



Lecture Notes on  
Pattern Recognition

Session 01(B): Introduction to P.R.

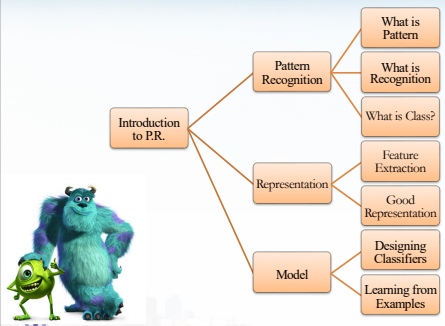


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Deakin University, VIC 3125, Australia

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Road map



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Pattern Recognition



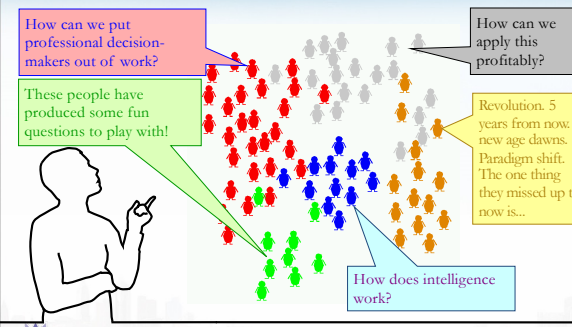
- What is Pattern?
- What is Recognition?
- What is Pattern Class?

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An AI cocktail party





How can we put professional decision-makers out of work?

These people have produced some fun questions to play with!

How can we apply this profitably?

Revolution. 5 years from now: A new age dawns. Paradigm shift. The one thing they missed up to now is...

How does intelligence work?






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What Kinds of AI research?


Natural AI	Algorithmic AI
<ul style="list-style-type: none"> <li>• Can we make something that is as intelligent as a human (or a bee)?</li> <li>• Can we get something that is evolutionary and self improving and autonomous and flexible?</li> </ul>	<ul style="list-style-type: none"> <li>• Can we save this bank \$50billion by auto fraud detection?</li> <li>• Can we start a new industry of automated negotiation/voice translation etc.?</li> </ul>



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Pattern Discovery from Data



- Why do we tend to patterns in the cloud?
  - Our mind prefers patterns.
  - Our brains do 'clustering' unconsciously.
  - In fact, we are 'encoded' to see patterns in everything:
    - shopping, traffic,
    - what to eat, wear, etc. ...
- How do we 'teach' a computer to do this?
  - This is a form of learning.
  - Also called unsupervised learning.
  - Key component of **exploratory data analysis**.

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## Pattern Recognition


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- A basic attribute of people: categoryization of sensory input

```

graph LR
    pattern --> Preprocessing --> Feature_extraction[Feature extraction] --> Classification --> Class_label
  
```

- Examples:
  - Diagnosis from medical images
  - Face detection from photo
  - etc.



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## Pattern Recognition

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- Machine Recognition of Patterns

```

graph LR
    pattern --> Preprocessing --> Feature_extraction[Feature extraction] --> Classification --> Class_label
  
```

- Preprocessing**
  - remove noise, normalize, etc.
- Feature Extraction**
  - makes some "problem-specific" measurement on the input pattern
- Classifier**
  - maps each feature vector to a class label

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## Pattern Recognition

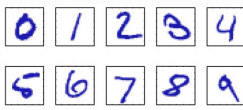
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- Machine Recognition of Patterns

```

graph LR
    pattern --> Preprocessing --> Feature_extraction[Feature extraction] --> Classification --> Class_label
  
```

- Examples: Character Recognition**
  - Pattern → Image
  - Class → Identify of Character
  - Features → Binary Image, Projection, Moments, etc.



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## Pattern Recognition

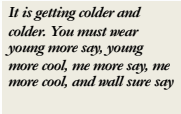
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- Machine Recognition of Patterns

```

graph LR
    pattern --> Preprocessing --> Feature_extraction[Feature extraction] --> Classification --> Class_label
  
```

- Examples: Speech Recognition**
  - Pattern → 1D signal or its samples
  - Class → the semantics
  - Features → Spectral Info, LPC model, cepstrum, etc.



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## Pattern Recognition


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- Machine Recognition of Patterns

```

graph LR
    pattern --> Preprocessing --> Feature_extraction[Feature extraction] --> Classification --> Class_label
  
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- Examples: Speech Recognition**
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## Pattern Recognition


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- Machine Recognition of Patterns

```

graph LR
    pattern --> Preprocessing --> Feature_extraction[Feature extraction] --> Classification --> Class_label
  
```

- Examples: Video Surveillance**
  - Pattern → Video sequence
  - Class → levels of alertness
  - Features → Motion Trajectories, parameters of a prefixed model, etc.



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- Machine Recognition of Patterns

pattern → Preprocessing → Feature extraction → Classification → Class label

- Examples: Spam Detection**
  - Pattern → An Email
  - Class → Spam or Legitimate
  - Features → TF-IDF, BOW, word context, IP addresses, etc.



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## Pattern Recognition

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- Machine Recognition of Patterns

pattern → Preprocessing → Feature extraction → Classification → Class label

- Examples: Fingerprint (iPhone5S-)**
  - Pattern → Image plus an identity claim
  - Class → Yes or No
  - Features → Position of Minutiae, Orientation fields of Ridge lines, etc.



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## Pattern Recognition

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- Machine Recognition of Patterns

pattern → Preprocessing → Feature extraction → Classification → Class label

- Examples: Credit Screening**
  - Pattern → Details of an Applicant
  - Class → Yes or No
  - Features → income, job history, levels of credits, credits history etc.



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## Pattern Recognition

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- Pattern Recognition System

pattern → Preprocessing → Feature extraction → Classification → Class label

**Recognition**

**Training**


Patterns + Class labels → Preprocessing → Feature selection → Learning → Model → Classification → Class label

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## Representation

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- Feature Engineering
- Difficulties
- Representation

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## Feature Engineering

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- Features depend on the problem

pattern → Preprocessing → Feature extraction → X → Classification → Class label

- After **feature extraction**, each pattern is represented as a **vector**
  - A representation could consist of a vector of real-valued numbers, ordered list of attributes, parts and their relations....
- Some techniques available to extract more relevant quantities from the initial measurements (like PCA)

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## Difficulties of Representation

- **Feature Selection** vs. **Feature Extraction**
- How many and which subset of features to use in constructing the decision boundary?
  - Some features may be redundant
- Curse of dimensionality
  - Error rate may in fact increase with too many features in the case of small number of training samples



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## Intra-Class Variability



"T" in different typefaces



Same face under different expression, pose, illumination

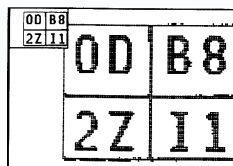


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## Inter-Class Similarity



Characters that look similar



Twins



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## Good Representation

- Account for *intra-class variations*
- Ability to *discriminate* pattern classes of interest;
  - low inter-class similarity
- Should have some *invariant* properties
  - e.g., w.r.t. rotation, translation, scale...
- *Robustness* to noise, occlusion,...
- Lead to simple matching or decision-making strategies (e.g., linear decision boundary)
- Low measurement cost; real-time



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## Example

(Salmon vs Bass Classification)

- Preprocessing
  - image enhancement and segmentation
    1. separate touching or occluding fishes;
    2. extract fish contour

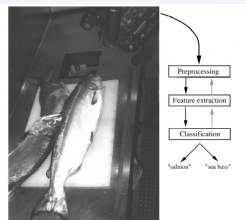


FIGURE 1.1. The objects to be classified are first sensed by a transducer (camera), whose signals are preprocessed. Next the features are extracted and finally the classification is carried out, how either "salmon" or "bass". Although the information flow is often chosen to be from the source to the classifier, some systems employ information flow in which earlier levels of processing can be altered based on the tentative or preliminary response in later levels (dotted arrows). Yet others combine two or more stages into a unified step, such as simultaneous segmentation and feature extraction. From: Richard O. Duda, Peter E. Hart, and David G. Stork, Pattern Classification. Copyright © 2001 by John Wiley & Sons, Inc.



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## Example

(Salmon vs Bass Classification)

- Fish length as a feature

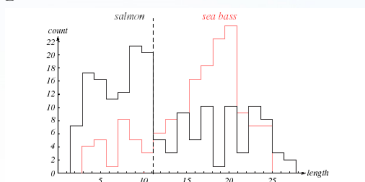


FIGURE 1.2. Histograms for the length feature for the two categories. No single threshold value of the length will serve to unambiguously discriminate between the two categories; using length alone, we will have some errors. The value marked  $P^*$  will lead to the smallest number of errors, on average. From: Richard O. Duda, Peter E. Hart, and David G. Stork, Pattern Classification. Copyright © 2001 by John Wiley & Sons, Inc.



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## Example

(Salmon vs Bass Classification)

- *Fish lightness* as a feature

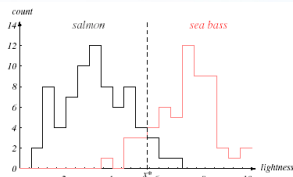


FIGURE 1.3. Histograms for the lightness feature for the two categories. No single threshold value  $x^*$  (decision boundary) will serve to unambiguously discriminate between the two categories; using lightness alone, we will have some errors. The value  $x^*$  marked will lead to the smallest number of errors, on average. From: Richard O. Duda, Peter E. Hart, and David G. Stork, *Pattern Classification*. Copyright © 2001 by John Wiley & Sons, Inc.



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## Example

(Salmon vs Bass Classification)

- There are two possible classification errors.
  1. Deciding the fish was a sea bass when it was a salmon.
  2. Deciding the fish was a salmon when it was a sea bass.
- Which error is more important?
  - It depends; e.g., if the fish packing company knows that:
    - Customers who buy salmon will object vigorously if they see sea bass in their cans.
    - Customers who buy sea bass will not be unhappy if they occasionally see some expensive salmon in their cans.
- How does this knowledge affect our decision?



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## Example

(Salmon vs Bass Classification)

- 2D Features leads to better separation

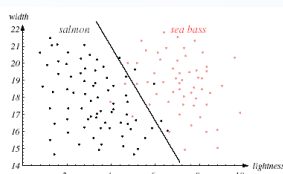


FIGURE 1.4. The two features of lightness and width for sea bass and salmon. The dark line could serve as a decision boundary of our classifier. Overall classification error on the data shown is lower than if we use only one feature as in Fig. 1.3, but there will still be some errors. From: Richard O. Duda, Peter E. Hart, and David G. Stork, *Pattern Classification*. Copyright © 2001 by John Wiley & Sons, Inc.



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## How Many Features

- Does adding more features always improve the results?
  - Correlated features do not improve performance.
  - It might be difficult to extract certain features.
  - It might be computationally expensive to extract many features.
  - “Curse” of dimensionality ...

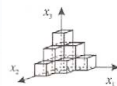


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## How Many Features

- Adding too many features can, paradoxically, lead to a worsening of performance.
  - Divide each of the input features into a number of intervals, so that the value of a feature can be specified approximately by saying in which interval it lies.



- If each input feature is divided into  $M$  divisions, then the total number of cells is  $M^d$  ( $d$ : # of features) which grows exponentially with  $d$ .
- Since each cell must contain at least one point, the number of training data grows **exponentially!**

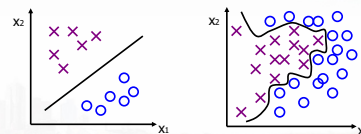


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## Representation


- Each pattern is represented as a point in  $d$ -dimensional feature space
  - Choice of features and their invariance properties are domain-specific
- Good representation implies
  1. *small* intra-class variation,
  2. *large* inter-class separation and
  3. *simple* decision boundary



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## Classifiers



- Designing Classifiers
- Learning from Examples
- Issues on Classifiers
- Statistical Pattern Recognition

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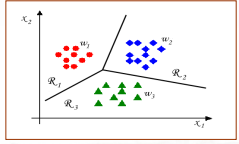
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## Classifiers

- After Representation, patterns are represented in a feature space
  - **Feature Space**: set of all possible feature vectors
  - **Classifier**: a decision model or function that maps the feature space to class labels  $\{1, 2, \dots, M\}$ 
    - We consider 2-class problem
    - For M-class, design M 2-class problem 'one vs rest'



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## Designing Classifiers

- Need to decide how feature vector values determine the class
  - In most applications, it is impossible to design classifiers from "*physics of the problem*"
- The difficulties are
  - Variability in patterns of a single class
  - Variability in feature vector values
  - Feature vectors of patterns from different classes can be arbitrarily close
  - Noise in measurements

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## Designing Classifiers

- Often the only information available for the design is a training set of example patterns
  - **Training Set**:  $\{(X_i, Y_i), i = 1, \dots, n\}$ 
    - Take representative patterns of known category and obtain the feature vectors
  - Now learn an appropriate function  $h$  as classifier
    - Model Choice
  - Test and validate the classifier on more data
    - Noise in measurements

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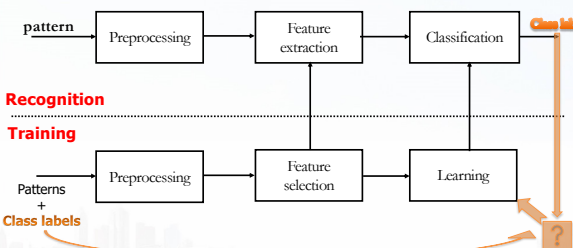
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## Learning from Examples

- Designing a classifier is learning from examples



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## Learning from Examples

- Nature of feedback determines the capability of the learning problem
  - **Supervised Learning**
    - The true label for each feature vector
  - **Reinforcement Learning**
    - Noisy assessment of performance
  - **Unsupervised Learning**
    - No feedback on the true labels

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## Learning from Examples

(Generalization)

- **Errors** on the **training set** do not necessarily tell how good is the classifier
  - Any classifier that amounts to only store the training set is useless
- Interested in the '**generalization ability**'
  - The ability of a classifier to produce correct results on **novel** patterns.



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## Learning from Examples

(Generalization)

- How can we **improve generalization ability**?
  - More training examples
    - i.e., better model estimates
  - Simpler models usually yield better performance.
    - Occam's Razor



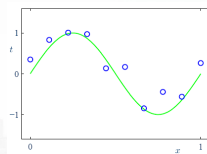
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## Learning from Examples

(Generalization)

- **Regression** example:
  - plot of 10 sample points for the input variable  $x$  along with the corresponding target variable  $t$  (assuming some noise). Green curve is the true function that generated the data.



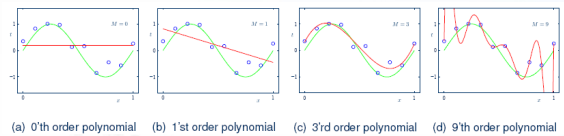
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## Learning from Examples

(Generalization)

- **Regression** example:
  - plots of polynomials having various orders, shown as red curves, fitted to the set of 10 sample points.



(a) 0th order polynomial (b) 1st order polynomial (c) 3rd order polynomial (d) 9th order polynomial



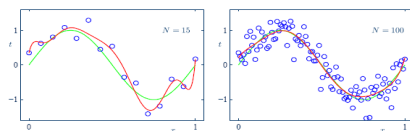
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## Learning from Examples

(Generalization)

- **Regression** example:
  - plots of 9th order polynomials fitted to 15 and 100 sample points



(a) 15 sample points

(b) 100 sample points



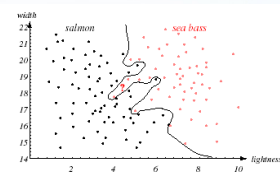
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## Example

(Salmon vs Bass Classification)

- 2D Features leads to better separation



**FIGURE 1.5.** Overly complex models for the fish will lead to decision boundaries that are complicated. While such a decision may lead to perfect classification of our training samples, it would lead to poor performance on future patterns. The novel test point marked  $t$  is evidently most likely a salmon, whereas the complex decision boundary shown leads it to be classified as a sea bass. From: Richard O. Duda, Peter E. Hart, and David G. Stork, *Pattern Classification*. Copyright © 2001 by John Wiley & Sons, Inc.



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## Example

(Salmon vs Bass Classification)

- 2D Features leads to better separation

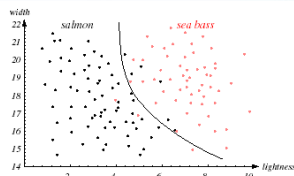


FIGURE 1.6. The decision boundary shown might represent the optimal tradeoff between performance on the training set and simplicity of classifier, thereby giving the highest accuracy on new patterns. From: Richard O. Duda, Peter E. Hart, and David G. Stork, *Pattern Classification*. Copyright © 2001 by John Wiley & Sons, Inc.



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## Overfitting

- Models complex than necessary lead to **overfitting**
  - i.e., **good** performance on the **training (seen)** data but **poor** performance on **novel (unseen)** data
- How can we adjust the complexity of the model?
  - not very complex or simple
  - Are there principled methods for finding the best complexity?



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## Domain Knowledge

- When there is insufficient training data, **incorporate domain knowledge**:
  - Model how each pattern is generated
    - analysis by synthesis
    - not easy! (e.g., recognize all types of chairs).
  - Incorporate some knowledge about the pattern generation method.
    - e.g., optical character recognition (OCR) assuming characters are sequences of strokes



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## Context

- Utilizing **Side Information**

*How mch  
info mation are  
yu mi sing*



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## Classifier Combination

- Performance can be improved using a **“pool”** of classifiers.
  - How should we combine multiple classifiers?



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## Why Classifier Combination works? A simplified explanation

Expected Result



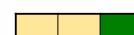
M<sub>1</sub> (66.6%)



M<sub>2</sub> (66.6%)



M<sub>3</sub> (66.6%)



} Majority Voting

Ensemble (100%)



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## Classification Error

- Each classification is associated with a risk
  - e.g., classification error involving costs for different errors
- How can we incorporate knowledge about such risks?
- Can we estimate the lowest possible risk of any classifier?



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## Main Sources of Error in Classifier Design

$$P(\omega_i / \mathbf{x}, D_i) = \frac{p(\mathbf{x} / \omega_i, D_i) P(\omega_i)}{\sum_j p(\mathbf{x} / \omega_j, D_j) P(\omega_j)}$$

- **Bayes error**
  - The error due to overlapping densities  $p(\mathbf{x} | \omega_i)$
- **Model error**
  - The error due to choosing an incorrect model.
- **Estimation error**
  - The error due to incorrectly estimated parameters
  - Inadequate training samples

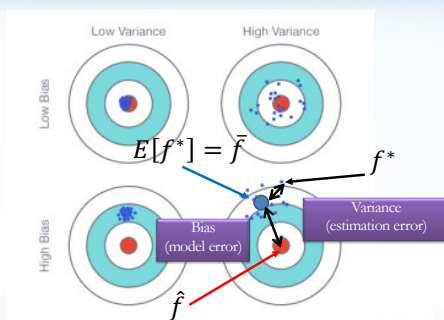


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## Bias and Variance



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## Computational Complexity

- How does an algorithm scale with
  - the number of feature dimensions
  - the number of patterns
  - the number of categories
- Brute-force approaches might lead to perfect classifications results but usually have impractical time and memory requirements.
- Consider tradeoffs between computational complexity and performance.



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## Statistical Pattern Recognition

- The classifier should perform well despite inherent variability of patterns and noise in feature extraction and/or in class labels as given in training set
- **Statistical Pattern Recognition**
  - An approach where the variabilities are captured through probabilistic models

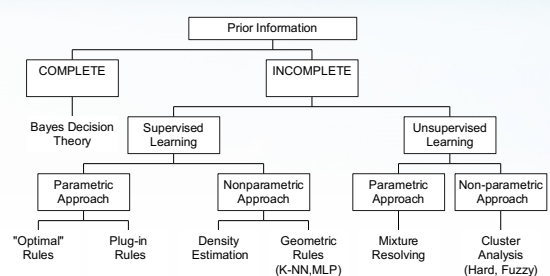


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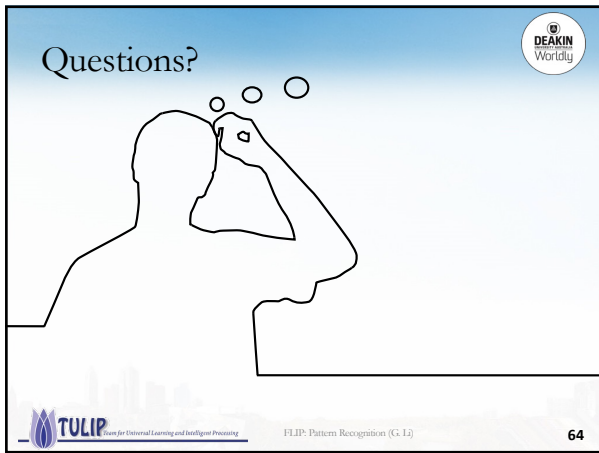
## Statistical Pattern Recognition



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