacy Preserving Related Reference



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Questions?



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