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## Chapter 1

### **Functions**

- 1.1 arygcd binary-like gcd algorithms
- 1.1.1 bit num the number of bits

```
\text{bit} \quad \text{num(a: } integer) \rightarrow integer
```

a のビット数の値を返す。

1.1.2 binarygcd – gcd by the binary algorithm

```
	ext{binarygcd}(	ext{a:} integer, 	ext{b:} integer) 
ightarrow integer
```

binary gcd algorithm を使って a, b の最大公約数の値を返す。

1.1.3 arygcd i – gcd over gauss-integer

```
arygcd_i(a1: integer, a2: integer, b1: integer, b2: integer)
→ (integer, integer)
```

二つの gauss 数体 a1+a2i, b1+b2i の最大公約数の値を返す。 "i" は虚数。

If the output of  $arygcd_i(a1, a2, b1, b2)$  is (c1, c2), then the gcd of a1+a2i and b1+b2i equals c1+c2i.

†This function uses (1+i)-ary gcd algorithm, which is an generalization of the binary algorithm, proposed by A.Weilert[2].

#### 1.1.4 arygcd w – gcd over Eisenstein-integer

```
\begin{array}{c} \mathtt{arygcd\_w(a1:} \ integer, \ \mathtt{a2:} \ integer, \ \mathtt{b1:} \ integer, \ \mathtt{b2:} \ integer) \\ \longrightarrow (integer, \ integer) \end{array}
```

Eisenstein 数体  $a1+a2\omega$ ,  $b1+b2\omega$  の最大公約数の値を返す。" $\omega$ " は 1 の虚立方根。

If the output of arggcd\_w(a1, a2, b1, b2) is (c1, c2), then the gcd of a1+a2 $\omega$  and b1+b2 $\omega$  equals c1+c2 $\omega$ .

†This functions uses  $(1-\omega)$ -ary gcd algorithm, which is an generalization of the binary algorithm, proposed by I.B. Damgård and G.S. Frandsen [1].

#### Examples

```
>>> arygcd.binarygcd(32, 48)
16
>>> arygcd_i(1, 13, 13, 9)
(-3, 1)
>>> arygcd_w(2, 13, 33, 15)
(4, 5)
```

## Bibliography

- [1] Ivan Bjerre Damgård and Gudmund Skovbjerg Frandsen. Efficient algorithms for the gcd and cubic residuosity in the ring of Eisenstein integers. Journal of Symbolic Computation, Vol. 39, No. 6, pp. 643–652, 2005.
- [2] André Weiler. (1+i)-ary gcd computation in  $\mathbb{Z}[i]$  as an analogue to the binary gcd algorithm. *Journal of Symbolic Computation*, Vol. 30, No. 5, pp. 605–617, 2000.