

# Exergetic efficiency definitions for oil and gas platforms

Tuong-Van Nguyen<sup>a,\*</sup>, Mari Voldsund<sup>b</sup>, Brian Elmegaard<sup>a</sup>, Ivar Ståle Ertesvåg<sup>c</sup>

<sup>a</sup>*Section of Thermal Energy, Department of Mechanical Engineering, Technical University of Denmark, Building 403, Nils Koppels Allé, 2800 Kongens Lyngby, Denmark*

<sup>b</sup>*Department of Chemistry, Norwegian University of Science and Technology, Høgskoleringen 5, 7491 Trondheim, Norway*

<sup>c</sup>*Department of Energy and Process Engineering, Norwegian University of Science and Technology, Kolbjørn Hejes vei 1b., 7491 Trondheim, Norway*

---

## Abstract

Exergy-based efficiencies are a measure of the thermodynamic perfection of systems and processes: they can be expressed for any plant for which the inputs and outputs are expressible in terms of exergy. However, an exact formulation of this criterion for oil and gas platforms is made difficult by the great differences in working conditions, design setups and operating strategies amongst them. In this paper, possible interpretations of exergetic efficiencies for these specific systems are presented and discussed. We assessed and compared several formulations of exergetic efficiencies introduced in the literature for relatively similar processes. They were then applied to four real-case studies of the North Sea region and their relevance was evaluated. The ‘input-output’ exergy efficiency was above 98% in all cases while the corresponding figures for the ‘consumed-produced’ exergy efficiency were between 10% and 75%, depending on the considerations on the ‘consumed’ and ‘produced’ exergies and on the case study.

**Keywords:** Exergy, Efficiency, Oil and gas platforms

---

## 1. Introduction

Conventional indicators for evaluating the performance of oil and gas platforms, such as the power consumption per unit of oil equivalent produced, or the amount of carbon dioxide produced per unit of oil equivalent, present inherent limitations. Each oil field has different natural characteristics (e.g. gas-to-oil ratio, well-fluid composition, field size) and comparing different facilities with these metrics could be misleading. They provide useful information on the energy use of the onsite processes, but they cannot be used alone to compare the performance of different facilities [1,2].

Exergy Analysis is a quantitative assessment method that is based on both the First and Second Laws of Thermodynamics. This thermodynamic method presents advantages over a conventional energy analysis: it pinpoints the locations and types of the irreversibilities taking place within a given system. As emphasised by Rivero [3], the application of the exergy concept in the petroleum industry would provide more detailed and consistent information on the performance of petrochemical systems. The exergy concept was introduced in the literature along with the concept of exergetic efficiency, which aims at measuring the degree of thermodynamic perfection of the process under investigation.

Formulations of exergy-based criteria of performance have been proposed from the middle of the 20<sup>th</sup> century, with, amongst others, the contributions of Nesselmann [4] and Fratzscher [5,6]. Both works reported the definition of the exergetic efficiency of a given system as the ratio of its total exergy output to its total exergy input and discussed the advantages and drawbacks of such formulation. Grassmann [7] and Nesselmann [8] suggested to define the exergetic efficiency as the ratio of the part of the exergy transfers that contribute to the transformations taking place,

---

\*Principal corresponding author. Tel.: +45 4525 4129

Email addresses: [tungu@mek.dtu.dk](mailto:tungu@mek.dtu.dk) (Tuong-Van Nguyen), [mari.voldsund@ntnu.no](mailto:mari.voldsund@ntnu.no) (Mari Voldsund), [be@mek.dtu.dk](mailto:be@mek.dtu.dk) (Brian Elmegaard), [ivar.s.ertesvag@ntnu.no](mailto:ivar.s.ertesvag@ntnu.no) (Ivar Ståle Ertesvåg)

## Nomenclature

$T$	Temperature, K	kin	kinetic
$\bar{e}$	specific exergy (molar), J/mol	m	mechanical
$\dot{E}$	Exergy rate, MW	ph	physical
$\dot{S}$	Entropy rate, MW/K	pot	potential
$e$	specific exergy (mass), J/kg	Q	heat
$h$	specific enthalpy (mass), J/kg	t	thermal
$p$	pressure, MPa	W	work
$s$	specific entropy (mass), J/(kg·K)	<i>Subscripts</i>	
$y$	component/sub-system exergy ratio	0	dead state
$z$	pollutant molar fraction	cool	cooling medium
<i>Abbreviations</i>		cv	control volume
EOS	Equation of State	cv	control volume
GOR	Gas-to-Oil Ratio	d	destruction
HP	High Pressure	f	fuel
LHS	Left-Hand Side	feed	feed
LP	Low Pressure	fg	fuel gas
NHV	Net Heating Value, kJ/kmol	gen	generation
OP	Overall Plant	h	hypothetical
PP	Processing Plant	i	chemical compound
RHS	Right-Hand Side	in	inlet
TEG	Triethylene Glycol	j	stream
UT	Utility Plant	k	component
WOR	Water-to-Oil Ratio	l	loss
<i>Greek letters</i>		min	minimum
$\beta$	chemical exergy correction factor	mix	mixture
$\varepsilon$	exergetic efficiency	mt	metal
<i>Superscripts</i>		out	outlet
*	relative	p	product
+	increase	tot	total
-	decrease	tr	transit
ch	chemical		

i.e. ‘consumed’ exergy, to the part of the exergy transfers that are generated within the system, i.e. ‘produced’ exergy. Based on these works, Baehr [9,10] proposed his own expressions for these two terms. He also stressed the difficulty of providing a non-ambiguous definition of an exergetic efficiency, as different views on ‘consumed’ and ‘produced’ exergies may apply.

Further advances within this field include the studies of Brodyansky [11], Szargut [12–14], Kotas [15] and Tsat-

saronis [16,17]. Brodyansky [11] suggested a systematic procedure for calculating the ‘produced’ and ‘consumed’ exergies, without regarding whether they are useful to the owner of the system. His work was based on the concept of ‘transit exergy’ introduced by Kostenko [18] and discussed also in Sorin et al. [19]. Szargut [12–14], Kotas [15] and Tsatsaronis [16,17] proposed to consider only the exergy transfers representing the ‘desired’ exergetic output and the ‘driving’ exergetic input of the system, leading to the concept of ‘product’ and ‘fuel’ exergies. Such considerations must be consistent with the purpose of owning and operating the system of investigation [20–23], both from an economic and a thermodynamic prospect. Lazzaretto and Tsatsaronis [24,25] suggested a systematic procedure for defining the exergetic efficiency at a component level. However, at a process level, a unique formulation may not be available and several expressions may be appropriate [16].

Various expressions of exergetic efficiency for separation systems have been illustrated in the literature and different considerations have applied [11,15,16,26]. Cornelissen [27] investigated three of the proposed formulations for an Air Separation Unit (ASU) and a Crude Distillation Plant (CDP). Different values were obtained, illustrating the variations and lack of uniformity across the exergetic efficiency definitions [9,10,28]. However, the only studies dealing exclusively with oil or gas processing plants are the works of Oliveira and Van Hombeeck [29], Voldsund et al. [30,31], and Rian and Ertesvåg [32], who proposed their own interpretations of ‘product’ and ‘fuel’ exergies.

The literature seems to contain little, if none, on (i) a uniform performance parameter for oil and gas installations, (ii) the application of the exergetic efficiency concept, and on (iii) the comparison of the different definitions. This study is aimed at addressing these gaps and is part of two broader projects conducted at the Norwegian University of Science and Technology (NTNU) and at the Technical University of Denmark (DTU). Four main steps were required in the present study:

- derivation and formulation of exergetic efficiencies for offshore platforms;
- modelling and simulation of four oil and gas facilities in the North Sea region;
- application of the different expressions;
- analysis of their sensitivity to changes in design and operating conditions.

This paper is structured as follows: Section 2 presents the oil and gas platforms investigated in this study and Section 3 describes the theoretical background. Section 4 reports the derived definitions of exergetic efficiencies, while Section 5 illustrates the comparison of the four oil and gas facilities. The pertinence of the different exergetic efficiency formulations is discussed in Section 6 and concluding remarks are outlined in Section 7.

## 2. System description

### 2.1. General overview

Offshore platforms are large structures with facilities to extract and process petroleum from subsea reservoirs. Petroleum is a complex multiphase mixture: it contains a large spectrum of chemical compounds, from light hydrocarbons in gaseous form (e.g. methane) to heavy ones in liquid phase (e.g. naphthenes and cycloalkanes) and is extracted along with subsurface water. The aim of these offshore facilities is to separate efficiently the different phases to satisfy the different process and export constraints, and to maximise the hydrocarbon production. Crude oil mostly consists of medium- to heavy hydrocarbons in liquid form, while natural gas mostly consists of light-weight alkanes. Differences across offshore platforms can be summarised as follows [33–40]:

- reservoir characteristics (e.g. initial temperature and pressure);
- fluid properties (e.g. chemical composition, gas- and water-to-oil (GOR and WOR) ratios);
- product requirements (e.g. export pressure and temperature, chemical purity);
- operating strategies (e.g. oil and gas recovery, gas treatment, condensate export).

These differences induce variations in temperatures, pressures and flow rates throughout the system as well as in demands for compression, heating, cooling, dehydration, desalting and sweetening. The structural design of these facilities stays nevertheless similar.

Oil, gas and water enter one or several production manifolds in which the well-fluid streams are mixed and the pressure reduced to ease separation between the liquid and gaseous phases. The well-fluid streams are fed into a separation system where oil, gas and water are separated by gravity in one to several stages, with throttling in between. Crude oil leaving the separation train enters a treatment and export pumping section. Gas leaving the separation and oil pumping steps enters the recompression train. It is cooled, sent to a scrubber where condensate and water droplets are removed, and recompressed to the pressure of the previous separation stage. It is then sent to the gas treatment train, where it is purified and possibly dehydrated by triethylene glycol (TEG). Gas may be compressed for export to the shore, lift or injection.

Condensate removed from the recompression and gas treatment trains is (i) either sent back to the separation train and mixed with crude oil or (ii) processed apart in a condensate treatment section. Produced water enters a wastewater handling train, in which suspended particulates and dissolved hydrocarbons are removed. It is then discharged into the sea or enters an injection train where it is further cleaned and pumped to a high pressure level. In parallel, seawater may be processed onsite for further injection into the reservoir for enhanced oil recovery.

The electrical power required onsite is produced by gas turbines fuelled with a fraction of the produced gas, or, alternatively, heavy oil or diesel. The heating demand is either met by using fuel gas burners, electric heaters or by indirect waste heat recovery. The cooling demand is satisfied by using a direct cooling medium, e.g. seawater or air, or an indirect one, e.g. a glycol/water mixture. Heat exchanger networks between the several streams flowing through the system may also be integrated to promote heat integration.

Processes such as condensate treatment and natural gas liquid recovery are uncommon offshore, with only a few applications worldwide. Oil and gas treatment is generally limited to gas dehydration in the North Sea, whereas it also includes oil desalting and gas sweetening in the Gulf of Mexico. Further details on oil and gas processing are given in [41] and more specific information on North Sea platforms are given in Refs. [33,42].

## 2.2. Case studies

The four oil and gas platforms investigated within this study are located in the North Sea region and present specific design characteristics (Figure 1 and Table 1).

Table 1: Comparison of the four offshore facilities discussed in this study

Platform	A	B	C	D
<b>System characteristics</b>				
Age (years)	20	10	10	20
Gas-to-oil ratio	increasing	increasing	increasing	decreasing
<b>System products</b>				
Oil	export	none	export	export
Gas	fuel injection	fuel export	fuel injection import lift	fuel export
Condensate	export (mixed with oil)	export	export (mixed with oil)	export (mixed with gas)
Produced water	discharge	discharge	discharge	discharge injection
Seawater	cooling	cooling	cooling	cooling injection (complement)
<b>Additional processes</b>				
Dehydration	n	n	n	y
Condensate treatment	n	n	n	y
Water injection	n	n	n	y

These four platforms, although similar in terms of structural design, present significant differences in well-fluid processing and in operating conditions:

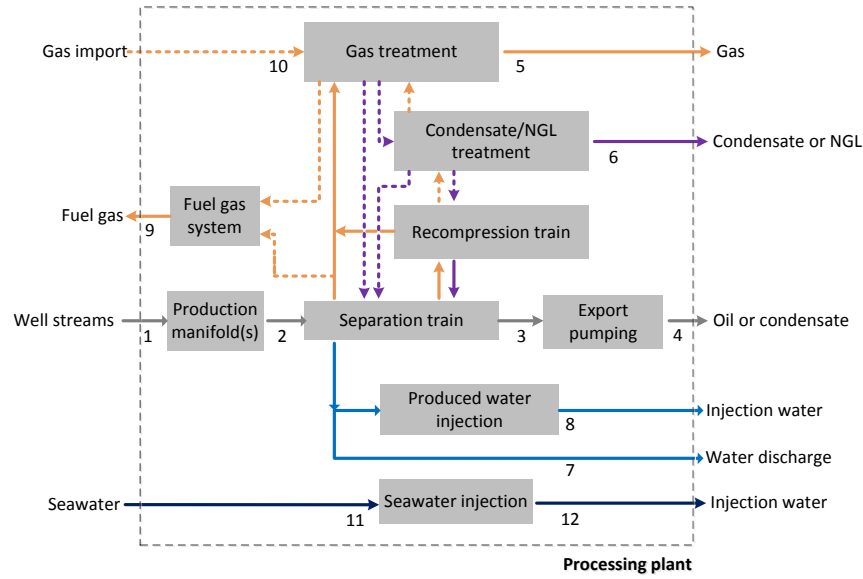


Figure 1: General overview of the processing plant

- The gas-to-oil ratio is either increasing (e.g. platforms A and B), meaning that the gas treatment train is run at full-design conditions or decreasing (e.g. platforms C and D), meaning that this subsystem is run in off-design conditions, and that anti-surge recycling is practiced to protect the compressors.
- Platforms processing heavy and viscous crude oil (e.g. platform C) or with a high propane content (e.g. platform D) require heating in the separation train to enhance vapour-liquid separation and to meet the export specifications.
- The pressure at the final stage of the separation train ( $p_3$ ) is constrained by the maximum allowable vapour pressure of the crude oil/condensate in the pipelines and shuffle tankers, and is below 3 bar for all platforms.
- The pressure of the produced oil/condensate at the outlet of the pumping section ( $p_4$ ) is either higher (e.g. platform C) or lower (e.g. platforms A, B and D) than at the outlet of the production manifold ( $p_2$ ).
- The pressure at the outlet of the gas treatment section ( $p_5$ ) is either higher (e.g. platforms A, C and D) or lower (e.g. platform B) than at the inlet of the separation system ( $p_2$ ). There is a need for gas compression in three of the four platforms.

The reader is referred to two previous works conducted by the same authors for further details on the studied platforms [43,44].

### 2.3. Modelling and simulation

The process simulations were carried out with Aspen HYSYS® [45] and Aspen Plus® version 7.2 [46], with the exception of the glycol dehydration system. Simulations of the production manifolds, petroleum separation, oil pumping, gas recompression and flaring were based on the Peng-Robinson equation of state (EOS) [47]. The water purification and injection processes were simulated based on the Non-Random Two Liquid (NRTL) model [48] and the dehydration process on the Schwartzentruber-Renon EOS [49,50]. Power generation was simulated by using the in-house tool DNA (Dynamic Network Analysis), which is a program developed at the Technical University of Denmark [51].

### 3. Theoretical background

#### 3.1. Exergy analysis

Exergy may be defined as the ‘maximum theoretical useful work (shaft work or electrical work) as the system is brought into complete thermodynamic equilibrium with the thermodynamic environment while the system interacts with this environment only’ [17,22,23]. ~~A system in thermal and mechanical equilibrium with the environment is called in environmental state and in dead state when it is also in chemical equilibrium [15].~~ In this work, the discussions on exergetic efficiencies focus exclusively on the exergy associated with mass and energy transfers, namely the ‘flow exergy’.

Unlike energy, exergy is not conserved in real processes – some is destroyed due to internal irreversibilities. On a time rate form and for a control volume with in- and outgoing flows, the exergy balance is expressed as [22]:

$$\begin{aligned}\dot{E}_d &= \sum \dot{E}_{in} - \sum \dot{E}_{out} \\ &= \sum \left(1 - \frac{T_0}{T_k}\right) \dot{Q}_k - \dot{W}_{cv} + \sum \dot{m}_{in} e_{in} - \sum \dot{m}_{out} e_{out}\end{aligned}\quad (1)$$

where  $\dot{E}_d$ ,  $\dot{E}_{in}$  and  $\dot{E}_{out}$  are the destroyed, inflowing and outflowing exergy rates, respectively.  $\dot{m}$  is the mass flow rate of a stream of matter,  $\dot{Q}_k$  and  $\dot{W}_{cv}$  the time rates of energy transfer by heat and work ( $\dot{Q} \geq 0$  indicates heat transfer to the system,  $\dot{W} \geq 0$  work done by the system),  $e$  the specific exergy of a stream of matter.  $T_0$  and  $T_k$  are the environmental and instantaneous temperatures. The subscripts *in* and *out* denote the inlet and outlet of the system, *k* the boundary of the component of interest and *cv* the control volume. The exergy destruction rate can also be calculated from the Gouy-Stodola theorem, which is, ~~on a time rate form~~, expressed as [52]:

$$\dot{E}_d = T_0 \dot{S}_{gen} \quad (2)$$

where  $\dot{S}_{gen}$  is the entropy generation rate.

Exergy destruction is also called ‘internal exergy losses’, ~~as they are~~ related to the irreversibilities taking place ~~within the system, i.e. inside~~ the control volume under study. The term exergy loss, written  $\dot{E}_l$  ~~on a time rate basis~~ [22] refers to the exergy discharged to the environment without any practical use (e.g. exergy content of exhaust gases from a gas turbine – exergy transferred to the cooling water), i.e. *outside* the control volume under study. This waste exergy is destroyed when mixed irreversibly with the environment (Figure 2) and is denoted ‘external exergy losses’ in the works of Szargut and Kotas [14,15].

Kostenko [18] and later Brodyansky [11] introduced the concept of ‘transit exergy’  $\dot{E}_{tr}$ , which is the part of the exergy supplied to a system that flows through the system without undergoing any physical or chemical transformation. By opposition, they named the fraction of the exergy flowing into the system that is not transit exergy ‘consumed exergy’ and the fraction of the exergy flowing out that is not transit exergy ‘produced exergy’. Transit exergy can be divided into the transit exergy carried with the waste streams  $\dot{E}_{tr,l}$  and carried with the utilisable streams  $\dot{E}_{tr,u}$ .

Finally, Tsatsaronis [22,53] introduced the concept of ‘fuel exergy’ and ‘product exergy’ and proposed the following nomenclature. The *product exergy* ( $\dot{E}_p$  on a time rate basis) represents the desired result of the system, expressed in terms of exergy. The product exergy term includes, according to Lazzaretto and Tsatsaronis [24,25]:

- all the exergy values to be considered at the outlet;
- all the exergy increases between inlet and outlet (i.e. exergy additions to material streams) that are in accord with the purpose of operating the system under study.

The *fuel exergy* ( $\dot{E}_f$  on a time rate basis) stands for the necessary resources used to drive the process under consideration to generate the product exergy. Fuel does *not* always correspond to a given fuel such as natural gas, oil or diesel but represents the exergetic resources utilised within the system. The fuel exergy term includes, according to Lazzaretto and Tsatsaronis [24,25]:

- all the exergy values to be considered at the inlet (e.g. exergy of the fuel gas entering a gas turbine);

- all the exergy decreases between inlet and outlet (i.e. exergy removals from material streams).

Hence, the exergetic balance becomes [22,53]:

$$\dot{E}_p = \dot{E}_f - \dot{E}_l - \dot{E}_d \quad (3)$$

The general concept of ‘fuel’ and ‘product’ has been extensively applied over the last decades to characterise the thermodynamic performance of various systems [16,17,22,54].

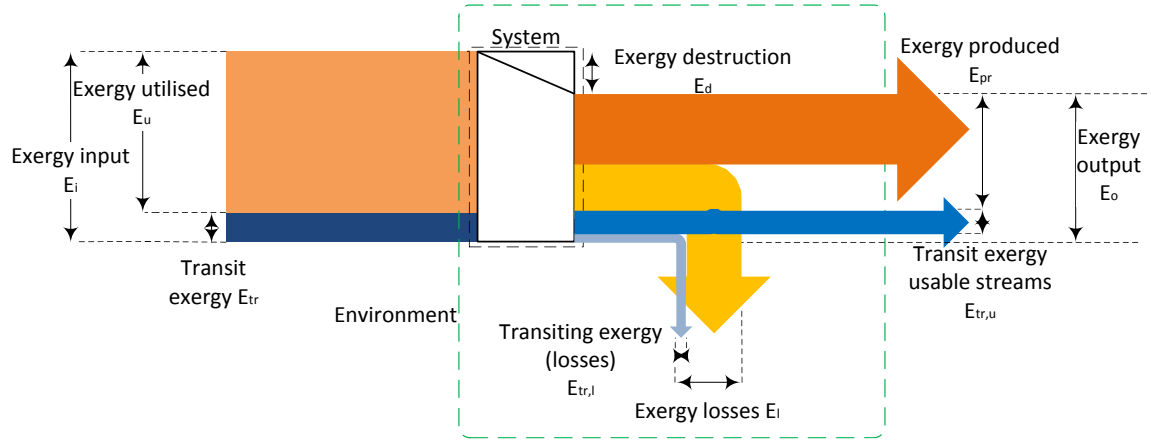


Figure 2: Conceptual representation of the exergy balance

### 3.2. Flow exergy

In the absence of nuclear, magnetic and electrical interactions, the exergy associated with a stream of matter is a function of its physical  $e^{ph}$ , chemical  $e^{ch}$ , kinetic  $e^{kin}$  and potential  $e^{pot}$  components [22]. The specific exergy of a material stream, on a mass basis, is expressed as:

$$e = e^{ph} + e^{ch} + e^{kin} + e^{pot} \quad (4)$$

Physical exergy accounts for temperature and pressure differences from the environmental state and is defined as:

$$e^{ph} = (h - h_0) - T_0(s - s_0) = \underbrace{h - h(T_0, p) - T_0(s - s(T_0, p))}_I + \underbrace{h - h(T, p_0) - T_0(s - s(T, p_0))}_{II} \quad (5)$$

where  $h$  and  $s$  are the specific enthalpy and entropy of a stream of matter per unit-of-mass, respectively. *Term I* and *Term II* refer to the temperature- and pressure-based components of the physical exergy [15], respectively, and are also named thermal  $e^t$  and mechanical  $e^m$  exergies [16].

Chemical exergy accounts for deviations in chemical composition from reference substances present in the environment. In this work, chemical exergy is calculated ~~based on the concept of standard chemical exergy discussed by Moran and Shapiro [55] and~~ using the reference environment defined in Szargut [12,56,57]. The specific chemical exergy of a given mixture  $\bar{e}_{mix}^{ch}$ , on a molar basis, is expressed as [58]:

$$\bar{e}_{mix}^{ch} = \underbrace{\sum_i \bar{x}_i \bar{e}_{i,mix}^{ch}}_I = \underbrace{\sum_i \bar{x}_i \bar{e}_{i,0}^{ch}}_{II} + \underbrace{\left( \sum_i \bar{x}_i (h_{i,mix} - h_{i,0}) \right) - T_0 \left( \sum_i \bar{x}_i (s_{i,mix} - s_{i,0}) \right)}_{III}$$

where the molar fraction, the chemical compound and the mixture are denoted by  $\bar{x}$ ,  $i$  and  $mix$ , respectively. The specific molar exergy of a given chemical compound is written  $\bar{e}_{i,mix}^{ch}$  when it is in the mixture and  $\bar{e}_{i,0}^{ch}$  when it is in a pure component state. The term  $I$  illustrates the chemical exergy of each individual chemical component in the mixture, the term  $II$  the chemical exergy of these components in an unmixed form and the term  $III$  the reduction in chemical exergy due to mixing effects.

If no chemical transformations are taking place within a separation system, the terms related to the chemical exergy of pure components cancel and the change in chemical exergy is equal to the exergy used to perform the separation work [15]. The variation of chemical exergy between the inlet and the outlet of that system, which is, in this specific case, equal to the exergy used for separation, can be expressed as:

$$\Delta \dot{E}^{ch} = \sum_k \dot{E}_k^{ch} - \dot{E}_{mix}^{ch} = \sum_k \left( \sum_i \dot{n}_{i,k} (h_{i,k} - h_{i,mix}) - T_0 \left( \sum_i \dot{n}_{i,k} (s_{i,k} - s_{i,mix}) \right) \right) = \sum_k \Delta \dot{E}_k^{ch} \quad (6)$$

where  $\Delta \dot{E}_k^{ch}$  corresponds to the exergy used for separation into each stream  $k$  exiting the system:

$$\Delta \dot{E}_k^{ch} = \left( \sum_i \dot{n}_{i,k} (h_{i,k} - h_{i,mix}) \right) - T_0 \left( \sum_i \dot{n}_{i,k} (s_{i,k} - s_{i,mix}) \right) \quad (7)$$

The specific chemical exergy of hypothetical components  $\bar{e}_h^{ch}$  is determined with the heuristic correlations of Rivero [59]:

$$\bar{e}_h^{ch} = \beta NHV_h + \sum \bar{z}_{mt} \bar{e}_{mt}^{ch} \quad (8)$$

where  $NHV$  stands for Net Heating Value,  $z_{mt}$  for the mass fraction of metal impurities,  $e_{mt}^{ch}$  for the corresponding chemical exergy and  $\beta$  for the chemical exergy correction factor.

Kinetic and potential contributions on the flow exergies were assumed to be negligible toward physical and chemical exergies. Exergy transported with work is equal to its energy and depends on the system and environmental temperatures when it is transferred with heat.

The transiting exergy associated with a stream of matter is defined as the sum of the transiting physical, chemical, potential and kinetic exergies. The transiting physical exergy for a stream  $j$  is the minimum physical exergy between the inlet and outlet of the system. It is defined, for an input and output temperature higher than the environment temperature, as:

$$\dot{E}_{tr}^{ph} = \sum_j \dot{m}_{j,tr} \cdot \min(e_{in}^{ph}(p_{in}, T_{min}); e_{in}^{ph}(p_{out}, T_{min}); e_o^{ph}(p_{in}, T_{min}); e_o^{ph}(p_{out}, T_{min})) \quad (9)$$

Similarly, the transiting chemical exergy corresponds to the chemical exergies of each chemical compound that is not transformed between the system inlet and outlet:

$$\dot{E}_{tr}^{ch} = \sum_s \dot{n}_{tr,s} \cdot \min(\bar{e}_i^{ch}, \bar{e}_o^{ch}) \quad (10)$$

The transiting exergies of an energy flow are defined as the minimum associated exergies at the inlet or outlet of the system. The concept of transiting exergy is also mentioned by Cornelissen [27], who applied this method to an air separation unit and a crude oil distillation plant. The lack of ambiguity and the complexity of the calculations were underlined, as this method requires a precise decoupling of the exergy flows into their components.

### 3.3. Exergetic efficiency

The definitions of exergetic efficiency, as presented and discussed in the open literature, can be divided into two main groups, as suggested by Lior and Zhang [28]:

- the ‘input-output’, ‘universal’ or ‘total’ exergetic efficiency, which is defined as the ratio of all outgoing to ingoing exergy flows, without any consideration on whether they are actually consumed within the process or useful to the owner of the system;



- the ‘consumed-produced’, ‘functional’ or ‘utilitarian’ exergetic efficiency, which is defined as the ratio of the exergy terms associated with the products generated within the system, i.e. the ‘produced exergy’, to the exergy terms associated with the resources expended to achieve these outputs, i.e. the ‘consumed exergy’.

### 3.3.1. Input-Output efficiency

For a given open thermodynamic system at steady-state, the exergy balance can be expressed, on a time rate form, as:

$$\sum \dot{E}_{in} = \sum \dot{E}_{out} + \dot{E}_d \quad (11)$$

where  $\dot{E}_{in}$  and  $\dot{E}_{out}$  are the exergy inputs and outputs to and from the system, associated with streams of matter and of energy, and  $\dot{E}_d$  the exergy destruction.

The ‘universal’ or ‘total’ exergetic efficiency  $\varepsilon_t$  is defined as the ratio of all exergy outflows to inflows [27,28,60]:

$$\varepsilon_t \equiv \frac{\sum \dot{E}_{out}}{\sum \dot{E}_{in}} = 1 - \frac{\dot{E}_d}{\sum \dot{E}_{in}} \quad (12)$$

This definition is claimed to be adequate when (i) the ingoing and outgoing exergy flows are converted to other forms of exergy [27] or (ii) a major part of the outflowing exergy can be considered as useful, as it is the case of power plants [28] or (iii) for dissipative processes and devices [15,61].

A variant of this ‘total’ exergetic efficiency is proposed in Fratzscher [6] and in Wall [60], excluding the exergy associated with waste products.

$$\varepsilon_t \equiv \frac{\sum \dot{E}_{out} - \dot{E}_l}{\sum \dot{E}_{in}} = 1 - \frac{\dot{E}_d + \dot{E}_l}{\sum \dot{E}_{in}} \quad (13)$$

### 3.3.2. Consumed-Produced efficiency

The concept of ‘total’ exergetic efficiency has been criticised as it takes into account all the exergetic flows entering and exiting a system, without considering whether they are utilised in the thermodynamic conversions. The ‘task’ exergetic efficiency, on the opposite, differentiates the exergy flows undergoing transformations from the exergy flows that are not affected, i.e. neither used nor produced. Grassmann [7] proposed a general formulation for an exergetic efficiency: he suggested the ratio of the intended increase to the used decrease in ability to do work. In exergy terms, this means that the exergetic efficiency should be defined as the ratio of the production of exergy that is desired  $\Delta \dot{E}^+$  to the reduction of exergy that is utilised  $\Delta \dot{E}^-$ .

$$\varepsilon \equiv \frac{\Delta \dot{E}^+}{\Delta \dot{E}^-} \quad (14)$$

It was emphasised that this performance criterion always has a value comprised between 0 and 1, as the increased ability to do work  $\Delta \dot{E}^+$  is always smaller than the decreased one  $\Delta \dot{E}^-$ . Baehr [10] proposed a variant of this formulation, considering *all* the exergy increases  $\Delta \dot{E}_i^+$  in the numerator and *all* the exergy decreases  $\Delta \dot{E}_i^-$  in the denominator. At the difference of the expression proposed by Grassmann [7], the total production and expenditure of exergy are considered, whether they are actually desired or utilised within the system:

$$\varepsilon \equiv \frac{\Delta \dot{E}_{tot}^+}{\Delta \dot{E}_{tot}^-} \quad (15)$$

It was pointed up that (i) exergetic efficiencies based on exergy differences are more sensitive to changes in the system and are therefore more suitable and (ii) different numerical values could be obtained with the formulation of exergetic efficiency proposed by Grassmann [7], as it depends on whether an exergy difference is considered as ‘useful’, ‘used’ or none of those.

Brodyansky [11] and Sorin [19] proposed to define the exergetic efficiency as the ratio of the total exergy output to the total exergy input, minus the transit exergy on both numerator and denominator. They named it the *intrinsic exergetic efficiency* and defined it as:

$$\varepsilon \equiv \frac{\sum \dot{E}_{out} - \sum \dot{E}_{tr}}{\sum \dot{E}_{in} - \sum \dot{E}_{tr}} = \frac{\sum \dot{E}_{pr}}{\sum \dot{E}_u} \quad (16)$$

where, on a time rate basis,  $\dot{E}_{tr}$  the transit exergy,  $\dot{E}_{pr}$  and  $\dot{E}_u$  the produced and used exergies, respectively, as called in the work of Brodyansky et al. [11].

A variant of the previous exergy efficiency formulation is proposed by Sorin et al. [62]. It was argued that all the produced exergy  $\dot{E}_{pr}$  is not usable, as a result of a discharge of exergy into the environment with waste products (i.e. external exergy losses). They defined therefore an alternative to the intrinsic exergetic efficiency, named the utilisable exergy coefficient, as:

$$\varepsilon \equiv \frac{\sum \dot{E}_o - \sum \dot{E}_l - \sum \dot{E}_{tr,u}}{\sum \dot{E}_i - \sum \dot{E}_{tr,u}} \quad (17)$$

Szargut [12,14,63], Tsatsaronis [54] and Kotas [15,21] argued that the exergetic efficiency should be defined as the ratio of (i) the *desired output* or *useful exergetic effect*  $\sum \Delta \dot{E}_{out}$  and (ii) the *necessary input* or *driving exergy expense*  $\sum \Delta \dot{E}_{in}$ . Both terms can be identified starting from the exergy balance put in the following form:

$$\sum \Delta \dot{E}_{in} = \sum \Delta \dot{E}_{out} + \dot{I}_{cv} \quad (18)$$

where  $\dot{I}_{cv}$  is defined as the irreversibilities taking place within the control volume under consideration, on a rate form. Hence, the proposed efficiency, named ‘rational’ efficiency, is defined, for any system for which a useful output can be expressed in terms of exergy [21,22], as:

$$\varepsilon \equiv \frac{\sum \Delta \dot{E}_{out}}{\sum \Delta \dot{E}_{in}} \quad (19)$$

Using the nomenclature proposed by Tsatsaronis [53], the rational exergetic efficiency, or simply called the ‘*exergy efficiency*’ in the works of Moran [55,61], Lazzaretto [24,25] and Valero [64] can be written as:

$$\varepsilon \equiv \frac{\dot{E}_p}{\dot{E}_f} = 1 - \frac{\dot{E}_l + \dot{E}_d}{\dot{E}_f} \quad (20)$$

#### 4. Efficiencies for oil and gas platforms

Only the formulations of the exergetic efficiencies based on the fuel-product concept are discussed, as the input-output and intrinsic efficiencies are calculated in a systematic way, using the algorithms presented in *Section 3*. The expressions for the fuel-product exergetic efficiencies were derived from other works dealing with the study of processes and systems that present common characteristics with oil and gas platforms [27,29–32].

##### 4.1. Exergy balances

The exergy balance for the processing plant of the oil and gas facility (*Figure 3*) can be expressed as:

$$\dot{E}_{feed} + \dot{E}_{heat}^Q + \dot{E}_{UT}^W = \sum_k \dot{E}_k + \dot{E}_{cool}^Q + \dot{E}_{d,PP} \quad (21)$$

The left-hand side (LHS) term represents, on a time rate basis, the exergy associated with the feed entering the processing plant (i.e. reservoir fluid)  $\dot{E}_{feed}$  and the exergy transfers with the heating medium  $\dot{E}_{heat}^Q$  and power  $\dot{E}_{UT}^W$  from the utility plant that are consumed within the separation and treatment modules. The right-hand side (RHS) term denotes the exergy of the outlet streams of the processing plant (i.e. oil, gas, condensate, flared gas, fuel gas, produced water)  $\sum_k \dot{E}_k$  and the exergy gain discarded with the cooling medium discharged to the environment  $\dot{E}_{cool}^Q$ .  $\dot{E}_{d,PP}$  is the exergy destroyed in the processing plant.

The exergy balance for the utility plant of the oil and gas facility (*Figure 3*) can be expressed as:

$$\dot{E}_{air} + \dot{E}_{k,fg} = \dot{E}_{heat}^Q + \dot{E}_{UT}^W + \dot{E}_{exh} + \dot{E}_{d,UT} \quad (22)$$

The left-hand side (LHS) term represents, on a time rate basis, the exergy entering the utility plant that are associated with the air  $\dot{E}_{air}$  and fuel gas  $\dot{E}_{k,fg}$  from the separation plant. The right-hand side (RHS) term denotes the exergy accompanying the power  $\dot{E}_{UT}^W$  and heat  $\dot{E}_{heat}^Q$  produced in the utility plant and  $\dot{E}_{exh}$  the exergy rejected into the environment with the exhaust gases.  $\dot{E}_{d,UT}$  is the exergy destroyed in the utility plant.

Hence, for the overall plant, i.e. the combination of the processing and utility plants (Figure 3), the exergy balance becomes:

$$\begin{aligned}\dot{E}_{feed} + \dot{E}_{air} &= \left( \sum_k \dot{E}_k - \dot{E}_{k,fg} \right) + \dot{E}_{cool}^Q + \dot{E}_{exh} + \dot{E}_{d,op} \\ &= \left( \sum_{k'} \dot{E}_{k'} \right) + \dot{E}_{cool}^Q + \dot{E}_{exh} + \dot{E}_{d,op}\end{aligned}\quad (23)$$

where  $\dot{E}_{d,OP}$  is the sum of the exergy destruction taking place within both plants.

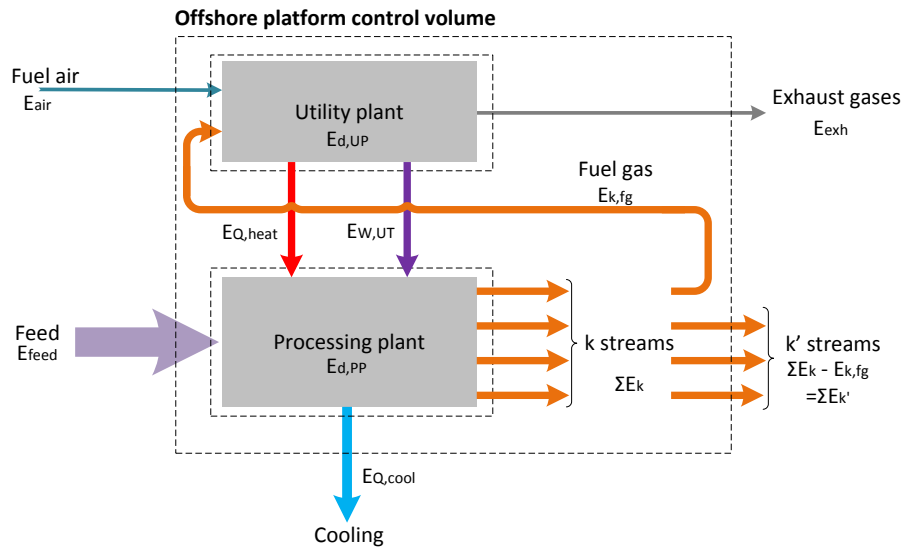


Figure 3: Control volume of oil and gas offshore facilities

#### 4.2. Exergetic efficiencies of the processing plant

The exergy balance for the processing plant solely can be rewritten as:

$$\underbrace{\dot{E}_{heat}^Q + \dot{E}_{UT}^W}_I = \underbrace{\left( \sum_k \dot{E}_k - \dot{E}_{feed} \right)}_{II} + \underbrace{\dot{E}_{d,PP}}_{III} + \underbrace{\dot{E}_{cool}^Q}_{IV}\quad (24)$$

The left-hand side term, *Term I* can be identified as the resources required to drive the processing plant, i.e. exergetic fuel, while, on the right-hand side, *Term II* can be identified as the exergetic product, *Term III* as the exergy destruction and *Term IV* as the exergy losses. The expression for the exergetic efficiency of this system is then given by:

$$\varepsilon_{PP} = \frac{\sum_k \dot{E}_k - \dot{E}_{feed}}{\dot{E}_{heat}^Q + \dot{E}_{UT}^W} = 1 - \frac{\dot{E}_{cool}^Q + \dot{E}_{d,PP}}{\dot{E}_{heat}^Q + \dot{E}_{UT}^W}\quad (25)$$

which is similar to the expression of the rational efficiency for a generalised separation plant, as proposed by Kotas [15] and used in Voldsund et al. [30,31].

Kotas [15] proposed in the same work an alternative to this expression, arguing that the exergy associated with the mixture may be high enough to perform the separation process. He proposed to differentiate the exergetic input of the mixture and the exergy output of the separated streams and to consider them as fuel and product, respectively. This approach is also used in the works of Cornelissen [27] and of Rian and Ertesvåg [32].

The flowing exergy associated to each stream of matter can be split into physical exergy and chemical exergies:

$$\dot{E}_{feed}^{ph} + \dot{E}_{feed}^{ch} + \dot{E}_{heat}^Q + \dot{E}_{UT}^W = \sum_k \dot{E}_k^{ph} + \sum_k \dot{E}_k^{ch} + \dot{E}_{cool}^Q + \dot{E}_{d,PP} \quad (26)$$

Hence, the exergetic balance can be rewritten as:

$$\begin{aligned} \underbrace{\dot{E}_{feed}^{ph} + \dot{E}_{heat}^Q + \dot{E}_{UT}^W}_I &= \sum_k \dot{E}_k^{ph} + \sum_k \dot{E}_k^{ch} - \dot{E}_{feed}^{ch} + \dot{E}_{cool}^Q + \dot{E}_{d,PP} \\ &= \underbrace{\sum_k \dot{E}_k^{ph} + \sum_k \Delta E_k^{ch}}_{II} + \underbrace{\dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,PP}}_{IV} \end{aligned} \quad (27)$$

The left-hand side of this equation (*Term I*) is now considered as the exergetic fuel, which is the sum of the exergy transfers by heat and power and the physical exergy of the feed. Similarly, the exergetic product is now taken as the difference of chemical exergies between the inlet and outlets of the processing plant as well as the physical exergy of the output streams (*Term II*). The expression for the exergetic efficiency of this system is then given by:

$$\varepsilon_{PP} = \frac{\sum_k \dot{E}_k^{ph} + \sum_k \Delta E_k^{ch}}{\dot{E}_{feed}^{ph} + \dot{E}_{heat}^Q + \dot{E}_{UT}^W} = 1 - \frac{\dot{E}_{cool}^Q + \dot{E}_{d,PP}}{\dot{E}_{feed}^{ph} + \dot{E}_{heat}^Q + \dot{E}_{UT}^W} \quad (28)$$

which is similar to the expression of the rational efficiency for a crude oil distillation plant and a natural gas liquefaction facility, as proposed respectively by Kotas [15] and by Rian and Ertesvåg [32].

Finally, following the methodology proposed by Lazaretto and Tsatsaronis [24,25], the fuel exergy is defined as the sum of the physical exergy decreases between the inflowing feed and the separated streams with a lower specific physical exergy ( $k^-$ ) and the exergy associated with heating and power (*Term I*). The product exergy is defined as the sum of the physical exergy increases between the inflowing feed and the separated products with a higher specific physical exergy ( $k^+$ ) and the chemical exergy increases between the feed and products (*Term II*). The exergy balance can therefore be expressed as:

$$\underbrace{\sum_{k^-} \dot{m}_{k^-} \cdot (e_{feed}^{ph} - e_{k^-}^{ph}) + \dot{E}_{heat}^Q + \dot{E}_{UT}^W}_I = \underbrace{\sum_{k^+} \dot{m}_{k^+} \cdot (e_{k^+}^{ph} - e_{feed}^{ph}) + \sum_k \Delta E_k^{ch}}_{II} + \underbrace{\dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,PP}}_{IV} \quad (29)$$

The expression for the exergetic efficiency of this system is then given by:

$$\varepsilon_{PP} = \frac{\sum_{k^+} \dot{m}_{k^+} \cdot (e_{k^+}^{ph} - e_{feed}^{ph}) + \sum_k \Delta E_k^{ch}}{\sum_{k^-} \dot{m}_{k^-} \cdot (e_{feed}^{ph} - e_{k^-}^{ph}) + \dot{E}_{heat}^Q + \dot{E}_{UT}^W} = 1 - \frac{\dot{E}_{cool}^Q + \dot{E}_{d,PP}}{\sum_{k^-} \dot{m}_{k^-} \cdot (e_{feed}^{ph} - e_{k^-}^{ph}) + \dot{E}_{heat}^Q + \dot{E}_{UT}^W} \quad (30)$$

which is similar to the expression of the exergetic efficiency for a generalised distillation column, as discussed by Tsatsaronis and Czielesla [17].

#### 4.3. Exergetic efficiency of the utility plant

The exergy balance for the utility plant solely can be rewritten as:

$$\underbrace{\dot{E}_{air} + \dot{E}_{k,fg}}_I = \underbrace{\dot{E}_{heat}^Q + \dot{E}_{UT}^W}_{II} + \underbrace{\dot{E}_{exh}}_{III} + \underbrace{\dot{E}_{d,UT}}_{IV} \quad (31)$$

The left-hand side (LHS) term (*Term I*) corresponds to the exergetic fuel of the utility system, i.e. the air and fuel gas from the processing plant that are combusted in the gas turbine system. The exergy transfers associated with power and heat (*Term II*), which are the desired outcomes of this plant, represent the exergetic product. The exergy content of the exhaust gases (*Term III*) denotes the exergy losses.

The exergetic efficiency of this combined heat and power plant can be written as:

$$\varepsilon_{UT} = \frac{\dot{E}_{heat}^Q + \dot{E}_{UT}^W}{\dot{E}_{air} + \dot{E}_{k,fg}} = 1 - \frac{\dot{E}_{exh} + \dot{E}_{d,UT}}{\dot{E}_{air} + \dot{E}_{k,fg}} \quad (32)$$

#### 4.4. Exergetic efficiencies for the complete plant

‘Fuel-product’ exergy efficiencies require particular attention on the definition of the *purpose* of the system. The objective of an oil and gas platform can be seen as to separate the inflowing feed into its oil, gas and water fractions and to deliver them at a given temperature and pressure level. In this regard, a fraction of the feed is consumed onsite to perform the separation work and to reach the desired specifications. In the following, the LHS *Term I* always refers to the fuel exergy and the RHS *Term II*, *Term III* and *Term IV* to the product, losses and destroyed exergies, on a time rate basis.

##### 4.4.1. Case 1 – all streams of matter exiting the processing plant are useful

The approaches presented in Refs. [15,24,25,27,29–32] can be extended from the oil and gas processing plant to the overall plant. The exergy balance can therefore be reformulated as:

- following the works of Kotas [15] and of Oliveira and Van Hombeeck [29], the consumed exergy consists of the exergies of the components present in the feed that are processed as fuel gas as well as the air processed in the gas turbines;

$$\underbrace{\sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}}_I = \sum_{k'} \sum_i \dot{n}_{i,k'} (\bar{e}_{i,k'} - \bar{e}_{i,feed}) + \dot{E}_{exh} + \dot{E}_{cool}^Q + \dot{E}_{d,OP} \quad (33)$$

$$= \underbrace{\sum_{k'} \Delta \dot{E}_{k'}}_{II} + \underbrace{\dot{E}_{exh} + \dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,OP}}_{IV}$$

The exact formulation proposed by Oliveira and Van Hombeeck [29] is slightly different, as they defined the consumed exergy as the chemical exergy of the fuel gas, and not as the flow exergy associated with the fraction of the feed that is processed to the power generation system. This results in minor numerical differences, as the physical exergy of the fuel gas and the difference of the exergy penalties due to the mixing effect are negligible in comparison to the chemical exergy of the pure components.

- considering the same work of Kotas [15] as well as the studies of Cornelissen [27] and Rian and Ertesvåg [32], the consumed exergy consists of the fuel gas exergy to the utility plant, the air processed in the gas turbines and the physical exergy of the feed;

$$\underbrace{\dot{E}_{feed}^{ph} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed}^{ch} + \dot{E}_{air}}_I = \underbrace{\sum_{k'} (\dot{E}_{k'}^{ph} + \Delta \dot{E}_{k'}^{ch})}_{II} + \underbrace{\dot{E}_{exh} + \dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,OP}}_{IV} \quad (34)$$

- finally, applying the fuel-product definitions described in Lazzaretto and Tsatsaronis [24,25], the fuel exergy consists of the chemical exergy of the fraction of the feed that goes to the utility plant, the air processed in the gas turbines and the decreases of physical exergy between the inlet and outlet of the system:

$$\underbrace{\sum_{k^-} \dot{m}_{k^-} \cdot (e_{feed}^{ph} - e_{k^-}^{ph}) + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}}_I = \underbrace{\sum_{k^+} \dot{m}_{k^+} \cdot (e_{k^+}^{ph} - e_{feed}^{ph}) + \sum_{k'} \Delta \dot{E}_{k'}^{ch}}_{II} + \underbrace{\dot{E}_{exh} + \dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,OP}}_{IV} \quad (35)$$

Eq. (35) reduces to Eq.(33) when all the streams exiting the oil and gas platform have a higher specific physical exergy than at the inlet.

#### 4.4.2. Case 2 – certain streams of matter exiting the processing plant are wasted

For oil and gas systems where material streams exiting the processing plant are discharged into the environment without any practical use (e.g. produced water, flared and vented gases), the exergy losses are identified as the sum of the exergy discharged to the sea via cooling, the exergy contents of the exhaust gases *and* of the waste streams of the processing plant. Hence, the exergy balance of the overall plant can be rewritten as:

$$\dot{E}_{feed} + \dot{E}_{air} = \left( \sum_{ku} \dot{E}_{ku} + \sum_{kw} \dot{E}_{kw} \right) + \dot{E}_{cool}^Q + \dot{E}_{exh} + \dot{E}_{d,OP} \quad (36)$$

where the indice *ku* indicates the streams resulting from the feed separation that are considered as useful (e.g. export, injection, lift) by opposition to the streams *kw* that are rejected to the environment and wasted. Accordingly, the physical and chemical exergies associated with these streams are accounted as losses, and the exergy balance becomes, following the reasoning of Kotas [15], Oliveira and Van Hombeeck [29]:

$$\underbrace{\dot{E}_{air} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \sum_{kw} \sum_i \dot{n}_{i,kw} (\bar{e}_{i,feed})}_{I'} = \underbrace{\sum_{ku} (\Delta \dot{E}_{ku})}_{II} + \underbrace{\sum_{kw} \dot{E}_{kw} + \dot{E}_{cool}^Q + \dot{E}_{exh}}_{III} + \underbrace{\dot{E}_{d,OP}}_{IV} \quad (37)$$

*Term I'* is the exergy rate, both physical and chemical, of the components *in the feed* that enter the platform and are discharged into the environment as waste. They correspond to the additional resources required within the system to provide the desired products and that are paid to compensate for the external losses. The overall *Term I* represents *all* the resources expended to generate the desired product, i.e. the fuel exergy. *Term II* corresponds to the desired product, i.e. the exergy increases between inlet and outlet for the outputs that are utilisable. *Term III* denotes the exergy losses of the offshore platform system, i.e. the exergy associated with the waste streams (e.g. produced water, flared and vented gas) and *Term IV* the internal irreversibilities of the platform.

Seemingly, following the reasonings of Kotas [15], Cornelissen [27] and Rian and Ertesvåg [32]:

$$\begin{aligned} & \underbrace{\dot{E}_{feed}^{ph} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed}^{ch} + \dot{E}_{air} + \sum_{kw} \sum_i \dot{n}_{i,kw} (\bar{e}_{i,feed}^{ch})}_{I'} \\ & \quad \underbrace{\hspace{10em}}_I \\ & = \underbrace{\sum_{ku} (\dot{E}_{ku}^{ph} + \Delta \dot{E}_{ku}^{ch})}_{II} + \underbrace{\sum_{kw} \dot{E}_{kw} + \dot{E}_{exh} + \dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,OP}}_{IV} \end{aligned} \quad (38)$$

And, following the reasoning of Lazzaretto and Tsatsaronis [24,25]:

$$\begin{aligned}
& \underbrace{\sum_{ku^-} \dot{m}_{ku^-} \cdot (e_{feed}^{ph} - e_{ku^-}^{ph}) + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}}_{I'} + \underbrace{\sum_{kw} \sum_i \dot{n}_{i,kw} (\bar{e}_{i,feed})}_{I''} \\
& \quad \underbrace{\hspace{10em}}_I \\
& = \underbrace{\sum_{ku^+} \dot{m}_{ku^+} \cdot (e_{ku^+}^{ph} - e_{feed}^{ph})}_{II} + \underbrace{\sum_{ku'} \Delta \dot{E}_{ku'}^{ch}}_{III} + \underbrace{\sum_{kw} \dot{E}_{kw} + \dot{E}_{exh} + \dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,OP}}_{IV}
\end{aligned} \tag{39}$$

The main differences between Eqs.(33–35) and Eqs.(37–39) lie in the accountings of (i) the exergetic fuel, which contains a term related to the extra resources paid by the owner of the system to generate the desired exergetic product, (ii) the exergetic product, which comprises only the useful exergetic effects associated with the streams not discharged as waste and (iii) the exergetic losses, which increase due to the non-use of some of the effluent streams exiting the processing plant.

#### 4.4.3. Auxiliary formulations

The exergy balances and interpretations of fuel and product presented in Eqs.(38–39) can be improved by expressing the physical and chemical exergy terms as functions of their thermal, mechanical, reactive and nonreactive components. Such decompositions may improve the accuracy of the exergy efficiency definitions although they require larger computational calculations [24,25]. However, it is also argued that a separation of the several exergy components may be necessary to obtain consistent results.

- based on the studies of Kotas [15] and Cornelissen [27] the product exergy (*Term II*) can be considered to be the pressure-based exergy only, and the temperature-based exergy is assumed as an exergy loss (*Term III*) of the oil and gas system.

$$\begin{aligned}
& \underbrace{\dot{E}_{feed}^{ph} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed}^{ch} + \dot{E}_{air}}_{I'} + \underbrace{\sum_{kw} \sum_i \dot{n}_{i,kw} (\bar{e}_{i,feed}^{ch})}_{I''} \\
& \quad \underbrace{\hspace{10em}}_I \\
& = \underbrace{\sum_{ku} (\dot{E}_{ku}^m + \Delta \dot{E}_{ku}^N)}_{II} + \underbrace{\sum_{ku} (\dot{E}_{ku}^t)}_{III} + \underbrace{\sum_{kw} \dot{E}_{kw} + \dot{E}_{exh} + \dot{E}_{cool}^Q}_{III} + \underbrace{\dot{E}_{d,OP}}_{IV}
\end{aligned} \tag{40}$$

- based on the considerations on fuel and product exergies, as presented in Lazzaretto and Tsatsaronis [24,25], the fuel exergy *Term I* consists of the chemical exergy of the fraction of the feed that goes to the utility plant, the air processed in the gas turbines and the decreases of thermal and mechanical exergy between the inlet and outlet of the system. The product exergy (*Term II*) consists of the increases of chemical and mechanical exergies. Conversely, the increases of the thermal exergies are included in the exergy losses (*Term III*), as they are not useful to the owner of the system and are dissipated via heat losses in further oil and gas processing.

$$\begin{aligned}
& \underbrace{\sum_{ku^{m-}} \dot{m}_{ku^{m-}} \cdot (e_{feed}^m - e_{ku^{m-}}^m) + \sum_{ku^{t-}} \dot{m}_{ku^{t-}} \cdot (e_{feed}^t - e_{ku^{t-}}^t) + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}}_{I'} \\
& + \underbrace{\sum_{kw} \sum_i \dot{n}_{i,kw} (\bar{e}_{i,feed})}_{I''} \\
& = \underbrace{\sum_{ku'} \Delta \dot{E}_{ku'}^{ch} + \sum_{ku^{m+}} \dot{m}_{ku^{m+}} \cdot (e_{ku^{m+}}^m - e_{feed}^m)}_{II} + \underbrace{\sum_{ku^{t+}} \dot{m}_{ku^{t+}} \cdot (e_{ku^{t+}}^t - e_{feed}^t) + \sum_{kw} \dot{E}_{kw} + \dot{E}_{exh} + \dot{E}_{cool}^Q}_{III} \\
& + \underbrace{\dot{E}_{d,OP}}_{IV}
\end{aligned} \tag{41}$$

where the subscripts  $ku^{m+}$ ,  $ku^{t+}$ ,  $ku^{m-}$ ,  $ku^{t-}$  refer to the useful streams exiting the oil and gas platform with, respectively, a greater mechanical, greater thermal, smaller mechanical and a smaller thermal specific exergy.

For oil and gas systems receiving or delivering exergy that is transferred with power, e.g. interconnected platforms, the associated exergy rates are added to the fuel term if power is received and to the product term if delivered. Similarly, if gas and injection seawater are imported or exported to another oil and gas facility, as it is the case of several platforms located in the North Sea region, the corresponding exergy flows are considered either in the required resources to expend by the owner or in the desired products.

#### 4.4.4. Summary of the definitions

The exergy-based efficiencies of the total plant can therefore be grouped as the input-output and the consumed-produced efficiencies (Table 2).  $\varepsilon_{I,1}$  and  $\varepsilon_{I,2}$  denote the input-output exergy efficiencies, as discussed in the works of Nesselmann [4,8], Baehr [10], and Fratzscher [6].  $\varepsilon_{II,1}$  and  $\varepsilon_{II,2}$  denote the consumed-produced exergy efficiencies that are based on the concept of transit exergy and proposed by Brodyansky [11] and Sorin [19].  $\varepsilon_{II,3}$ ,  $\varepsilon_{II,4}$  and  $\varepsilon_{II,5}$  denote the consumed-produced exergy efficiencies that are based on the concept of fuel-product, with the application of possible interpretations that were also found in the literature [15,24,25,27,29–32].  $\varepsilon_{II,6}$  and  $\varepsilon_{II,7}$  are extensions of  $\varepsilon_{II,4}$  and  $\varepsilon_{II,5}$ , decomposing the physical and chemical exergies into their components.

## 5. Comparison of oil and gas platforms

## 6. Discussion

This expression is unambiguous but may be misleading, as it can be relatively insensitive to changes taking place within the system. For instance, when only a small fraction of the inflowing exergy is transformed, the exergy destruction taking place within the system is small in comparison to the total input exergy flows. Calculations of the input-output exergetic efficiency will return a high value, giving the impression of a high thermodynamic performance.

However, mathematically, this efficiency expression may have a negative value if the term  $\sum_k \dot{E}_k - \dot{E}_{feed}$  is below 0, which is the case only when the exergy of the separated products is lower than the exergy of the feed.

## 7. Conclusion

## Acknowledgements

## References

- [1] Svalheim SM. Environmental Regulations and Measures on the Norwegian Continental Shelf. In: Proceedings of the SPE International Conference on Health, Safety and Environment in Oil and Gas Exploration and Production. Kuala Lumpur, Malaysia: Society of Petroleum Engineers; 2002, p. 1–10 (Paper SPE 73982).
- [2] Svalheim SM, King DC. Life of Field Energy Performance. In: Proceedings of the SPE Offshore Europe Conference. July; Aberdeen, United Kingdom: Society of Petroleum Engineers; 2003, p. 1–10 (Paper SPE 83993).



Table 2: Exergy-based efficiencies for oil and gas platforms

	Input-Fuel	Output-Product	Efficiency
$\varepsilon_{I,1}$	$\dot{E}_{feed} + \dot{E}_{air}$	$\sum_{k'} \dot{E}_{k'} + \dot{E}_{exh} + \dot{E}_{CW}^Q$	$\frac{\sum_{k'} \dot{E}_{k'} + \dot{E}_{exh} + \dot{E}_{CW}^Q}{\dot{E}_{feed} + \dot{E}_{air}}$
$\varepsilon_{I,2}$	$\dot{E}_{feed} + \dot{E}_{air}$	$\sum_{k'} \dot{E}_{k'}$	$\frac{\sum_{k'} \dot{E}_{k'}}{\dot{E}_{feed} + \dot{E}_{air}}$
$\varepsilon_{II,1}$	$\dot{E}_{feed} + \dot{E}_{air} - \dot{E}_{tr}$	$\sum_{k'} \dot{E}_{k'} + \dot{E}_{exh} + \dot{E}_{CW}^Q - \dot{E}_{tr}$	$\frac{\sum_{k'} \dot{E}_{k'} - \dot{E}_{tr}}{\dot{E}_{feed} + \dot{E}_{air} - \dot{E}_{tr}}$
$\varepsilon_{II,2}$	$\dot{E}_{feed} + \dot{E}_{air} - \sum \dot{E}_{tr,u}$	$\sum_{k'} \dot{E}_{k'} - \sum \dot{E}_{tr,u}$	$\frac{\sum_{k'} \dot{E}_{k'} - \sum \dot{E}_{tr,u}}{\dot{E}_{feed} + \dot{E}_{air} - \sum \dot{E}_{tr,u}}$
$\varepsilon_{II,3}$	$\sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}$	$\sum_{k'} \Delta \dot{E}_{k'}$	$\frac{\sum_{k'} \Delta \dot{E}_{k'}}{\sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}}$
$\varepsilon_{II,4}$	$\dot{E}_{feed}^{ph} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed}^{ch} + \dot{E}_{air}$	$\sum_{k'} (\dot{E}_{k'}^{ph} + \Delta \dot{E}_{k'}^{ch})$	$\frac{\sum_{k'} (\dot{E}_{k'}^{ph} + \Delta \dot{E}_{k'}^{ch})}{\dot{E}_{feed}^{ph} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed}^{ch} + \dot{E}_{air}}$
$\varepsilon_{II,5}$	$\sum_{k-} \dot{m}_{k-} \cdot (e_{feed}^{ph} - e_{k-}^{ph})$ + $\sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}$	$\sum_{k+} \dot{m}_{k+} \cdot (e_{k+}^{ph} - e_{feed}^{ph})$ + $\sum_{k'} \Delta \dot{E}_{k'}^{ch}$	$\frac{\sum_{k+} \dot{m}_{k+} \cdot (e_{k+}^{ph} - e_{feed}^{ph}) + \sum_{k'} \Delta \dot{E}_{k'}^{ch}}{\sum_{k-} \dot{m}_{k-} \cdot (e_{feed}^{ph} - e_{k-}^{ph}) + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}}$
$\varepsilon_{II,6}$	$\dot{E}_{feed}^{ph} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed}^{ch} + \dot{E}_{air}$	$\sum_{k'} (\dot{E}_{k'}^m + \Delta \dot{E}_{k'}^{ch})$	$\frac{\sum_{k'} (\dot{E}_{k'}^m + \Delta \dot{E}_{k'}^{ch})}{\dot{E}_{feed}^{ph} + \sum_i \dot{n}_{i,fg} \bar{e}_{i,feed}^{ch} + \dot{E}_{air}}$
$\varepsilon_{II,7}$	$\sum_{k'm-} \dot{m}_{k'm-} \cdot (e_{feed}^m - e_{k'm-}^m)$ + $\sum_{k't-} \dot{m}_{k't-} \cdot (e_{feed}^t - e_{k't-}^t)$ + $\sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}$	$\sum_{k'm+} \dot{m}_{k'm+} \cdot (e_{k'm+}^m - e_{feed}^m)$ + $\sum_{k'} \Delta \dot{E}_{k'}^{ch}$	$\frac{\sum_{k'm+} \dot{m}_{k'm+} \cdot (e_{k'm+}^m - e_{feed}^m) + \sum_{k'} \Delta \dot{E}_{k'}^{ch} + \dots}{\sum_{k'm-} \dot{m}_{k'm-} \cdot (e_{feed}^m - e_{k'm-}^m) + \sum_{k't-} \dot{m}_{k't-} \cdot (e_{feed}^t - e_{k't-}^t) + \dots}$ $\frac{\sum_{k't-} \dot{m}_{k't-} \cdot (e_{k't-}^t - e_{feed}^t)}{\sum_i \dot{n}_{i,fg} \bar{e}_{i,feed} + \dot{E}_{air}}$

Table 3: Results of exergy-based efficiencies for oil and gas platforms

	Platform A	Platform B	Platform C	Platform D
$\varepsilon_{I,1}$				
$\varepsilon_{I,2}$				
$\varepsilon_{II,1}$				
$\varepsilon_{II,2}$				
$\varepsilon_{II,3}$				
$\varepsilon_{II,4}$				
$\varepsilon_{II,5}$				

- [3] Rivero R. Application of the exergy concept in the petroleum refining and petrochemical industry. *Energy Conversion and Management* 2002;43(9-12):1199–220.
- [4] Nesselmann K. Über den thermodynamischen Begriff der Arbeitsfähigkeit. *Allgemeine Wärmetechnik* 1952;3(5–6):97–104.
- [5] Fratzscher W, Beyer J. Stand und Tendenzen bei der Anwendung und Weiterentwicklung des Exergiebegriffs. *Chemische Technik* 1981;33(1):1–10.
- [6] Fratzscher W, Brodjanskij VM, Michalek K. *Exergie: Theorie und Anwendung*. Leipzig, Germany: Deutscher Verlag für Grundstoffindustrie; 1986.
- [7] Grassmann VP. Zur allgemeinen Definition des Wirkungsgrades. *Chemie Ingenieur Technik* 1950;4(1):77–80.
- [8] Nesselmann K. Der Wirkungsgrad thermodynamischer Prozesse und sein Zusammenhang mit der Umgebungtemperatur. *Allgemeine Wärmetechnik* 1953;4(7):141–7.
- [9] Baehr HD. *Energie und Exergie – Die Anwendung des Exergiebegriffs in der Energietechnik*. Düsseldorf, Germany: VDI-Verlag; 1965.
- [10] Baehr HD. Zur Definition exergetischer Wirkungsgrade – Eine systematische Untersuchung. *Brennstoff-Wärme-Kraft* 1968;20(5):197–200.
- [11] Brodyansky VM, Sorin MV, Le Goff P. *The Efficiency of Industrial Processes: Exergy Analysis and Optimization*. Amsterdam, The Netherlands: Elsevier; 1994.
- [12] Szargut J, Morris D, Steward F. *Exergy analysis of thermal, chemical, and metallurgical processes*. New York, USA: Hemisphere; 1988.
- [13] Morris D, Steward F, J. S. Technological assessment of chemical metallurgical processes. *Canadian Metallurgical Quarterly* 1994;33(4):289–95.
- [14] Szargut J. Exergy in the thermal systems analysis. In: Bejan A, Mamut E, editors. *Proceedings of the NATO Advanced Study Institute on Thermodynamic Optimization of Complex Energy Systems*; vol. 69 of *NATO Science Series*. Neptun, Romania: Kluwer Academic Publishers; 1998, p. 137–50.
- [15] Kotas TJ. *The Exergy Method of Thermal Plant Analysis*. Malabar, USA: Krieger Publishing; 1995.
- [16] Tsatsaronis G. Thermo-economic analysis and optimization of energy systems. *Progress in Energy and Combustion Science* 1993;19:227–57.
- [17] Tsatsaronis G, Czesla F. *Encyclopedia of Physical Science and Technology*; vol. 16; chap. Thermo-economics. 3rd ed.; Academic Press; 2002, p. 659–80.
- [18] Kostenko G. Efficiency of Heat Processes (in Russian). *Promishlenaya Teplotekhnika* 1983;4:70–3.
- [19] Sorin MV, Brodyansky VM, Paris J. Observations on exergy efficiency coefficients. In: Carnevale E, Manfrida G, Martelli F, editors. *Proceedings of the Florence World Energy Research Symposium*; vol. 94. Padova, Italy: SG Editoriali; 1994, p. 941–9.
- [20] Kotas TJ. Exergy concepts for thermal plant: First of two papers on exergy techniques in thermal plant analysis. *International Journal of Heat and Fluid Flow* 1980;2(3):105–14.
- [21] Kotas TJ. Exergy Criteria of Performance for Thermal Plant: Second of two papers on exergy techniques in thermal plant analysis. *International Journal of Heat and Fluid Flow* 1980;2(4):147–63.
- [22] Bejan A, Tsatsaronis G, Moran M. *Thermal Design & Optimization*. New York, USA: John Wiley & Sons; 1996.
- [23] Moran MJ. Fundamentals of exergy analysis and exergy-based thermal systems design. In: Bejan A, Mamut E, editors. *Proceedings of the NATO Advanced Study Institute on Thermodynamic Optimization of Complex Energy Systems*; vol. 69 of *NATO Science Series*. Neptun, Romania: Kluwer Academic Publishers; 1998, p. 73–92.
- [24] Lazzaretto A, Tsatsaronis G. On the calculation of efficiencies and costs in thermal systems. In: Aceves SM, Garimella S, Peterson RB, editors. *Proceedings of the ASME Advanced Energy Systems Division*; vol. 39. New York, USA; 1999, p. 421–30.
- [25] Lazzaretto A, Tsatsaronis G. SPECO: A systematic and general methodology for calculating efficiencies and costs in thermal systems. *Energy* 2006;31:1257–89.
- [26] Sorin MV, Paris J, Brodjanskij VM. Thermodynamic evaluation of a distillation. In: *Thermodynamics and the Design, Analysis, and Improvement of Energy Systems*; vol. 33. New York, USA: ASME; 1994, p. 125–34.
- [27] Cornelissen R. *Thermodynamics and sustainable development – The use of exergy analysis and the reduction of irreversibility*. Ph.D. thesis; Universiteit Twente; Enschede, The Netherlands; 1997.
- [28] Lior N, Zhang N. Energy, exergy, and Second Law performance criteria. *Energy* 2007;32(4):281–96.
- [29] Oliveira Jr. SD, Van Hombeeck M. Exergy Analysis of Petroleum Separation Processes in Offshore Platforms. *Energy Conversion and Management* 1997;38(15-17):1577–84.
- [30] Voldsund M, Ertesvåg IS, Røsjorde A, He W, Kjelstrup S. Exergy Analysis of the Oil and Gas Separation Processes on a North Sea Oil Platform. In: Favrat D, Maréchal F, editors. *Proceedings of ECOS 2010 - The 23rd International Conference on Efficiency, Cost, Optimization, Simulation and Environmental Impact of Energy Systems*; vol. IV Power plants & Industrial Processes. Lausanne, Switzerland: CreateSpace Independent Publishing Platform; 2010, p. 303–10.
- [31] Voldsund M, He W, Røsjorde A, Ertesvåg IS, Kjelstrup S. Evaluation of the Oil and Gas Processing at a Real Production day on a North Sea Oil Platform Using Exergy Analysis. In: Desideri U, Manfrida G, Sciubba E, editors. *Proceedings of ECOS 2012 - The 25th International Conference on Efficiency, Cost, Optimization, Simulation and Environmental Impact of Energy Systems*; vol. II. Perugia, Italy: Firenze University Press; 2012, p. 153–66.
- [32] Rian AB, Ertesvåg IS. Exergy Evaluation of the Arctic Snøhvit Liquefied Natural Gas Processing Plant in Northern Norway – Significance of Ambient Temperature. *Energy & Fuels* 2012;26:1259–67.
- [33] Bothamley M. Offshore Processing Options for Oil Platforms. In: *Proceedings of the SPE Annual Technical Conference and Exhibition*. Houston, USA: Society of Petroleum Engineers; 2004, p. 1–17 (Paper SPE 90325).
- [34] Danish Energy Agency. Danmarks olie og gas produktion. Tech. Rep.; Energistyrelsen; København, Denmark; 2011.
- [35] Norwegian Ministry of Petroleum and Energy. Facts 2012 – The Norwegian Petroleum Sector. Tech. Rep.; Norwegian Petroleum Directorate; Oslo, Norway; 2012.
- [36] Jones DSJS, Pujadó PR, editors. *Handbook of Petroleum Processing*. Dordrecht, The Netherlands: Springer; 2006.
- [37] Manning FS, Thompson RE. *Oilfield processing of petroleum: Natural Gas*; vol. 1. Tulsa, USA: PennWell Books; 1991.
- [38] Plisga WCL, J. G, editors. *Standard Handbook of Petroleum & Natural Gas Engineering*. Second ed.; Burlington, USA: Gulf Professional Publishing; 2004.

- [39] Abdel-Aal HK, Aggour M, Fahim MA. Petroleum and Gas Field Processing. Chemical Industries; New York, USA: Marcel Dekker; 2003.
- [40] Vik EA, Dinning AJ. Produced Water Re-Injection - The Potential to Become an Improved Oil Recovery Method. Tech. Rep.; Aquatem A/S; Oslo, Norway; 2009.
- [41] Manning FS, Thompson RE. Oilfield processing of petroleum: Crude oil; vol. 2. Tulsa, USA: PennWell Books; 1991.
- [42] Nguyen TV, Pierobon L, Elmegaard B, Haglind F, Breuhaus P, Voldsund M. Exergetic assessment of energy systems on North Sea oil and gas platforms; 2013. doi:<http://dx.doi.org.globalproxy.cvt.dk/10.1016/j.energy.2013.03.011>; Energy (in press).
- [43] Voldsund M, Ertesvåg IS, He W, Kjelstrup S. Exergy Analysis of the Oil and Gas Processing a Real Production Day on a North Sea Oil Platform; 2013. doi:<http://dx.doi.org.globalproxy.cvt.dk/10.1016/j.energy.2013.02.038>; Energy (in press).
- [44] Voldsund M, Nguyen TV, Elmegaard B, Ertesvåg I, Røsjorde A, Jøssang K, et al. Comparative study of the sources of exergy destruction on four North Sea oil and gas platforms. In: Proceedings of ECOS 2013 - The 26th International Conference on Efficiency, Cost, Optimization, Simulation and Environmental Impact of Energy Systems. 2013,.
- [45] Aspen Technology . Aspen Hysys 2004.2 ®– User Guide. Cambridge, USA: Aspen Technology; 2004.
- [46] Aspen Technology . Aspen Plus – Modelling Petroleum Processes. Burlington, USA: Aspen Technology; 1999.
- [47] Peng DY, Robinson DB. A New Two-Constant Equation of State. Industrial & Engineering Chemistry Fundamentals 1976;15(1):59–64.
- [48] Renon H, Prausnitz JM. Local compositions in thermodynamic excess functions for liquid mixtures. AIChE Journal 1968;14(1):135–44.
- [49] Schwartzentruber J, Renon H. Extension of UNIFAC to High Pressures and Temperatures by the Use of a Cubic Equation of State. Industrial & Engineering Chemistry Research 1989;28(7):1049–55.
- [50] Schwartzentruber J, Renon H, Watanasiri S. Development of a new cubic equation of state for phase equilibrium calculations. Fluid Phase Equilibria 1989;52:127–34.
- [51] Elmegaard B, Houbak N. DNA – A General Energy System Simulation Tool. In: Amundsen J, editor. Proceedings of SIMS 2005 - 46th Conference on Simulation and Modeling. Trondheim, Norway: Tapir Academic Press; 2005, p. 43–52.
- [52] Bejan A. Advanced Engineering Thermodynamics. Third ed.; New York, USA: John Wiley & Sons; 2006.
- [53] Tsatsaronis G. Definitions and nomenclature in exergy analysis and exergoeconomics. Energy 2007;32(4):249–53.
- [54] Tsatsaronis G, Winhold M. Exergoeconomic analysis and evaluation of energy-conversion plants – I. A new general methodology. Energy 1985;10(1):69–80.
- [55] Moran MJ, Shapiro HN. Fundamentals of Engineering Thermodynamics. 6th ed.; New York, USA: John Wiley & Sons; 2007.
- [56] Szargut J. Chemical exergies of the elements. Applied Energy 1989;32(4):269–86.
- [57] Morris DR, Szargut J. Standard chemical exergy of some elements and compounds on the planet earth. Energy 1986;11(8):733–55.
- [58] Sato N. Chemical Energy and Exergy: An Introduction to Chemical Thermodynamics for Engineers. 1st ed.; Amsterdam, The Netherlands: Elsevier; 2004.
- [59] Rivero R, Rendon C, Monroy L. The Exergy of Crude Oil Mixtures and Petroleum Fractions: Calculation and Application. International Journal of Applied Thermodynamics 1999;2(3):115–23.
- [60] Wall G. Encyclopedia of Energy; vol. 2; chap. Exergy. Academic Press; 2004, p. 593–606.
- [61] Moran MJ. Availability analysis: a guide to efficient energy use. 2nd ed.; New York, USA: ASME Press; 1989.
- [62] Sorin MV, Lambert J, Paris J. Exergy flows analysis in chemical reactors. IChemE 1998;76(A):389–95.
- [63] Szargut J. International progress in second law analysis. Energy 1980;5(8-9):709–18.
- [64] Valero A, Alconchel JA. Toward a Universal Formula of Efficiency. In: Moran MJ, Sciubba E, editors. Second Law Analysis of Thermal Systems, Proceedings of ASME Annual Winter Meeting. New York, USA; 1987, p. 193–7.

Table .4: Process details for the four studied platforms (HP = high pressure, LP = low pressure)

Stream number (type)	Platform A		Platform B		Platform C		Platform D	
	p (bar)	T (°C)	p (bar)	T (°C)	p (bar)	T (°C)	p (bar)	T (°C)
1 (reservoir fluid)	80–170	79–87			12–131	34–73	15–187	
2 (reservoir fluid)	70	74	135	110	44.5 (HP) 7.3 (LP)	65 (HP) 69 (LP)	8	
3 (oil–pumping)	2.8	55	2.4	56	2.7	98	1.7	
4 (oil–export)	32	50	103	59	168	81	50	
5 (treated gas)	236	78	127	35	187	73	179	
6 (condensate)	–		103		–		179	
7 (produced water)								
8 (discharged water)								
9 (seawater)	1.0		1.0		1.0		1.0	
10 (injection water)							127–147	