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# Chapter 1

## Classes

### 1.1 poly.termorder – hoge class object

- Classes
  - †**TermOrderInterface**
  - †**UnivarTermOrder**
  - **MultivarTermOrder**

### 1.1.1 TermOrderInterface – interface of term order

#### Initialize (Constructor)

**TermOrderInterface**(comparator: *function*)  $\rightarrow$  *TermOrderInterface*

A term order is primarily a function, which determines precedence between two terms (or monomials). By the precedence, all terms are ordered.

More precisely in terms of `Python`, a term order accepts two tuples of integers, each of which represents power indices of the term, and returns 0, 1 or -1 just like `cmp` built-in function.

A `TermOrder` object provides not only the precedence function, but also a method to format a string for a polynomial, to tell degree, leading coefficients, etc.

`comparator` accepts two tuple-like objects of integers, each of which represents power indices of the term, and returns 0, 1 or -1 just like `cmp` built-in function.

This class is abstract and should not be instantiated. The methods below have to be overridden.

## Methods

### 1.1.1.1 `cmp`

`cmp(self, left: tuple, right: tuple) → integer`

Compare two index tuples `left` and `right` and determine precedence.

### 1.1.1.2 `format`

`format(self, polynom: polynomial, **keywordsdict)  
→ string`

Return the formatted string of the polynomial `polynom`.

### 1.1.1.3 `leading_coefficient`

`leading_coefficient(self, polynom: polynomial) → CommutativeRingElement`

Return the leading coefficient of polynomial `polynom` with respect to the term order.

### 1.1.1.4 `leading_term`

`leading_term(self, polynom: polynomial) → tuple`

Return the leading term of polynomial `polynom` as tuple of (degree index, coefficient) with respect to the term order.

## 1.1.2 `UnivarTermOrder` – term order for univariate polynomials

### Initialize (Constructor)

`UnivarTermOrder(comparator: function) → UnivarTermOrder`

There is one unique term order for univariate polynomials. It's known as degree.

One thing special to univariate case is that powers are not tuples but bare integers. According to the fact, method signatures also need be translated from the definitions in `TermOrderInterface`, but its easy, and we omit some explanations.

`comparator` can be any callable that accepts two integers and returns 0, 1 or -1 just like `cmp`, i.e. if they are equal it returns 0, first one is greater 1, and otherwise -1. Theoretically acceptable comparator is only the `cmp` function.

This class inherits **TermOrderInterface**.

## Methods

### 1.1.2.1 format

```
format(self, polynom: polynomial, varname: string='X', reverse:  
bool=False)  
    → string
```

Return the formatted string of the polynomial `polynom`.

- `polynom` must be a univariate polynomial.
- `varname` can be set to the name of the variable.
- `reverse` can be either `True` or `False`. If it's `True`, terms appear in reverse (descending) order.

### 1.1.2.2 degree

```
degree(self, polynom: polynomial) → integer
```

Return the degree of the polynomial `polynom`.

### 1.1.2.3 tail\_degree

```
tail_degree(self, polynom: polynomial) → integer
```

Return the least degree among all terms of the `polynom`.

This method is *experimental*.

## 1.1.3 MultivarTermOrder – term order for multivariate polynomials

### Initialize (Constructor)

```
MultivarTermOrder(comparator: function) → MultivarTermOrder
```

This class inherits **TermOrderInterface**. Though this class is the main purpose of the module, descriptions of every methods are identical to the base class.

# Bibliography