EEE 391 HW #1 Turgut Alp Edis 21702587

a)
$$3e^{5\pi/3} + 4e^{-5\pi/6} => 0_1 = \frac{\pi}{3}$$
 $0_2 = \frac{\pi}{6}$ $0_3 = \frac{\pi}{6}$ $0_4 = \frac{\pi}{3}$ $0_5 = \frac{\pi}{6}$ $0_7 = \frac{\pi}{6}$

= 3.cos(
$$\frac{\pi}{5}$$
)+ \int . 3. sin($\frac{\pi}{5}$) + 4.cos($\frac{\pi}{5}$)+ \int .4. sin($\frac{\pi}{5}$)

$$= \frac{3}{2} + 3[3j + 2[3-2]] = \frac{3}{2} + 2[3+5](\frac{3[3-2]}{2})$$

b)
$$(1-j)^2$$
 = -2j => x=0 1 = $\sqrt{x^2+y^2}$ (Cartesian form) = -2j => x=0 0 0 = $\sqrt{x^2+y^2}$

c)
$$(3-35)^{10}$$
 = -124416 + 124416 $37 = x = -124416$
(Cortesion Form) $y = 124416 \cdot 37 = x = -124416 \cdot 3$

d)
$$(\sqrt{2}+5)$$
 (1) $(\sqrt{4}+5)$ =) $x_1=12$ $x_2=1$ } $x_3=1$ $x_4=1$ $x_5=1$ x

=)
$$\frac{2e^{i\frac{\pi}{4}}}{2e^{i\frac{\pi}{4}}} = e^{i\frac{\pi}{12}}$$

e) Redje
$$5\pi 3$$
 = Refe⁵ = $7\pi 3$ = Refe⁵ = $\cos(\pi) = \frac{3}{2}$

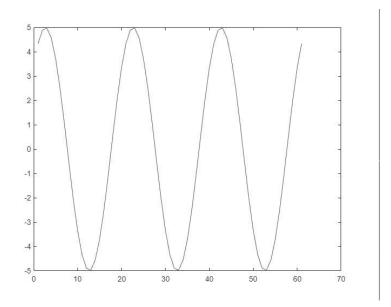
=)
$$x=\frac{1}{2}y=0$$
 => $r=\frac{1}{2}\theta=\pi$ => $\frac{1}{2}e^{3\pi}$

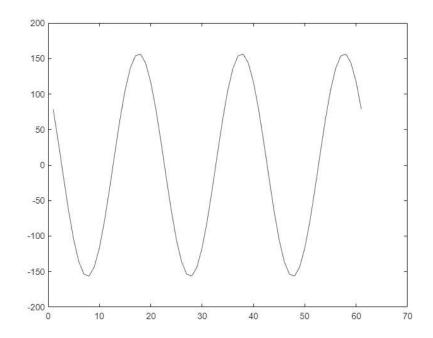
$$f(1-j)$$
 = 5+1 => x=1 y=1 => $r=1$ $\theta=4$ => e^{54} (Cartesian form)

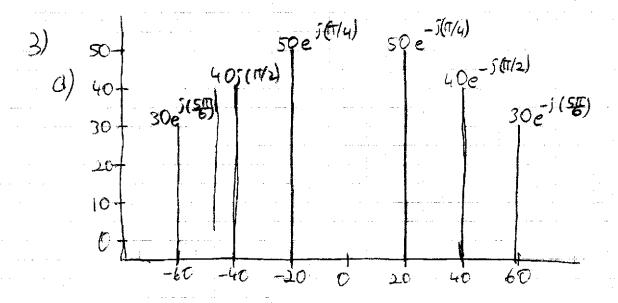
9)
$$(3-3)^{-1}$$
 => $x=\sqrt{3}$ $y=-3=$) $r=2\sqrt{3}$ $0=\frac{2\pi}{3}=$ > $(2\sqrt{3}e^{\frac{3}{2}})^{-1}$
(cartesion form)

$$= \frac{e^{-\frac{12\pi}{3}}}{2(3)} = \frac{3e^{-\frac{12\pi}{3}}}{6}$$

2) In this question, I used Matlab top lot the graphs.

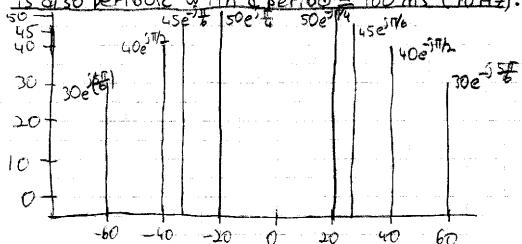






b) this signel is periodic with a period = 50ms (20 Hz).

c) T(t) is periodic with a period 1/30-5 (30 Hz). And the signal is also periodic with a period = 100 ms (10 Hz).



d) the new signal is not periodic because of the frequency of 140/11 Hz.

So the signal is not periodic

a)
$$o_0 = \frac{1}{2} \int_0^1 t dt + \frac{1}{2} \int_1^2 (2-t) dt = \frac{1}{2}$$

b)
$$g(t) = \frac{dx(t)}{dt} = \begin{cases} 1, & 0 \le t \le 1 \\ -1, & 1 \le t \le 2 \end{cases}$$

$$b_0 = \frac{1}{2} \int_0^1 dt - \frac{1}{2} \int_0^2 dt = 0 \text{ and } b_k = \frac{1}{2} \int_0^2 g(t) e^{-\int (2\pi/T)^k t} dt$$

$$-\frac{1}{2} \int_0^2 g(t) e^{-\int (2\pi/T)^k t} dt$$

$$= \frac{1}{2\pi k} \left[1 - e^{-\int \pi k} \right]$$

C)
$$y_n = \int nw X_n = \int \frac{1-e^{-\int nk}}{\int nk} = \int kw X_k$$

 $= \int X_k = \frac{e^{-\int nk}}{\int n^2 + \int k^2}$

$$X(t) = 2.2 \cos(1800 \pi t - \pi/3)$$

$$X[n] = X_1[n] = X_2[n] = 2.2 \cos(0.3\pi \eta - \pi/3)$$

$$X_1 [n] = 2.2 \cos(-0.3 \pi n + 2 \pi n + \pi/3)$$

$$X_2(t) = 2.2 \cos(13800 \text{ T} t - \pi/3)$$

6)

a) $y_1[n] = \chi[n] * h[n] = \sum_{k=-\infty}^{\infty} \chi[k] h[n-k]$

71[n] = h [-1] x [n+1] + h [1] x [n-1] = 2x [n+1] + 2x [n-1] 41 [n] = 28[n+1] + 48[n] -28[n+2] +28[n-1] + 48[n-2] -28[n-4]

71[n] = -28[n-4] +28[n-2] +28[n-1] +48[n] +28[n+1]

(b) $y_2[n] = x[n+2] *h[n] = \sum_{k=-\infty}^{\infty} h[k] x[(n+2)-k] => y_2[n] = y_4[n+2]$ So, $y_2[n] = -2\delta[n-2] + 2\delta[n] + 2\delta[n+1] + 4\delta[n+2] + 2\delta[n+3]$

C) $y_3 [n] = x[n] * h[n+2] = \sum_{k=-\infty}^{\infty} h[k] x[n+2-k]$ $= \sum_{k=-\infty}^{\infty} h[k] x[n+2-k]$ $= \sum_{k=-\infty}^{\infty} h[k] x[n+2-k] + \sum_{k=-\infty}^{\infty} h[k] x[n+2-k]$

73[n]=-28[n-2]+28[n]+28[n+]+48[h+2]+28[n+3]