Watts' Network Cascades Model A Simple Model of Global Cascades on Random Networks

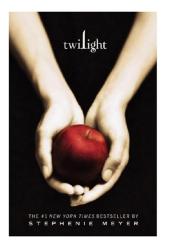
Marco Brack Carsten Hartenfels

2016-08-05

Content

- Motivation
- Simulation
- Explanation
- ► Watts' Model
- Findings
- Limitations

Motivation - Culture



Twilight

Source: https://en.wikipedia.org/wiki/File:Twilightbook.jpg

Motivation - Technology Adoption



WhatsApp

Source: https://commons.wikimedia.org/wiki/File:WhatsApp.svg

Motivation - Social Dynamics



Political Coups

Source: http://tinyurl.com/jmv529r

Network Cascades

Network Cascades

(Maybe)

Network Cascades

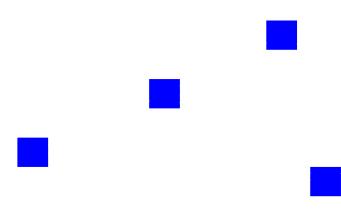
(Maybe)

(It's a Nice Model Anyway)

Simulation

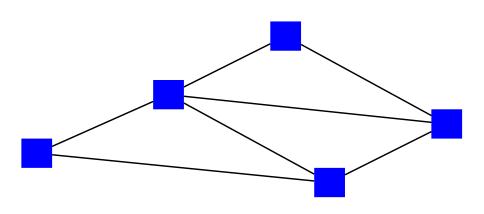
https://github.com/turbopope/nss/tree/master/simulator

Nodes

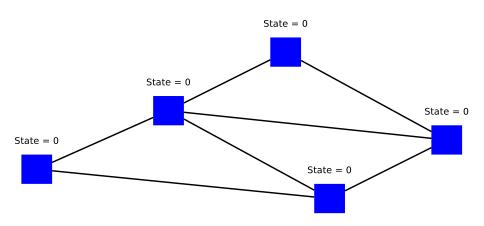




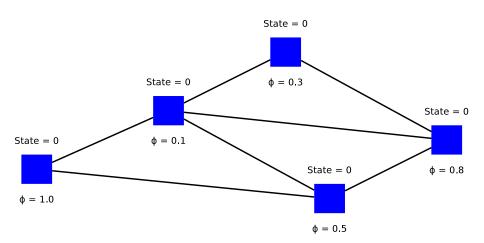
► Observe *k* Neighbors



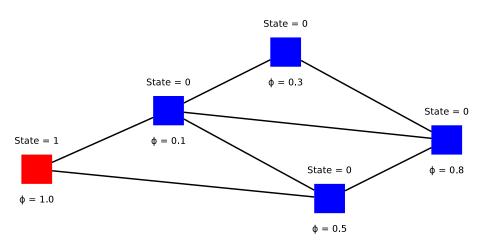
▶ State $\in \{0,1\}$



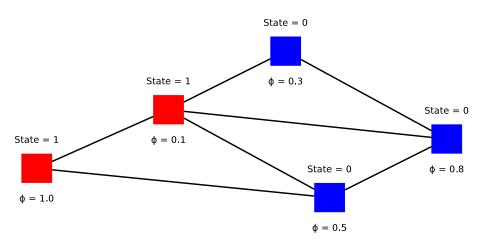
▶ Threshold $\Phi \in [0, 1]$



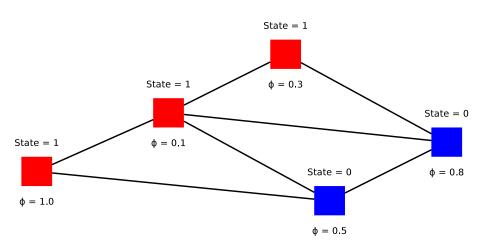
Random Impulse Happens



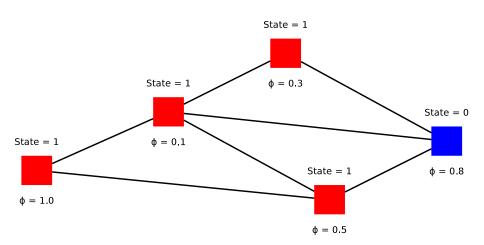
Nodes Check in Random Intervals



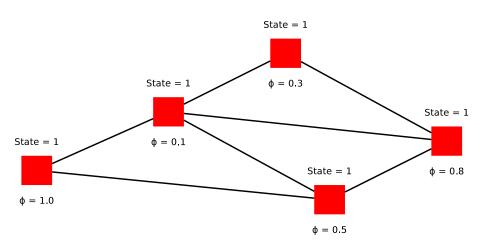
Stuff Happens



► Things Occur



Coup Successful



Watts' Model

► Each Person/Agent is a Node in a Graph

▶ Agents Have a State $\in \{0,1\}$

Agents Observe Their Neighbors

▶ Agents Change to a State 1 if Neighbor Threshold is Reached

▶ *n* Nodes

▶ n Nodes

 $ightharpoonup p_k$ Probability of n to Have k Neighbors

▶ n Nodes

 \triangleright p_k Probability of n to Have k Neighbors

 $ightharpoonup z = \langle k \rangle$ Expectation Value or Average Degree

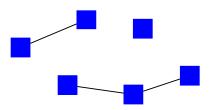
n Nodes

 \triangleright p_k Probability of n to Have k Neighbors

 $ightharpoonup z = \langle k \rangle$ Expectation Value or Average Degree

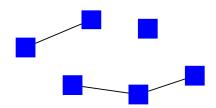
 $ho_k = rac{e^{-z}z^k}{k!}$ Poisson-Distributed (Erdős–Rényi-Model with $p = rac{z}{n}$)

Cascades in Sparse Networks

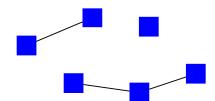


Cascades in Sparse Networks

Limited by Connectivity



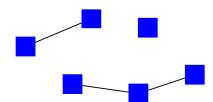
Cascades in Sparse Networks



Limited by Connectivity

Cascade Size Exhibits Power-Law Distribution

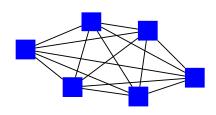
Cascades in Sparse Networks



- Limited by Connectivity
- Cascade Size Exhibits Power-Law Distribution

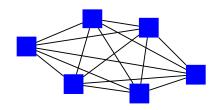
Most Highly Connected Cluster is Critical Triggers

Cascades in Dense Networks



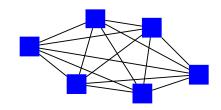
Cascades in Dense Networks

Limited by Threshold



Cascades in Dense Networks

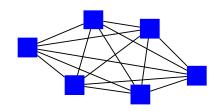
Limited by Threshold



Cascade Size Bimodal (Most are Small, Some are Large)

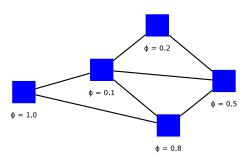
Cascades in Dense Networks

Limited by Threshold

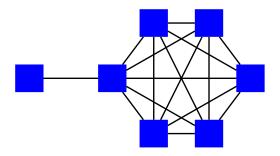


► Cascade Size Bimodal (Most are Small, Some are Large)

Cluster with Average Degrees are Triggers (Because They are Frequent)



► Threshold Heterogenity Increases Cascade Likelihood



▶ Degree Heterogenity Decreases Cascade Likelihood

► No Personal Knowledge

- ▶ No Personal Knowledge
- ► No Global Adoption Rate

- ▶ No Personal Knowledge
- ► No Global Adoption Rate
- No Relationship Strength

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- Sample Size for Bimodal Distribution Very Limited

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- No Global Adoption Rate
- ► No Relationship Strength
- One-Way Threshold
- Sample Size for Bimodal Distribution Very Limited
- No Threats to Validity Mentioned

Thank You All For Listening