

MICHIGAN STATE UNIVERSITY MATH 234 – FALL 2023

SOME PROBLEMS 2023-08-31

- 1. Find the unit vectors that are parallel to the tangent line of $f(x) = x^2 2x + 3$ through the point (2,3).
- 2. Find the orthogonal projection of v = (1, 2, 3) onto **k**. Explain why your answer makes sense.
- 3. (Extra 12.3.31 in the textbook) Find the acute angles between the curves at their points of intersection (The angles between two curves is the angle between their tangent lines at the point of intersection).

$$y = x^2$$
, and $y = x^3$.

4. (Extra - 12.3.53 in the textbook) Use a scalar projection to show that the distance from a point $P_1(x_1, y_1)$ to the line ax + by + c = 0 is

$$\frac{|ax_1+by_1+c|}{\sqrt{a^2+b^2}}.$$

Use this formula to find the distance from the point (-2,3) to the line 3x - 4y + 5 = 0.

5. (Extra - 12.3.32 in the textbook) Find the acute angles between the curves at their points of intersection (The angles between two curves is the angle between their tangent lines at the point of intersection).

$$y = \sin x$$
, and $y = \cos x$, $0 \le x \le \frac{\pi}{2}$.