

```

""#-----#""
""#-----METU Cognitive Sciences-----#""
""#-----Turgay Yildiz-----#""
""#-----yildiz.turgay@metu.edu.tr-----#""
""#-----#""

```

```

""-----""
""-----Exercise 3.1-----""
""-----""

```

```

; Define a procedure GUESS. It will have one parameter, an integer including and
; between 0 and 99. You will make the computer make successive guesses to find
; this number, where each guess will appear on the screen – use PRINT for this. You
; will need the LISP expression (random 100) to make a guess. Needless to say,
; the only acceptable way to go on making guesses as long as needed is keep calling
; yourself.

```

```

(defun guess (x)

  (let ((y (random 100)))

    (cond ((= x y) x)
          ((print y) (guess x))
          )
    )
)

```

```

"" random 100 will change if you call it again even inside let ""

```

```

; (let ( ( y (random 100) ) )
;
; (and (print y) (print (random 100) ) )
; )

```

```

"" returned : 39 70 70 ""

```

```

""-----#""
""-----Exercise 3.2-----#""
""-----#""

```

```

; Define a procedure that multiplies two integers using only addition as a primitive
; arithmetic operation.

```

```

(defun mltp (x y)

  (if (= x 0)
      0
      (+ (mltp (- x 1) y) y)
  )
)

```

```

(defun mltp2 (x y z )

  (if (= x 0)
      z
      (mltp2 (- x 1) y (+ y z) )
  )
)

```

```

(defun mltp3 (x y)

  (mltp2 x y 0)
)

```

```

""-----#""
""-----Exercise 3.3-----#""
""-----#""

```

; The factorial of a non-negative integer is defined as follows:

```
(defun factorial (x)
```

```
  (if (= x 0)
      1
      (* (factorial (- x 1)) x)
  )
```

```
""-----""
""-----Exercise 3.4-----""
""-----""
```

; Define a recursive procedure that computes the sum of the squares of the first n
; non-negative integers.

```
(defun sumOfSquares (x)
```

```
  (if (= x 1)
      1
      (+ (sumOfSquares (- x 1)) (* x x) )
  )
```

```
""-----""
""-----Exercise 3.5-----""
""-----""
```

; The way to toss a fair coin in LISP is to do (random 2), which would evaluate to
; 0 or 1 with a fifty-fifty chance.

```
(defun toss (n)
```

```
  (if (and (> n 1) (print (random 2)) )
      (toss (- n 1))
      (defvar end (print (random 2) ))
  )
)
```

```
""-----""
""-----Exercise 3.6-----""
""-----""
```

```
(defun coll (n)
```

```
  (cond ( (= n 1) 1)
        ( (evenp n) (coll (/ n 2)) )
        ( (oddp n) (coll (+ (* 3 n) 1)) )
  )
)
```

```
""-----""
""-----Exercise 3.7-----""
""-----""
```

; Define a recursive procedure that takes two integers, say x and y, and returns the
; sum of all the integers in the range including and between x and y. Do not use a
; formula that directly computes the result.

```
(defun sumRange (x y)
```

```
  (if (= x y)
      x
      (+ (sumRange x (- y 1)) y)
  )
)
```

Exercise 3.9

```
(defun exponential (x y)
  (if (= x 1)
      y
      (* (exponential (- x 1) y) y)
  )
)
```

Exercise 3.10

; The Fibonacci numbers

```
(defun fib (n)
  (if (< n 2)
      n
      (+ (fib (- n 1)) (fib (- n 2)) )
  )
)
```

Exercise 3.11

; Newton's Method

```
(defun getnewY (x y)
  (let ( (newY (/ (+ (/ x y) y) 2) ) )
    newY
  )
)
```

```
(defun newton (x newY)
  (print "initial guess : " )
  (print newY)
  (if (<= (abs (- x (* newY newY))) 0.00001 )
      newY
      (newton x (getnewY x newY))
  )
)
```

Exercise 3.12

; Sum of a geometric progression. $a.r^0 + a.r^1 + a.r^2 \dots + a.r^n = a (r^0 + r^1 + \dots + r^n)$

```
(defun geo (a r n)
  (if (= n 0)
      a
      (+ (* a (expt r n) ) (geo a r (- n 1)) )
  )
)
```

```

"""-----"""
"""-----Exercise 3.13-----"""
"""-----"""

```

```

; (RANDOM N) returns a random number between and including 0 and n - 1. Define a
; procedure that takes two arguments n and r, and prints r random numbers between
; and including 0 and n. You will need to use PRINT; you can discover how it works
; by trying it at REPL.

```

```

(defun rd (n r)

  (if (= r 1)
      (random n)
      (and (print (random n)) (rd n (- r 1) ) )
  )
)

```

```

"""-----"""
"""-----Exercise 3.14-----"""
"""-----"""

```

```

; remember collatz function

```

```

(defun coll (n)
;
; (cond ( (= n 1) 1)
; ( (evenp n) (coll (/ n 2)) )
; ( (oddp n) (coll (+ (* 3 n) 1)) )
; )
; )

```

```

;; from SICP (here in clojure)
;; http://www.sicpdistilled.com/section/1.2.6/

```

```

(defun square (n)
  (* n n))

(defun dividesp (a b)
  (zerop (mod b a)))

(defun find-divisor (n test-divisor)
  (cond ((> (square test-divisor) n) n)
        ((dividesp test-divisor n) test-divisor)
        (t (find-divisor n (1+ test-divisor)))))

```

```

(defun smallest-divisor (n)
  (find-divisor n 2))

```

```

(defun primep (n)
  (= n (smallest-divisor n)))

```

```

(defun if-prime (x)

  (if (primep x)
      (and (print "Prime found : " ) (print x) t)
      (cond ( (= x 1) 1)
            ( (evenp x) (and (print x) (if-prime (/ x 2)) ))
            ( (oddp x) (and (print x) (if-prime (+ (* 3 x) 1) ) ) )
            )
      )
)

```

```

"""-----"""
"""-----Exercise 3.15-----"""
"""-----"""

```

```

;Your task is to write a program that takes a positive (n > 0) integer as an input and
;reduce it to 1 by using the Collatz' function. While doing this, you are required
;to report any prime number you encounter along the way. Besides reporting the
;primes, your program should also report and return the sum of these primes.
;You need to write two versions: one, call it K00, where you accumulate the sum
;as you go along and return it when you reach 1; the other, call it F00, where you do
;not accumulate the answer as you go along.

```

```

(defun collatz (x)
  (cond ( (= x 1)      1)
        ( (evenp x) (/ x 2) )
        ( (oddp  x) (+ (* 3 x) 1) ) )
  )

(defun foo (x)
  (if (= x 1)
      (and (print "END" ) t)

      (if (primep x)
          (and (print "Prime found : ") (print x) (foo (collatz x)) )
          (foo (collatz x)) )
      )
  )

(defun zo (x sum)
  (if (= x 1)

      (and (print "Total sum of the primes : ") (print sum) t)

      (if (primep x)
          (and (print "Prime found : ") (print x) (zo (collatz x) (+ x sum) ) )
          (zo (collatz x) sum )
          )
      )
  )

(defun zoo (x)
  (zo x 0)
)

```

```

"""-----"""
"""-----Exercise 3.16-----"""
"""-----"""

```

```

; Define a procedure that takes a positive integer (n > 0), reduces it to 1 by Collatz'
; algorithm, printing in each step, the difference between the current number and the
; one computed before it.

```

```

(defun collatz (x)
  (cond ( (= x 1)      1)
        ( (evenp x) (/ x 2) )
        ( (oddp  x) (+ (* 3 x) 1) ) )
  )

```

```
(defun collatz-diff (x)

  (if (= x 1)
      (and (print "END") t)

      (and (print (- (collatz x) x)) (collatz-diff (collatz x)) )
  )
)
```