

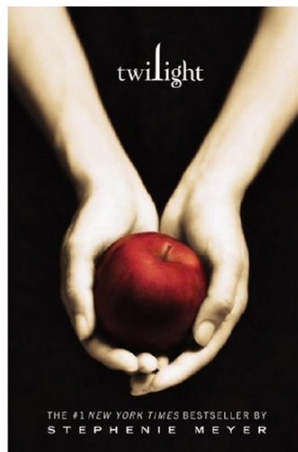
# Watts' Network Cascades Model

## A Simple Model of Global Cascades on Random Networks

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2016-08-05

- ▶ Motivation
- ▶ Simulation
- ▶ Explanation
- ▶ Watts' Model
- ▶ Findings
- ▶ Limitations



## Twilight

Source: <https://en.wikipedia.org/wiki/File:Twilightbook.jpg>



## WhatsApp

Source: <https://commons.wikimedia.org/wiki/File:WhatsApp.svg>



## Political Coups

Source: <http://tinyurl.com/jmv529r>

# The Cause Revealed

## Network Cascades

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(Maybe)



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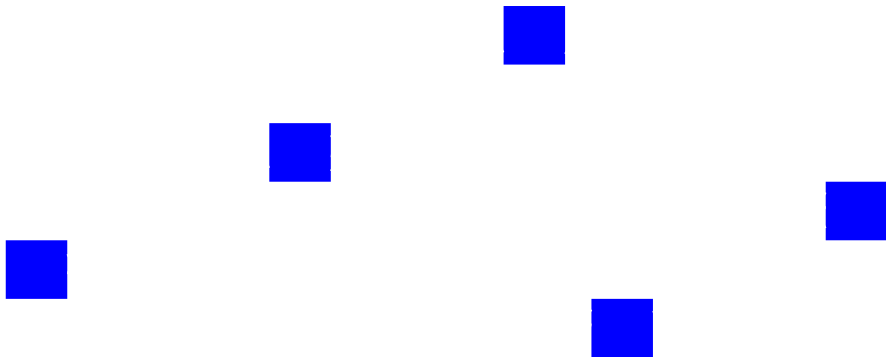
(It's a Nice Model Anyway)

# Simulation

<https://github.com/turbopope/nss/tree/master/simulator>

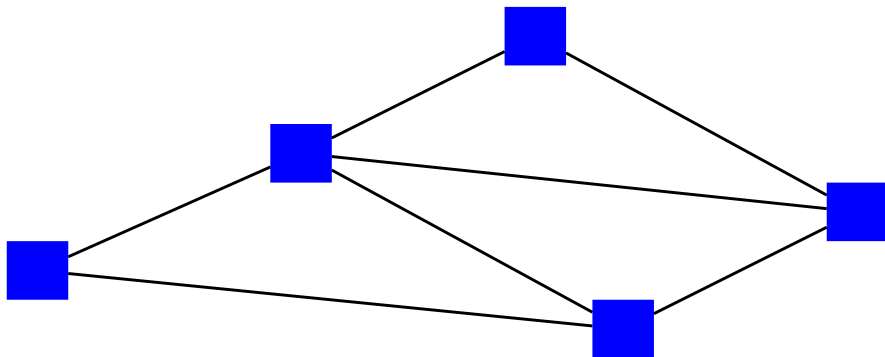
# Explanation by Example

## ► Nodes



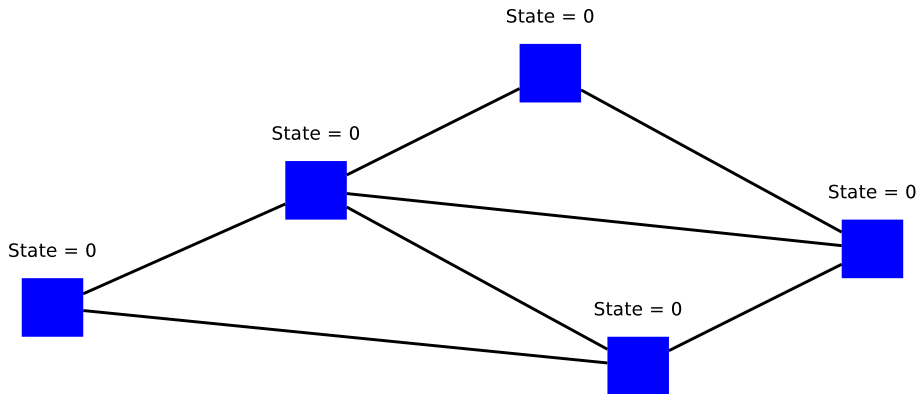
# Explanation by Example

- Observe  $k$  Neighbors



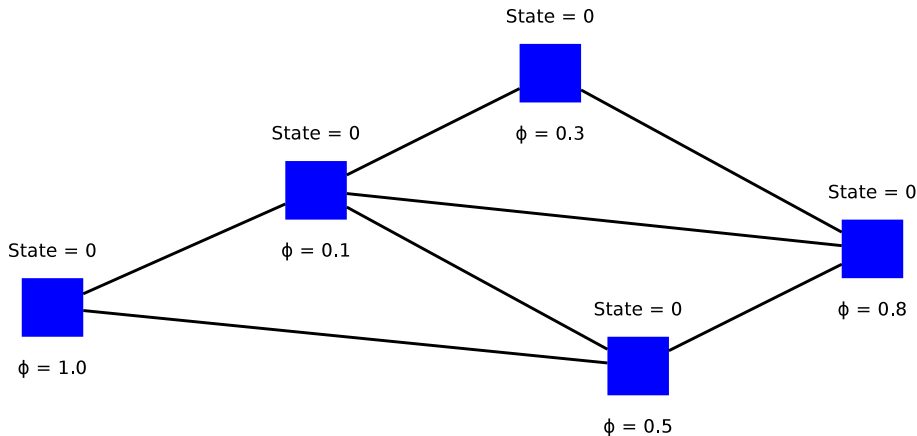
# Explanation by Example

- State  $\in \{0, 1\}$



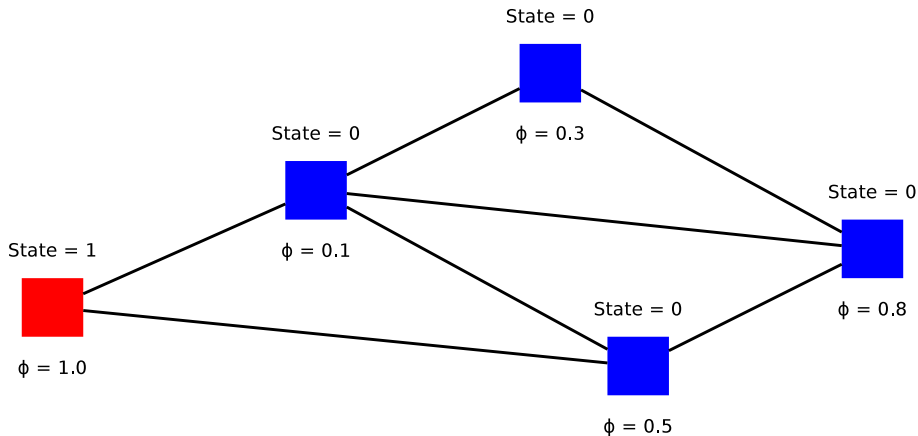
# Explanation by Example

- Threshold  $\Phi \in [0, 1]$



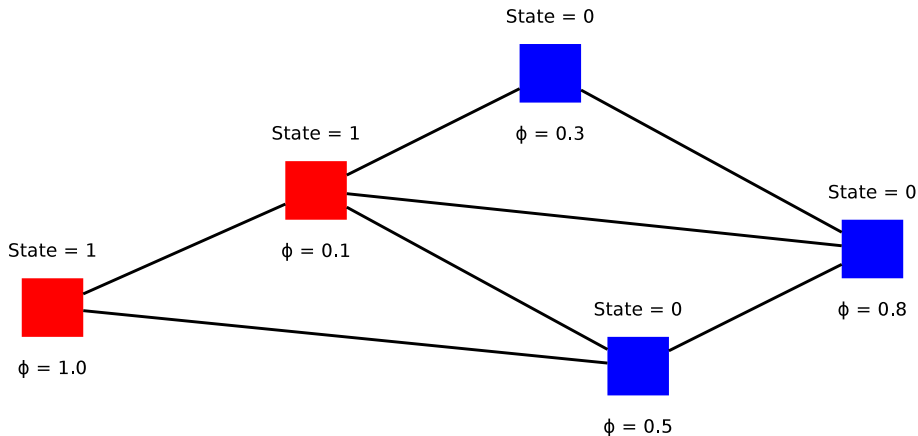
# Explanation by Example

## ► Random Impulse Happens



# Explanation by Example

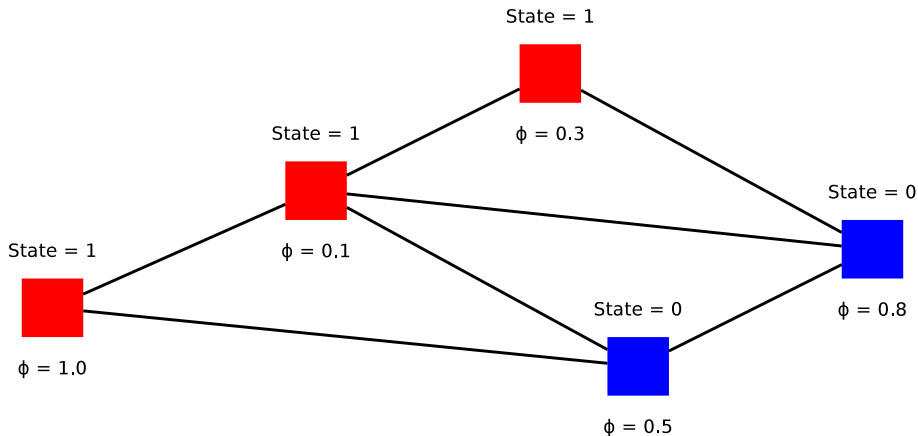
## ► Nodes Check in Random Intervals





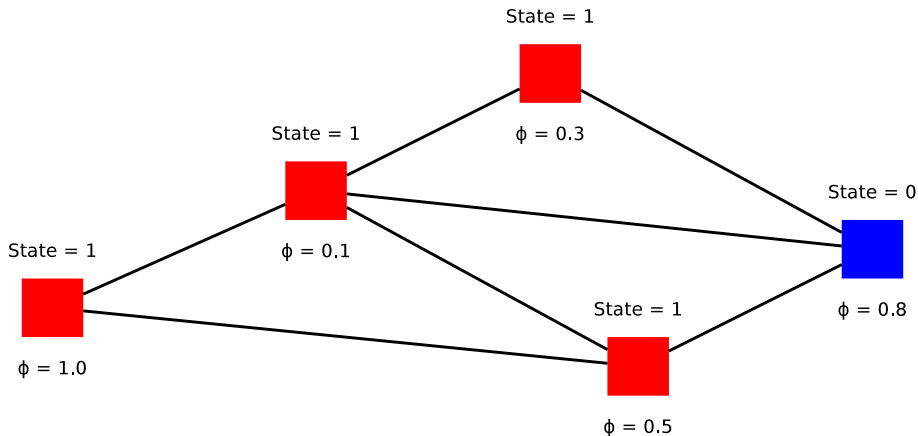
# Explanation by Example

## ► Stuff Happens



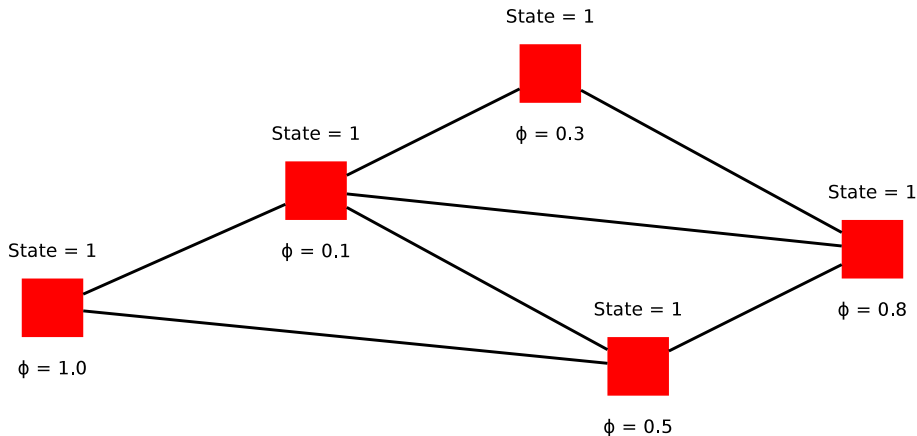
# Explanation by Example

## ► Things Occur



# Explanation by Example

## ► Coup Successful



- ▶ Each person/agent is a node in a graph
- ▶ Agents have a state  $\in \{0, 1\}$
- ▶ Agents observe their neighbors
- ▶ Agents change to a state if a fraction of their neighbors has that state

# Watts' Model – Random Graph

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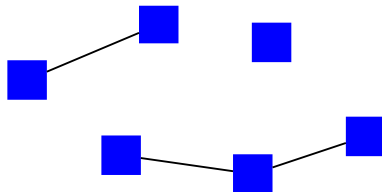
- ▶  $n$  nodes
- ▶  $p_k$  propability of  $n$  to have  $k$  neighbors
- ▶  $z = \langle k \rangle$  expectation value or average degree



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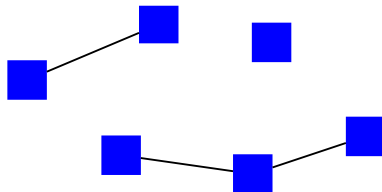
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- ▶  $z = \langle k \rangle$  expectation value or average degree
- ▶  $p_k = \frac{e^{-z} z^k}{k!}$  Poisson-distributed (Erdős–Rényi-Model with  $p = \frac{z}{n}$ )

- Cascades in Sparse Networks

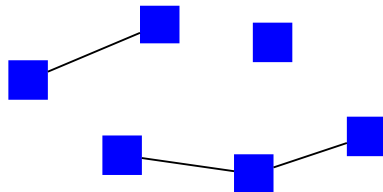


- ▶ Cascades in Sparse Networks

- ▶ Limited by Connectivity



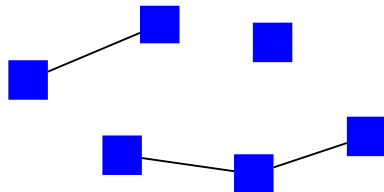
- ▶ Cascades in Sparse Networks



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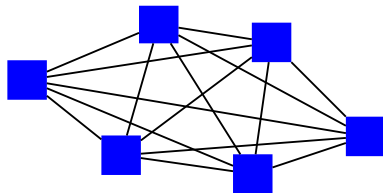
- ▶ Cascade Size Exhibits Power-Law Distribution

- Cascades in Sparse Networks

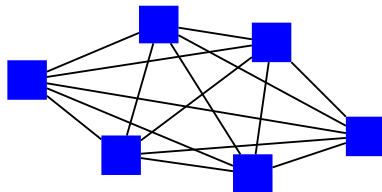


- Limited by Connectivity
- Cascade Size Exhibits Power-Law Distribution
- Most Highly Connected Cluster is Critical Triggers

- Cascades in Dense Networks



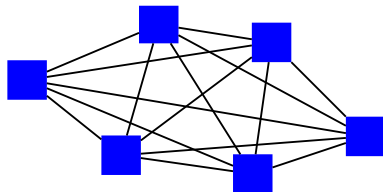
- ▶ Cascades in Dense Networks
  - ▶ Limited by Threshold



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- ▶ Limited by Threshold

- ▶ Cascade Size Bimodal (Most are Small, Some are Large)



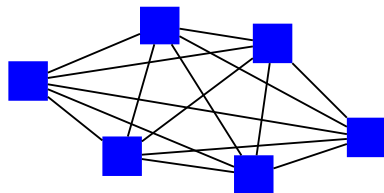


- ▶ Cascades in Dense Networks

- ▶ Limited by Threshold

- ▶ Cascade Size Bimodal (Most are Small, Some are Large)

- ▶ Cluster with Average Degrees are Triggers (Because They are Frequent)



# Findings

- ▶ Threshold Heterogeneity Increases Cascade Likelihood

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- ▶ Degree Heterogeneity Decreases Cascade Likelihood

# Limitations

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- ▶ Sample Size for Bimodal Distribution Very Limited
- ▶ No Threats to Validity Mentioned

Thank You All For Listening