

Forecasting Supply Chain Demand by Clustering Customers

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Abstract: Demand forecasts are essential for managing supply chain activities but are difficult to create when collaborative information is absent. Many traditional and advanced forecasting tools are available, but applying them to a large number of customers is not manageable. In our research, we use data mining techniques to identify segments of customers with similar demand behaviors. Historical usage is used to cluster customers with similar demands. Once customer segments are identified, a manageable number of forecasting models can be built to represent the customers within the segments.

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1. INTRODUCTION

Supply chains have existed since the onset of industrialization, but the study of supply chains is relatively new (Janvier-James, 2012). The overall objective of a supply chain is to transform and transport materials or products, add value, and satisfy the demand of each step of the process (Janvier-James, 2012). Understanding downstream demand is prerequisite to accomplishing the overall supply chain objective (Carbonneau et al., 2008). The traditional supply chain behaviors where customers placed orders and generally advised their demand requirements are no longer prevalent; nowadays, responsibility for inventory management and forecasting has often shifted upstream to the vendor. Collaborative Forecasting Planning & Replenishment (CFPR) and Vendor Managed Inventory (VMI) are two strategies where forecasting responsibility is transferred to the supplier (Holweg et al., 2005).

Forecasting is sometimes complicated by the fact that downstream supply chain members cannot or will not share information to support building the forecast (Holweg et al., 2005). Sharing information between supply chain members can be hindered by a general reluctance or inability of supply chain partners to share forecast data (Kembro and Näslund, 2014). When collaborative information is not available, the supplier must rely on historical data and qualitative knowledge of the marketplace to build the forecast.

Creating a forecast without the benefit of customer information is not a new activity. For example, seminal research in forecasting with time series analysis was published nearly 50 years ago (Box and Jenkins, 1968). However, traditional statistical methods are less effective when there are many downstream supply chain members

exhibiting a variety of usage patterns, particularly when the usage patterns are non-linear (Aburto and Weber, 2007).

This paper proposes a methodology for forecasting based on demand behaviors of segments of customers. Data mining techniques are utilized to interpret historical usage and the effects of external factors to develop a prediction method that can accurate forecast demand.

The remainder of the paper is organized as follows: the next section is a review of the literature for the topics of CFPR, VMI, customer segmentation, and forecasting methods. Following the state of the art are sections on methodology, case study results, and discussion. We close with a conclusion and present suggestions for future research.

2. LITERATURE REVIEW

2.1 Collaborative Forecasting, Planning & Replenishment

Communication between supply chain members is beneficial for building better forecasts and improving competitiveness (Vachon et al., 2009); collaboration is the key to successful CFPR. Downstream information is transmitted from customer to supplier through a variety of modes including electronic data exchange, forecasts, and interaction between personnel of the supply chain partners.

Despite the benefits of CFPR, research has shown that in practice collaboration frequently does not prevail (Holweg et al., 2005). One factor inhibiting CFPR is the lack of information technology with sufficient sophistication to enable data sharing. Data sharing is not possible if supply chain partners' computing systems are inadequate or incompatible (Hernández et al., 2014). When electronic data sharing is not possible, CFPR can still be accomplished

through manual preparation and sharing of information. The labor and efforts, however, limit the scope of this method (Holweg et al., 2005). Finally, a significant enabler of CFPR is trust and personal relationships between personnel within the partner organizations (Wang et al., 2014), the absence of trusting relationships further hinders information sharing. While CFPR is an important and beneficial component of supply chain performance, if it does not exist, other strategies must be employed to build a forecast. These methods are discussed in the following sections.

2.2 Vendor Managed Inventory (VMI)

In the case of VMI, responsibility for forecasting lies entirely with the supplier. Ideally, the supplier in a VMI strategy has access to downstream information sources including consumption rates, inventory levels, and forecasts (Achabal et al., 2000). Research has shown that VMI strategies are effective at increasing supply chain efficiency, reducing overall costs in the supply chain, and increasing supply chain competitiveness (Achabal et al., 2000, Jung et al., 2005). Despite a direct link between supply chain performance and information sharing (Forslund and Jonsson, 2007), supply chain partners are sometimes unwilling or unable to share useful forecasting information (Kembro and Näslund, 2014, Holweg et al., 2005). When collaborative information is absent, the supplier must rely on alternate methods to ensure its ability to satisfy demand.

2.3 Customer Segmentation

In a VMI arrangement where forecast information does not exist, the supplier must develop a forecast with the information it has available, that information is typically historical data. While statistical methods exist for developing forecasts based on historical data, it is impractical to attempt to build individual forecasts for a large number of unique customer demands. Therefore, grouping customers into logical segments is necessary so that a small number of forecast models can be utilized to represent the total customer population.

There are several methods for segmenting a population of customers, and it is important to carefully select a suitable clustering algorithm to obtain accurate results (Kashwan and Velu, 2013). Rudimentary segmentation based on geographic location or customers' industry is tempting since it is relatively easy. However, the demand characteristics within these segments may be very different and therefore rudimentary segmentation is not a suitable method (Shapiro, 2007). There are several more advanced segmentation methods which are categorized as partitioning, hierarchical, density-based, grid-based and model-based (Han and Kamber, 2006) – of these, the most common are hierarchical and partitioning (Le et al., 2009, Chakraborty, 2013).

Partitional clustering is more suitable for handling large data sets due to lower computational costs. The most common partitioning method, k-means, appears frequently in literature. It is not a new technique, appearing in Fisher (1958) and further developed by MacQueen (1967). With k-means, a set of N data point are grouped into K clusters with the mean of each cluster becoming its identifying location.

Despite its frequent use, k-means has failings due to it ignores natural cluster pattern and rigidly assigns points to individual groups (MacKay, 2003).

An alternative clustering strategy to k-means is Artificial Neural Networks (ANN) and the related Kohonen Self-Organizing Maps (SOM) (Altintas and Trick, 2014). SOM was formally developed by Kohonen as an unsupervised alternative to traditional ANNs (Kohonen, 1990). Unlike k-means where the number of clusters must be pre-defined, ANNs are unsupervised; the number of clusters is part of the ANN's output.

Several variants of both k-means and ANNs have been developed to overcome some of their failings. These include the addition of fuzzy logic to avoid the rigid assignment of points to clusters (MacKay, 2003). Fuzzy logic allows the identification of groups with similar attributes (Barajas and Agard, 2014) and when combined with partitional clustering it allows flexibility of assigning points proportionally to more than one cluster. The variants are titled with various names that describe their content, such as soft k-means, fuzzy k-means, and fuzzy ANNs.

2.4 Forecasting Methods

Forecasting tools based on elementary and advanced statistical methods have proven useful to predict future demand when the situation is correct for their application (Kuo, 2001). More advanced statistical methods, such as genetic algorithm initiated fuzzy networks (GFNN) have shown the potential to improve on the results provided by traditional forecasting methods (Kuo, 2001). These methods were popular due to easy implementation, and in cases where external factors were not influential, they provided usable information. However, research has found that simple statistical methods tend to amplify the Bullwhip effect (Carbonneau et al., 2008).

More advanced time series methods such as auto-regressive integrated moving average (ARIMA), and Winter's method were developed (Chang et al., 2011). ARIMA is widely used for forecasting, but has less value for non-linear patterns (Pai and Lin, 2005). Researchers have applied more sophisticated methods to traditional statistical tools. For example, Ferbar et al. (2009) attempted to obtain better results from exponential smoothing by incorporating wavelet denoising into it. Results attained showed improvement over exponential smoothing, but did not compare with other forecasting tools.

Historical sales levels might give an indication of demand, but they do not account for exogenous variables. Data mining with decision making algorithms is one approach to understanding the historical data, incorporating the exogenous factors, and eventually producing useful results (Kusiak, 2007).

Artificial neural networks (ANNs) were identified as potentially suitable for supply chain forecasting in the 1990's (Leung, 1995) and have since been found to be very effective for developing forecasts. The ANNs architecture known as multi-layer perceptron (MLP) with back propagation is commonly used (Beccali et al., 2004). However, Chang et al. (2011) point out some shortcomings with back propagating

models. They suggest that a modified ANN can provide a better result. The modification proposed by Chang et al. (2011) involves incorporating genetic algorithms (GAs) into the ANN as an improvement to define the ANN prior to training. GAs, first introduced by John Holland in 1975, are sometimes used to configure the topography of ANNs (Kaylani et al., 2010).

The problem of establishing the desired level of complexity in an ANN model is discussed by Efendigil et al (2009). In research conducted, they conclude that model complexity is determined by the number of hidden layers which could be heuristically determined. Furthermore, they employ fuzzy logic in an ANN to overcome the limitations of using conventional mathematical tools. The adaptive network-based fuzzy inference system (ANFIS) was employed as well. The benefit to ANFIS is that it allows human knowledge to define the input-output mapping (Jang, 1993). The inclusion of a priori knowledge allows the user to influence the direction of the ANN model rather than letting the model operate unsupervised.

Another modification to forecasting with ANNs that appears frequently in the literature involves incorporating a fuzzy component (Chang et al., 2011, Efendigil et al., 2009, Kuo, 2001, Neto et al., 2011) and others. Fuzzy logic is used to improve decision making processes by avoiding the constraint of yes/no binary decisions (Barajas and Agard, 2014). In the case of ANNs, fuzzy logic allows observations to hold proportional membership in multiple nodes.

While hybrid models have received much attention in the literature, Pai and Lin (2005) used a different approach. Rather than combining ANNs and fuzzy logic, they combined support vector machine (SVM) with ARIMA. In their research, Pai and Lin found that the hybrid model performed better than either SVM or ARIMA. However, their model was not compared to other forecasting tools. SVM is a member of the machine learning family and as with ANNs, it is generally associated with classification problems. Developments in the field of SVM have led to strategies such as soft margins (Campbell and Ying, 2011). Soft margins allow flexibility in the model, similar to applying fuzzy logic, and allow the data to be fit less rigidly.

3 METHODOLOGY

The literature review shows that developing forecasts without collaborative information is possible, and that hybrid methods can provide improved accuracy over traditional methods. However, it does not answer our problem that the data used for forecasting, regardless of the method used, needs to be sufficiently complete and accurate prior to building a forecast model. Here we develop a methodology that addresses data accuracy and takes advantage of the advances made in customer segmentation and forecasting.

Our methodology includes three stages: data preprocessing, segmentation, and forecasting. Fig. 1 illustrates the sequence of the stages and the linkage between activities.

Preprocessing

Transform data into vectors
Remove outliers
Reduce Bullwhip effect

Segmentation

Customer
Segmentation

Segments
OK?

No

Forecasting

Forecast
Segments

Fig. 1: Methodology

3.1 Preprocessing

Prior to attempting to analyze the case study data, the important stage of evaluating and resolving data quality had to be addressed (Kantardzic, 2011). In our case study, the supplier was able to provide four years of delivery activity including delivery dates, quantities, locations, and industry SIC code. Although the data was extracted from actual delivery activities, some information created outliers and distorted true behavior. Administrative entries created false spikes in quantities, and new or lost customers created false periods of zero-usage.

When preprocessing data, one must be careful to clean the data enough to allow discovery of useful patterns of information within the data while not removing valuable information. To facilitate this, customers were evaluated on a yearly basis. For example, the yearly evaluation allowed the data from a new or lost customer to be retained for the years where it was valid. Outliers in the data were identified through several simple statistical methods. Customers whose total consumption were nearly zero or negative were removed. Customers with spikes in quantities were identified and removed by evaluating the median and standard deviations in the quantities.

3.2 Segmentation

Customers were segmented using the computer program R (R Core Team, 2014) using k-means. The segmentation was based on monthly volume of product delivered and calculated with Euclidean distance measurement. Determining the optimum number of clusters to use in K-means is arbitrary (Kantardzic, 2011), however some guidance is given by applying Hartigan's Number which provides a recommended number of clusters based on the data presented to its algorithm (Madigan, n.d.). Results were evaluated followed by an iterative preprocessing and re-clustering.

3.3 Forecasting

Once the customers were segmented, forecasting models were applied to assess the viability of the segments. Creation of customer segments based on consumption behavior allowed for simple forecasting methods tailored for each segment. For example, segments with seasonal effect are treated differently from those with increasing or decreasing trends.

4 CASE STUDY

4.1 Context

The context of the case study for our research is a supplier of bulk materials which are used for a variety of processes in manufacturing, food packaging, and medical services (we use “BM” and “BM supplier” in this paper to preserve the industry partner’s anonymity). Points of use inventories of BM are managed by the BM supplier (vendor managed inventory); demand is driven by usage in the customers’ various operations. Those demands, in turn, are influenced by internal and exogenous variables. The resulting individual customer demand profiles vary and exhibit trends, seasonality, and stochastic properties. To forecast inventory requirements (the dependent variable), various factors (the independent variables) such as industry type, location, seasonality of demand, and other factors are considered. BM usage in some industries (e.g. fishing) has seasonal patterns. Other industries (e.g. aerospace manufacturing) have requirements that vary according to sales levels. The BM product requires specialized transportation and storage facilities which are expensive and not quickly available. Therefore, adjusting point of use storage capacity is avoided.

In our case study, the supplier is responsible for maintaining an uninterrupted supply at their customers’ point of use. Short-term demand forecasts are generated based on historical usage; current demand and shipments are triggered by telemetric data obtained from level sensors in the point of use storage tanks. A commitment to ensuring an uninterrupted inventory at customers’ sites and lack of medium and long-range forecast data forces the supplier to be conservative with future capacity decisions.

Data for delivery instances of BM is recorded, including customer, date, location, and quantity. Unfortunately, the number of records, over 200,000 per year, has resulted in a surfeit of data to interpret with traditional forecasting methods. Additionally, although there are similar strategies in place for products such as electrical distribution, there is no current method to assess and predict the impacts of external factors such as location, season, industry of user, and climate on bulk product demand.

4.2 Data Preprocessing

Our data consists of four years of history with nearly one million observations of delivery events, including customer, distribution center, quantity, and product type. We need to vector the data into monthly deliveries per customer per product, resulting in approximately 3500 time series vectors. Time-series data must be carefully prepared prior to clustering (Liao, 2005) with attention given to whether it

should be shifted to reflect similar behaviors that are offset in time; a process known as dynamic time warping (Berndt and Clifford, 1994). Three types of errors were apparent in the data and corrected with preprocessing.

Firstly, the data is a record of deliveries from the supplier, not of consumption by the customer. Point of use storage allows the supplier to deliver based on its own schedule and not necessarily on the customers’ consumption needs. Using the data in this form would impose a Bullwhip effect. To overcome the Bullwhip effect possibility, the values were smoothed with moving weighted averaging. Moving average was chosen because it is a simple method and has shown to be effective in reducing Bullwhip effect (Chen et al., 2000). Additionally, simple data processing methods are often proven to be as effective as more complex ones for data mining (Witten et al., 2011).

Second, administrative adjustments (debit and credit quantities) showed deliveries that were negative or greater than the equipment capability. These were removed by comparing standard deviation against median quantities; high variance vectors were removed.

Lastly, new or lost customers would exhibit false demand behavior if all four years of records were included since they have a period of zero demand. This was resolved by splitting the data into customer-year vectors. That is, every customer vector becomes four individual vectors with one year of data in each. Customer-year vectors with zero demand were then separated and the customers’ true demand behavior remained.

4.3 Segmentation

The initial clustering results were not satisfactory due to outliers in the data. As illustrated in Fig. 2, the majority of the customers fell into a single segment (Cluster #8). Investigation into the members of both the very large and very small clusters revealed outliers that had escaped detection in the initial data preprocessing. Adjustments to the filtering criteria in the preprocessing eventually produced better results.



Fig. 2: Initial Segmentation Results

After removal of outliers, the data was normalized and then re-segmented with k-means. The new segments, as illustrated in Fig. 3 are more evenly distributed. While a dominant segment remains (Cluster #3), there are sufficiently distinguishable segments for forecast testing and evaluation within those segments.

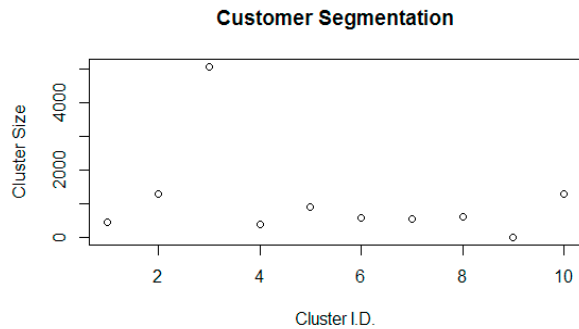


Fig. 3: Revised Segmentation

4.4 Forecasting

Reviewing a sample from one of the resulting clusters reveals a definite pattern. In Fig. 4, you can see that the majority of the customers in this cluster exhibit a seasonal pattern. Fig. 4 also reveals that some customers' data is significantly different from the main population of the group, but it was not detected as an outlier during the preprocessing stage.

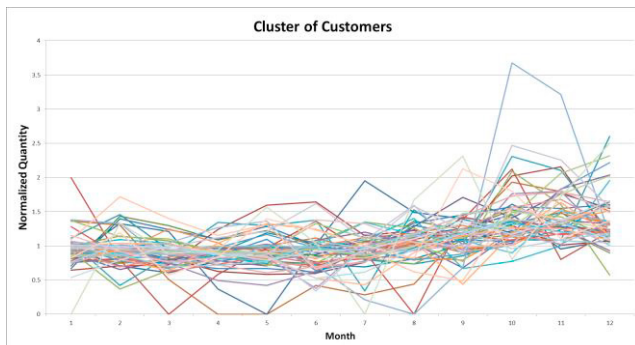


Fig. 4: Demand behavior within a cluster

5 DISCUSSION

The literature reviewed in section 2.3 above reveals a significant amount of research regarding methods of segmenting data into interesting clusters. And while data preprocessing is generally acknowledged as an important step (Kantardzic, 2011, Miller, 2009, Witten et al., 2011), it is not discussed in detail. During this study, several different clustering techniques, such as K-means, self-organizing maps (SOMs), and fuzzy clustering were explored. With each iteration of preprocessing and clustering it was revealed that the presence of outliers in the data had much greater influence on the results than the algorithm used to create the clusters. Eventually, the data analyst must decide when to stop removing outliers. In Fig 4, some customer data remains that could be categorized as outliers. However, the number of outliers remaining is significantly small enough that the overall behavior of the cluster is not adversely affected and therefore removal is not necessary. Once clusters of customers have been established they can be summarized into a single behavior pattern.

6 CONCLUSION AND FUTURE RESEARCH

This paper has presented a method for transposing a high number of individual customers into a small number of clusters of customers with similar demand behavior. Forecasting demand for the clusters is a manageable task. Many forecasting strategies use statistical tools to predict future demand of specific customers or products. In the context of our case study, it is impractical to attempt to build customer-specific forecasts due to the large number of customers. We have overcome this by segmenting customers based on behavior. We are then able to build a manageable number of forecast models and apply them within each customer segment.

Understand the cause for an overall change in demand allows the BM supplier to decide whether a change in capacity is necessary due to trends, or whether the change is due to seasonal effect and no capacity changes are necessary. In the case study, customers with demand behavior that does not follow a pattern were treated as outliers and removed. Further research is necessary to develop a method to classify these customers and reincorporate them into the model.

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