Personalized potassium and phosphorus intake recommendations can be reasoned for end-stage renal failure patients by simulating with hierarchical Bayesian multivariate model

Supplementary Materials

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This notebook reproduces in detail the analysis of personal diet recommendations described in the main article. The notebook starts visualizing the collected raw data, prepares it for analysis and estimates personal reaction models with these data. The personal reaction models are combined with the estimation of the current personal diets for constructing personal graphical models. These personal models generate the levels of blood concentrations when a diet is given, they are used in simulating recommended personal diets for reaching predefined normal concentrations. Finally, these personal diet recommendations are compared for showing the divergence among the studied patients.

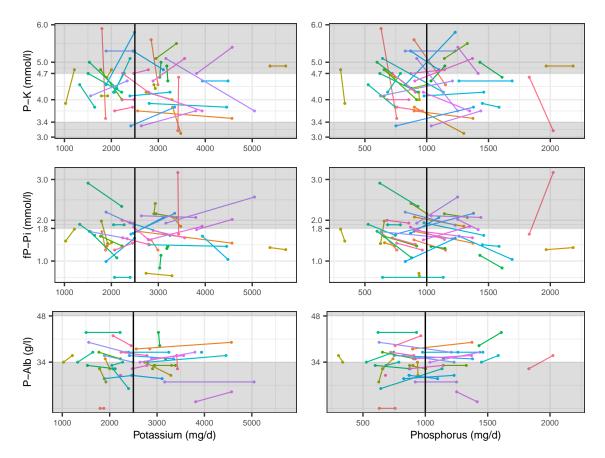
The notebook execution generates all the figures and tables that are included in the article, and produces also the referenced supplementary figures. The article is accompanied with a PDF rendetion of the notebook that shows all the supplementary figures and important parts of the program code so that the analysis can be followed in detail. The executable RMarkdown notebook with data can be found in a public Github repository of the corresponding author.

Dialysis patient data

The analyzed dataset consists of food records and laboratory measurements from end-stage renal patients in dialysis. Following nutrients are possible considered as predictors of concentrations. Note that we use energy-% of fats and protein as unit in our analysis. This is referred as Table 1 in the main article.

and also following personal details and medication are considered as predictors. This is referenced as Table 2 in the article.

Let us explore then how the intake of dietary potassium and phosphorus corresponds in data to plasma concentrations of potassium, phosphate and albumin



Supplementary Figure S 1: Figure shows the progress between two observations of plasma potassium (P-K), fasting plasma phosphate (fP-Pi) and plasma albumin (P-Alb) concentrations of the studied patients. White regions in the panels show the recommended concentration levels, P-K 3.4 - 4.7 mmol/l, fP-Pi < 1.8 mmol/l and P-Alb 34 - 48 g/l. Vertical black lines denote the commonly recommended maximum intakes of these nutrients. The goal is to find personal intake levels that keep the concentrations in recommended levels, if possible. The figure is plotted with ggplot2 package for R language (v 3.3.5, https://ggplot2.tidyverse.org).

Aim of this analysis is to find such personal levels of potassium and phosphorous intakes that keep all these concentrations in their normal levels marked with white regions, if possible.

Development of nutrition reaction model

In this work we construct personal generative models for concentrations that allow conditioning personal diet recommendations. Essential part of these models is the personal reactions to nutrients and other predictors. Simultaneous reactions on all considered concentrations are modeled as multivariate model that has all the concentrations are response variables.

For comparison, we estimate multivariate systems with and without cross-model covariance. With cross-model covariance estimated, the model corresponds to seemingly unrelated model system, and without the model is Bayesian network with separated local distributions. This simpler model is estimated first with only potassium and phosphorous concentrations as responses.

initial_graph <- mebn.fully_connected_bipartite_graph(datadesc_fat_epros)</pre>

In Bayesian network both responses were estimated separately. Next, we estimate a multivariate model where both distribution are estimated during single sampling. It does not factorize into separate distributions, but allows using more data.

Next we like to add plasma albumin concentration as a third constraint in the model, but unfortunately 8 of 37 patients have missing albumin measurements. From such a small dataset we don't want to remove any patients and so we predict the missing albumin levels and impute them to dataset.

For prediction, estimate the model without missing values in P-Alb. The rows with missing values are held out from the density estimation, but patients are kept in the model for estimating their parameters.

```
inputdata = dialysis,
targetdata = holdout_index,
predictor_columns = assumedpredictors_fat_epros,
assumed_targets = pk_fppi_palb_targets,
group_column = "potilas",
local_estimation = mebn.multivariate_sampling,
local_model_cache =
    "models/BLMM_gamma_qr_multivariate3/fat_epros_missing_palb",
stan_model_file = "mebn/v2/BLMM_gamma_qr_mv_cv.stan",
normalize_values = TRUE)
```

Personal data imputation models

Now we can create personal models for patients that have missing plasma albumin measurements. These models are then used for making personal predictions for replacing missing values.

Then we predict missing values with these data imputing models

```
# and use the data in this row to predict palb
  evidence <- rows_with_missing_palb[i, assumedpredictors_fat_epros$Name]</pre>
  posterior prediction <- mebn.personal prediction(reaction graph = personal graph,
                                   graph_dir = personal_model_dir,
                                   evidence = evidence,
                                   stan_model_file = "diet/posterior_prediction.stan")
  \# personal_predictions contains predictions multivariate predictions
  # P-K and fP-Pi are known, but P-Alb is missing
  posterior <- rstan::extract(posterior_prediction, par= "posterior[3]")</pre>
  # use predicted posterior mean for missing P-Alb value
  # - this is i:th NA value in dialysis
  predicted_palb <- mean(posterior$`posterior[3]`)</pre>
   \textit{\# rows in 'rows\_with\_missing\_palb' and 'original\_palb' are in same order } \\
  # so we can imput in the NA values at 'original_palb'
  for (m in 1:imput length)
      if (is.na(original_palb[m]))
          original_palb[m] <- predicted_palb</pre>
          break:
 }
}
dialysis2 <- dialysis
dialysis2$palb <- original_palb</pre>
saveRDS(dialysis2, "data/DIALYSIS_imputed_palb.rds")
```

With this data imputation we can estimate a cross-covariance model with three responses

```
pk_fppi_palb_targets <- datadesc_fat_epros[datadesc_fat_epros$Name %in% c('pk','fppi','palb'),]
initial_graph <- mebn.fully_connected_bipartite_graph(datadesc_fat_epros)</pre>
```

Finally, we consider also the effect of dialysis treatment type as new level of grouping in data. This allows us to estimate average effects of nutrition for each treatment type and then also personal effects within those treatments.

```
dialysis_imputed <- readRDS("data/DIALYSIS_imputed_palb.rds")</pre>
# add the dialysis treatment type as a grouping factor
dialysis_imputed$hoitoryhma <- as.factor(dialysis_imputed$hoitomuoto)</pre>
# and sort the data by treatment/patient/observation
dialysis_imputed <- dialysis_imputed[order(dialysis_imputed$hoitoryhma,</pre>
                                            dialysis imputed$potilas, dialysis imputed$havainto),]
dialdiet_gamma_mv3_two_level <- mebn.bipartite_two_level_multivariate(</pre>
                                    reaction_graph = initial_graph,
                                    inputdata = dialysis_imputed,
                                    targetdata = no holdout,
                                    predictor_columns = assumedpredictors_fat_epros,
                                    assumed_targets = pk_fppi_palb_targets,
                                    group_column = "hoitoryhma",
                                    subject_column = "potilas",
                                    local_estimation = mebn.two_level_multivariate_sampling,
                                    local model cache =
                                      "models/BLMM_gamma_mv_cross/two_levels",
                                    stan model file =
                                      "mebn/v2/BLMM_gamma_two_level_grouping.stan",
                                    normalize values = TRUE)
write.graph(dialdiet gamma mv3 two level,
            "graphs/dialysis_gamma_two_level_grouping.graphml", "graphml")
```

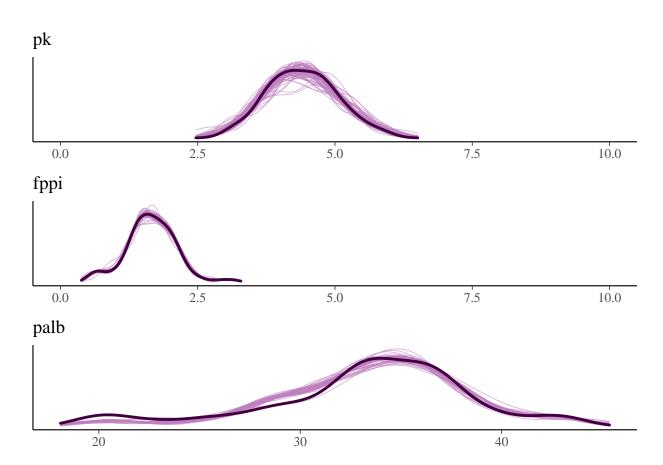
Model analysis

Here we evaluate the model's ability to repeat the measured observations with normalized root mean square error (NRMSE) and compare how adding the dialysis treatment as an explicit hierarchical layer in the model affects this error. We also assess the model's performance with visual posterior predictive check by comparing samples from the model with measured values. This would give away possible bias in the model.

Supplementary Table S 1: Supplementary Table S1: Comparison of model candidates. Personal graphical models with different reaction model candidates are evaluated with NRMSE for each modeled concentration and average model error.

	NRMSE						
Reaction model	P-K	fP-Pi	P-Alb	average error			
mv3_cross_two_levels mv3_cross_single_level		0.007 0.13	$0.002 \\ 0.059$	0.004 0.036			

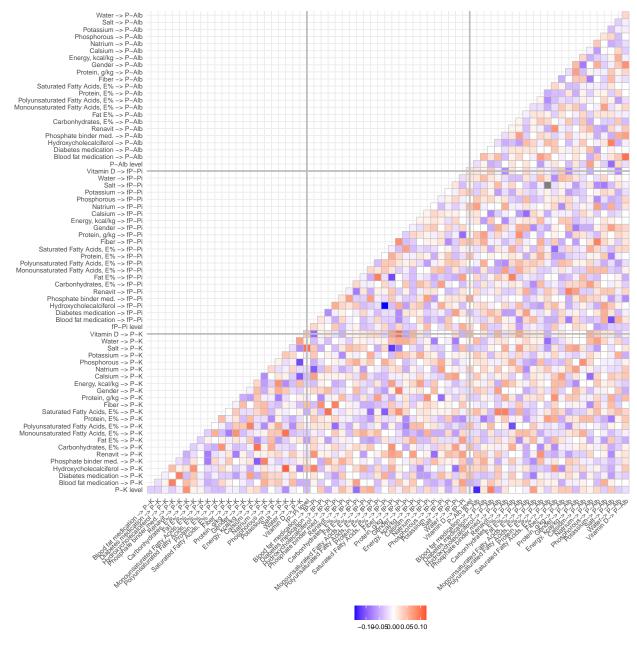
```
## [1] "pk"
## [1] "fppi"
## [1] "palb"
```



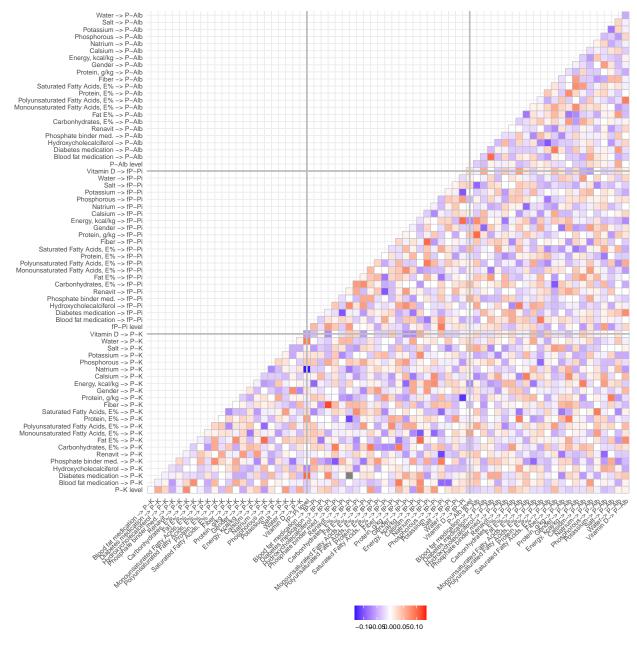
Supplementary Figure S 2: Posterior predictive check of the model where three concentrations and their parameters are stacked into one univariate model for estimating cross-model correlations.

Then we drill into the estimated correlation matrices of effects. The model estimates how much the effects of nutrients vary from general effects in dialysis treatment level and further how the effects vary personally within a treatment. These correlation plots show how the effects are correlated.

Scale for 'fill' is already present. Adding another scale for 'fill', which ## will replace the existing scale.



Supplementary Figure S 3: Correlation plot of matrix C_g that includes the estimated within-model and cross-model correlations in level of dialysis treatment



Supplementary Figure S 4: Correlation plot of matrix C_b that includes the estimated within-model and cross-model correlations of personal effects

Supplementary Table S 2: Table shows 40 highest positive or negative correlations between treatment effects of potassium and phosphorous with other treatment effects. This structure of correlations is used in estimating the personal effects based on personal intake and matching concentrations.

Treatment-level effects of nutrients							
Effect 1	Effect 2	Correlation					
Energy, kcal/kg -> P-K Natrium -> P-K Hydroxycholecalciferol -> fP-Pi Phosphorous -> P-K Calsium -> fP-Pi	Potassium -> P-K Potassium -> fP-Pi Potassium-> P-Alb Potassium -> fP-Pi Potassium -> P-K	0.083 0.073 0.070 0.065 0.063					
Diabetes medication -> fP-Pi Polyunsaturated Fatty Acids, E% -> fP-Pi Water -> P-Alb Diabetes medication -> P-K Protein, g/kg -> fP-Pi	Potassium-> P-Alb Potassium -> P-K Potassium -> P-K Potassium -> fP-Pi Potassium -> P-K	0.060 0.057 0.056 0.053 0.046					
Blood fat medication -> P-Alb Potassium -> fP-Pi Carbonhydrates, E% -> P-Alb Protein, E% -> P-K Natrium -> fP-Pi	Potassium -> P-K Potassium -> P-K Potassium -> fP-Pi Potassium-> P-Alb Potassium-> P-Alb	0.042 -0.040 -0.045 -0.048 -0.050					
fP-Pi level Fat E% -> P-K Gender -> P-Alb Phosphate binder med> P-Alb Protein, g/kg -> P-K	Potassium-> P-Alb Potassium -> P-K Potassium -> fP-Pi Potassium -> fP-Pi Potassium -> P-K	-0.052 -0.056 -0.057 -0.064 -0.076					
Protein, g/kg -> P-K Fiber -> fP-Pi Water -> P-K Potassium -> fP-Pi Carbonhydrates, E% -> P-K	Potassium -> fP-Pi Phosphorous-> P-Alb Phosphorous-> P-K Phosphorous -> P-K	-0.087 0.093 0.067 0.065 0.058					
Fat E% -> fP-Pi Protein, E% -> P-Alb Monounsaturated Fatty Acids, E% -> fP-Pi Fat E% -> P-K Saturated Fatty Acids, E% -> P-K	Phosphorous -> P-K Phosphorous -> P-K Phosphorous-> P-Alb Phosphorous -> P-K Phosphorous-> P-Alb	0.056 0.051 0.048 0.047 0.046					
Monounsaturated Fatty Acids, E% -> P-K Protein, E% -> fP-Pi Blood fat medication -> P-K Fat E% -> fP-Pi Phosphate binder med> P-Alb	Phosphorous -> fP-Pi Phosphorous -> fP-Pi Phosphorous -> fP-Pi Phosphorous -> fP-Pi Phosphorous-> P-Alb	-0.048 -0.050 -0.051 -0.053 -0.054					
Phosphate binder med> fP-Pi Calsium -> P-Alb fP-Pi level Protein, E% -> P-K Phosphorous -> P-Alb	Phosphorous -> fP-Pi Phosphorous-> P-Alb Phosphorous-> P-K Phosphorous -> fP-Pi	-0.056 -0.056 -0.062 -0.071 -0.073					
Renavit -> P-K	Phosphorous -> fP-Pi	-0.091					

Supplementary Table S 3: Table shows 40 highest positive or negative correlations between personal effects of potassium and phosphorous with other personal effects. This structure of correlations is used in estimating the personal effects based on personal intake and matching concentrations.

Personal effects of nutrie		
Effect 1	Effect 2	Correlation
Phosphate binder med> P-K Calsium -> fP-Pi fP-Pi level Gender -> P-Alb Calsium -> P-K	Potassium -> fP-Pi Potassium -> P-K Potassium-> P-Alb Potassium-> P-Alb Potassium-> P-Alb	0.094 0.078 0.071 0.068 0.059
Saturated Fatty Acids, E% -> fP-Pi	Potassium -> fP-Pi	0.056
Saturated Fatty Acids, E% -> fP-Pi	Potassium-> P-Alb	0.055
Polyunsaturated Fatty Acids, E% -> P-Alb	Potassium -> fP-Pi	0.052
Gender -> fP-Pi	Potassium-> P-Alb	0.050
Diabetes medication -> fP-Pi	Potassium -> fP-Pi	-0.050
Monounsaturated Fatty Acids, E% -> P-K	Potassium -> fP-Pi	-0.053
Water -> P-Alb	Potassium -> P-K	-0.053
Blood fat medication -> P-Alb	Potassium -> P-K	-0.054
Protein, E% -> P-Alb	Potassium -> P-K	-0.055
Monounsaturated Fatty Acids, E% -> P-K	Potassium -> P-K	-0.060
Phosphate binder med> P-Alb	Potassium -> P-K	-0.067
Salt -> P-Alb	Potassium-> P-Alb	-0.077
Protein, E% -> fP-Pi	Potassium-> P-Alb	-0.079
Saturated Fatty Acids, E% -> P-K	Potassium -> fP-Pi	-0.089
Vitamin D -> fP-Pi	Potassium -> fP-Pi	-0.104
Saturated Fatty Acids, E% -> P-K	Phosphorous-> P-Alb	0.089
Calsium -> P-K	Phosphorous -> fP-Pi	0.077
Vitamin D -> fP-Pi	Phosphorous -> fP-Pi	0.071
Gender -> fP-Pi	Phosphorous -> P-K	0.066
Monounsaturated Fatty Acids, E% -> fP-Pi	Phosphorous -> P-K	0.056
Polyunsaturated Fatty Acids, E% -> fP-Pi	Phosphorous -> fP-Pi	0.046
Polyunsaturated Fatty Acids, E% -> P-K	Phosphorous-> P-Alb	0.045
Fat E% -> fP-Pi	Phosphorous-> P-Alb	0.045
Fiber -> fP-Pi	Phosphorous-> P-Alb	0.044
Protein, g/kg -> P-K	Phosphorous -> fP-Pi	-0.045
Diabetes medication -> P-K fP-Pi level Energy, kcal/kg -> P-K Renavit -> P-Alb Protein, g/kg -> P-Alb	Phosphorous-> P-Alb Phosphorous-> P-K Phosphorous -> P-K Phosphorous -> fP-Pi Phosphorous -> P-K	-0.046 -0.047 -0.051 -0.052 -0.054
Fiber -> P-Alb	Phosphorous-> P-Alb	-0.058
Water -> P-Alb	Phosphorous-> P-Alb	-0.063
Salt -> fP-Pi	Phosphorous-> P-Alb	-0.065
Calsium -> fP-Pi	Phosphorous -> fP-Pi	-0.074
Monounsaturated Fatty Acids, E% -> P-K	Phosphorous -> fP-Pi	-0.088

Overview of nutritional effects

Following tables include all the estimated nutrition effects in general, dialysis treatment and personal levels.

Supplementary Table S4: Nutrition effect magnitudes from nutrients and other modeled features $(j=1,\dots,22)$ to blood concentrations $(i=1,\dots,3)$ for analyzed patients $(p=1,\dots,37)$ in all three additive levels of the model. General effects $(\hat{\beta}_{ij})$ are shown to vary between patients in home hemodialysis, hospital hemodialysis, and peritoneal dialysis. First column of each dialysis type (avg) shows typical effect of the treatment $(\hat{\beta}_{ij}+\hat{g}_{ijk},k=1,\dots,3)$ that can further vary personally. Minimum and maximum of these personal effects are shown within each treatment $(\hat{\beta}_{ij}+\hat{g}_{ijk}+\hat{b}_{ijp})$. The table is sorted in decreasing order of between-treatment variation $(\hat{\sigma}_g)$ and all the estimates include their 90%-credible intervals.

			Home hemodialysis			Hospital hemodialysis			Peritoneal dialysis		
Nutrient	Conc.	General effect	avg	min	max	avg	min	max	avg	min	max
Water	P-Alb	-0.94 [-1.03; 2.79] -2.60	-1.33 [-3.96; 2.19] -0.92	-2.09 [-5.21; 2.75] -2.78	-0.99 $[-4.14; 2.37]$ 0.21	-0.43 [-2.51; 1.46] -0.27	-0.77 $[-2.17; 1.47]$	0.36 $[-3.68; 3.52]$ 1.34	-1.53 [-5.03; 3.24] -6.70	-2.08 [-5.59; 3.46] -7.97	-0.97 [-5.15; 3.14]
Natrium	P-Alb	[-0.24; 7.58] 3.46	[-9.95; 7.96] 2.63	[-16.47; 7.74] 1.07	[-6.29; 8.56] 3.59	[-7.82; 7.72] 3.42	-1.87 [-13.40; 7.77] 1.76	[-4.12; 8.06] 4.16	[-30.75; 7.59] 3.49	[-36.19; 8.14] 2.91	-5.36 [-24.93; 7.70] 4.13
Energy, kcal/kg	P-Alb	[1.76; 15.59] 0.24	[-5.85; 12.96] 0.83	[-6.48; 11.89] -0.40	[-5.90; 14.48] 1.45	[-5.54; 14.49] -0.87	[-7.86; 12.96] -2.26	[-4.11; 15.21] 0.61	[-5.50; 15.16] 0.85	[-5.71; 15.90] -0.06	[-4.85; 17.20] 1.79
Phosphorous	P-Alb	[0.30; 9.18] 0.98	[-6.93; 7.38] -2.22	[-8.26; 7.29] -2.99	[-6.89; 8.04] -1.75	[-5.55; 6.58] 0.99	[-8.24; 6.32] 0.01	[-5.61; 7.50] 1.73	[-5.63; 9.97] 0.99	[-6.80; 9.46] -0.28	[-5.14; 11.47] 1.26
Diabetes medication	P-Alb	[2.55; 5.86]	[-8.21; 7.17]	[-9.13; 6.95]	[-9.01; 8.29]	[-5.89; 4.66]	[-7.55; 4.72]	[-6.02; 6.63]	[-7.53; 10.12]	[-10.08; 9.25]	[-8.79; 10.17]
Renavit	P-Alb	7.67 [10.56; 23.52] 3.73	$\begin{array}{c} \textbf{8.89} \\ [-11.49; 22.52] \\ \textbf{2.74} \end{array}$	8.78 [-12.02; 22.63] 0.88	9.72 [-11.07; 23.87] 2.86	5.50 [-10.54; 22.08] 3.01	4.28 [-10.88; 22.95] 1.68	6.86 [-10.28; 22.56] 4.57	6.41 [-11.66; 22.37] 2.26	6.07 [-12.09; 22.46] 1.19	7.41 [-11.94; 23.58] 3.46
Hydroxycholecalc		[4.17; 10.25] -0.33	[-7.13; 9.43] - 0.97	[-9.11; 9.33] -2.20	[-9.90; 11.57] 0.45	[-4.00; 9.51] 0.22	[-6.12; 7.45] -1.41	[-4.02; 12.35] 1.48	[-9.21; 9.34] 0.90	[-10.08; 9.84] 0.12	[-11.16; 14.06 1.85
Potassium	P-Alb	[-0.22; 3.86] -1.28	[-6.09; 3.72] -0.19	[-6.85; 3.35] -2.12	[-7.04; 7.24] 1.38	[-2.90; 3.23] -1.18	[-4.22; 2.72] -4.28	[-1.88; 5.78] 0.51	[-3.16; 5.94] -0.40	[-4.47; 5.37] -0.58	[-4.13; 7.86] 1.29
Phosphate binder med.	P-Alb	[-2.86; 14.60]	[-9.29; 10.80]	[-9.90; 9.54]	[-10.25; 9.85]	[-9.01; 6.76]	[-12.97; 7.67]	[-9.86; 8.53]	[-7.38; 8.54]	$\left[-9.27; 10.76\right]$	[-7.68; 10.11]
Carbonhydrates, E%	P-Alb	-0.08 [-1.17; 10.36]	0.12 [-12.32; 11.02]	$\begin{bmatrix} 0.01 \\ [-13.04; 11.41] \end{bmatrix}$	$0.97 \\ [-12.77; 11.32]$	-0.42 [-13.22; 9.82]	-1.34 $[-13.94; 9.83]$	0.67 [-13.89; 10.27]	-0.39 [-13.16; 10.13]	-1.57 [-14.61; 10.58]	-0.38 [-12.88; 9.79]
Fiber	P-Alb	0.67 [1.37; 4.02] -1.11	0.74 [-3.17; 3.45] -0.82	0.62 $[-3.62; 3.69]$ -2.29	0.96 [-3.23; 4.63] -0.30	$egin{array}{c} {f 0.89} \\ [-2.88; 3.37] \\ {f 2.62} \end{array}$	0.63 $[-3.18; 3.47]$ 1.14	$\begin{bmatrix} 1.25 \\ [-3.14; 4.96] \\ 4.31 \end{bmatrix}$	0.54 [-5.02; 5.33] -1.74	0.49 $[-4.98; 5.52]$ -3.39	0.66 $[-5.10; 5.86]$ -0.90
Gender	P-Alb	[0.04; 7.33] -1.17	[-13.78; 6.85] 0.65	-2.29 [-17.44; 6.89] 0.06	[-15.40; 8.63]	[-5.38; 9.55] -1.66	[-7.53; 9.67] -2.85	[-4.49; 16.23] -0.36	[-13.81; 9.41] 1.96	[-15.65; 7.52] 1.50	-0.90 [-13.88; 14.29]
Blood lipid medication	P-Alb	[-0.48; 9.57]	[-6.05; 13.04]	[-7.70; 13.61]	[-6.12; 15.32]	[-5.63; 4.27]	[-9.07; 4.49]	[-5.07; 5.04]	[-6.75; 11.86]	[-8.54; 11.88]	[-7.17; 11.72]
Blood lipid medication	P-K	$[-1.42 \\ [-1.74; 2.05]$	-0.22 [-3.30; 3.06]	-0.30 [-3.64; 3.11]	$\begin{bmatrix} 0.02 \\ [-2.97; 3.25] \end{bmatrix}$	-0.41 [-1.33; 0.90]	-0.53 [-1.69; 0.94]	-0.25 $[-1.41; 1.35]$	-0.42 [-4.45; 1.92]	-0.58 [-5.03; 1.82]	-0.27 [-4.20; 1.92]
Diabetes medication	P-K	-0.77 [-0.09; 1.45]	-1.04 [-3.70; 0.93]	-1.17 $[-4.67; 1.07]$	-0.62 [-3.47; 1.17]	-0.40 [-1.97; 0.73]	-0.75 $[-3.32; 0.61]$	-0.16 $[-1.99; 1.31]$	-1.64 [-3.86; 1.49]	-1.85 [-4.07; 1.40]	-1.39 [-3.59; 1.52]
Gender	P-K	-0.37 [-0.33; 2.45] 0.27	0.35 [-1.18; 2.54] -0.07	-0.32 [-3.71; 2.80] -0.10	0.81 [-1.06; 3.10] -0.05	0.20 [-1.35; 1.39] 0.42	-0.35 [-1.89; 1.65] 0.38	0.60 $[-1.34; 2.32]$ 0.45	$egin{array}{c} 0.97 \\ [-1.19; 2.77] \\ 0.12 \end{array}$	0.79 $[-1.51; 3.33]$ 0.10	$\begin{bmatrix} 1.34 \\ [-1.38; 3.52] \\ 0.16 \end{bmatrix}$
Carbonhydrates, E%	fP-Pi	[0.21; 3.28]	[-1.87; 2.32]	[-1.87; 2.34]	[-1.82; 2.34]	[-1.05; 2.66]	[-1.13; 2.65]	[-1.04; 2.69]	[-2.02; 3.59]	[-2.10; 3.53]	[-1.98; 3.62]
Fat E%	P-K	-0.68 [-0.26; 3.60] 0.03	-0.71 [-4.74; 3.07] -0.04	-0.85 [-6.11; 3.03] -0.12	-0.49 [-3.53; 3.29] 0.07	-0.67 [-4.62; 4.02] 0.12	-0.95 [-5.00; 3.65] 0.07	-0.47 $[-4.42; 4.62]$ 0.20	-0.68 [-5.02; 2.63] -0.16	-0.96 [-5.88; 2.50] -0.24	-0.58 [-5.22; 2.87] -0.08
Water	P-K	[0.23; 2.11] 2.46	[-2.09; 0.97] 2.52	[-2.39; 1.00] 2.46	$\begin{bmatrix} -2.23; 1.14 \end{bmatrix}$ 2.77	[-0.44; 0.71] 2.74	[-0.53; 0.63] 2.52	[-0.58; 0.96] 3.06	[-2.92; 1.43] 3.20	[-3.02; 1.37] 2.88	[-2.75; 1.61] 3.39
Renavit	P-K	[2.45; 6.63]	[-4.12; 8.39]	[-4.28; 8.64]	[-4.03; 9.24]	[-2.38; 6.89]	[-2.23; 6.82]	[-2.24; 7.19]	[-2.46; 8.22]	[-3.27; 7.77]	[-2.35; 8.18]
Protein, g/kg	P-Alb	-3.36 [-1.96; 4.65] -0.21	-6.42 [-15.03; 4.12] -0.81	-7.96 [-15.10; 4.31] -1.56	-4.16 [-13.91; 5.61] 0.30	-3.61 [-13.13; 4.26] 0.65	-6.61 [-13.09; 3.76] -1.04	-1.58 $[-12.52; 6.91]$ 2.12	-2.80 [-17.04; 5.18] -0.32	-4.29 [-17.36; 5.47] -1.23	-1.43 [-18.18; 10.29] 0.97
Monounsaturated Fatty Acids, E%	P-Alb	[-1.41; 7.64]	[-5.32; 6.33]	[-7.19; 6.64]	[-5.38; 6.36]	[-5.21; 6.08]	[-6.26; 6.10]	[-5.80; 6.43]	[-5.46; 6.88]	[-6.28; 7.11]	[-5.46; 7.37]
Calsium	P-Alb	1.71 [2.37; 7.24]	1.20 [-2.27; 6.36] 1.82	0.47 $[-4.00; 5.89]$ 1.02	$\begin{bmatrix} 1.62 \\ [-2.66; 8.20] \\ 2.89 \end{bmatrix}$	-0.01 [-4.83; 3.66]	-0.41 [-5.41; 3.16] 1.02	0.71 $[-3.47; 4.53]$ 3.21	0.96 [-4.96; 6.27] 2.29	$\begin{bmatrix} 0.57 \\ -6.78; 6.68 \end{bmatrix}$ $\begin{bmatrix} 2.10 \end{bmatrix}$	1.18 [-5.96; 7.21]
Fat E%	P-Alb	1.30 [3.41; 12.51] 1.02	[-11.70; 12.55] 1.38	[-12.73; 12.42] 0.97	[-11.07; 13.62] 2.03	1.77 [-11.60; 12.42] 1.26	[-12.90; 12.69] 0.99	[-10.96; 12.70] 1.66	[-11.90; 13.25] 1.19	[-12.15; 13.13] 0.89	3.09 [-10.81; 13.83 1.40
Vitamin D	P-Alb	[1.80; 4.83]	[-1.70; 3.73]	[-3.84; 4.93]	[-1.37; 5.05]	[-0.58; 2.48]	[-1.99; 3.09]	[-0.63; 4.42]	[-2.02; 5.15]	[-3.11; 5.20]	[-2.86; 6.39]
Phosphorous	P-K	0.18 [0.06; 1.91] -2.20	-0.16 [-1.65; 1.54] -1.44	-0.37 [-2.92; 1.57] -1.63	0.08 $[-1.29; 2.18]$ -1.23	0.24 [-1.20; 1.60] -0.23	$\begin{bmatrix} 0.02 \\ [-2.11; 1.51] \\ -0.56 \end{bmatrix}$	0.60 $[-0.57; 2.58]$ 0.27	-0.15 [-2.42; 1.70] -1.41	-0.51 [-3.66; 1.78] -1.79	0.09 [-2.12; 2.07] -1.29
Hydroxycholecalc		-2.20 [-0.70; 3.33] -2.95	[-5.94; 3.29] -1.50	-1.63 [-6.11; 3.32] -1.87	-1.23 [-6.09; 4.08] -1.12	-0.23 [-1.55; 1.43] -3.06	-0.56 [-2.90; 1.45] -3.49	[-1.65; 3.95] -2.55	-1.41 [-5.15; 3.91] -1.91	[-5.03; 3.53] -2.16	-1.29 [-4.99; 4.80] -1.61
Polyunsaturated Fatty Acids, E%	P-Alb	[-3.20; 2.81]	[-5.03; 4.81]	[-5.58; 4.18]	[-5.05; 6.15]	[-5.82; 0.19]	[-5.85; -0.32]	[-5.83; 2.79]	[-4.94; 2.78]	[-6.19; 3.18]	[-4.83; 3.58]
Salt	P-Alb	7.19 $[-1.91; 37.18]$	1.87 [-8.54; 14.87]	1.48 [-9.11; 14.84]	$\begin{bmatrix} 2.14 \\ [-8.25; 14.92] \end{bmatrix}$	1.30 [-5.87; 7.79]	0.76 [-9.44; 7.59]	1.99 $[-3.85; 7.92]$	3.87 [-9.82; 27.21]	3.68 [-10.66; 27.11]	4.37 [-9.20; 27.28]
Energy, kcal/kg	P-K	-0.23 [-1.01; 5.76]	$\begin{bmatrix} 1.00 \\ [-2.34; 5.98] \end{bmatrix}$	0.80 $[-2.42; 4.79]$	$\begin{bmatrix} 1.17 \\ [-2.42; 5.21] \end{bmatrix}$	-0.53 [-2.72; 4.53]	-0.89 [-3.12; 2.80]	-0.35 [-2.86; 6.97]	-0.75 [-4.05; 5.44]	-0.96 $[-4.03; 4.68]$	-0.56 [-3.88; 6.43]
Natrium	P-K	[-0.62; 1.53]	-1.36 [-8.97; 1.74]	-1.67 $[-9.14; 1.61]$	-0.90 [-8.30; 1.95]	-0.57 [-1.57; 0.71]	-0.96 $[-1.88; 0.66]$	-0.23 $[-1.57; 0.96]$	-1.74 [-5.59; 1.06]	-2.18 [-6.16; 1.14]	-1.68 [-5.51; 1.18]
Saturated Fatty Acids, E%	P-Alb	-3.58 [-5.11; 5.14]	-2.69 [-7.00; 5.14]	-2.91 [-7.55; 4.83]	-2.38 [-6.77; 5.28]	-2.15 [-6.96; 2.74]	-2.72 [-8.62; 2.46]	[-6.70; 3.49]	-1.81 [-7.80; 9.35]	[-8.43; 9.87]	-1.35 $[-7.35; 9.49]$
Hydroxycholecalc	if €P ⊕Pi	0.27 [0.27; 2.94]	-0.16 [-1.67; 2.17]	-0.33 [-2.38; 2.31]	0.09 $[-1.58; 3.70]$	0.50 [-0.58; 1.66]	0.13 [-1.72; 1.81]	0.77 [-0.44; 1.84]	0.10 [-2.28; 1.77]	-0.17 [-3.07; 2.03]	0.28 [-2.39; 2.21]

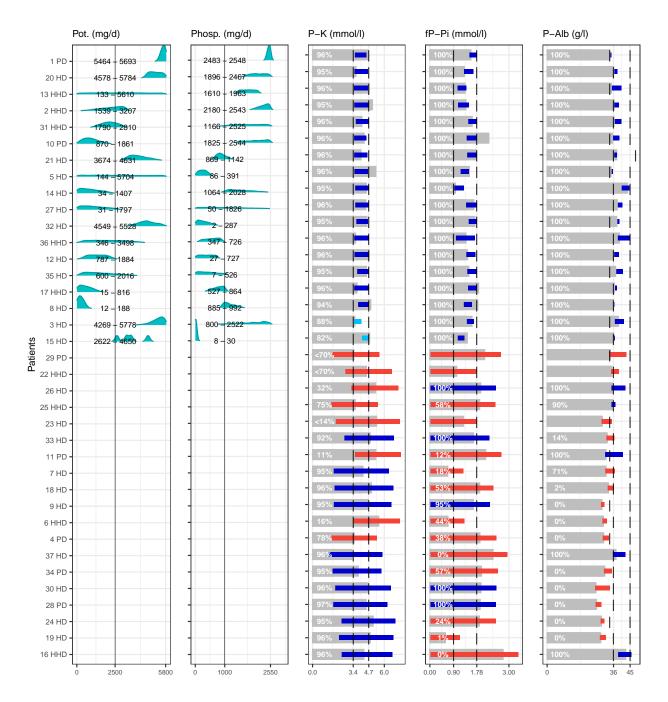
Supplementary Table S4 (continued)

			Home hemodialysis			Hospital hemodialysis			Peritoneal dialysis		
Nutrient	Conc.	General effect	avg	min	max	avg	min	max	avg	min	max
Protein, E%	P-Alb	2.61 [2.41; 9.62]	1.43 [-4.90; 5.88]	1.05 [-5.71; 6.62]	2.68 [-4.73; 7.60]	1.85 [-4.02; 6.45]	0.95 [-5.27; 5.72]	2.76 [-3.46; 8.24]	2.57 [-5.36; 10.19]	1.79 [-6.12; 8.54]	2.88 [-4.90; 10.60]
Fiber	fP-Pi	0.49 [0.10; 2.28]	0.12 [-0.61; 0.82]	0.04 [-0.75; 0.61]	0.16 $[-0.66; 0.78]$	-0.15 [-0.69; 0.51]	-0.26 [-0.86; 0.49]	-0.09 [-0.60; 0.55]	-0.11 [-0.73; 0.99]	-0.16 [-0.80; 0.85]	-0.07 [-0.80; 0.99]
Polyunsaturated Fatty Acids, E%	Р-К	-0.05 [0.00; 1.43]	-0.25 [-1.47; 0.73]	-0.35 $[-1.50; 0.77]$	-0.14 [-1.42; 1.10]	-0.09 [-0.93; 0.53]	-0.20 [-1.19; 0.57]	-0.01 [-0.97; 0.90]	$\begin{bmatrix} 0.02 \\ [-0.97; 1.06] \end{bmatrix}$	-0.05 [-0.98; 0.83]	$\begin{bmatrix} 0.07 \\ [-1.07; 1.09] \end{bmatrix}$
Monounsaturated Fatty Acids, E%	Р-К	$\begin{bmatrix} 1.62 \\ [1.27; 4.01] \end{bmatrix}$	$\begin{array}{c} {\bf 1.26} \\ [-1.07; 3.33] \end{array}$	$\begin{bmatrix} 1.06 \\ [-1.22; 2.63] \end{bmatrix}$	$\begin{bmatrix} 1.55 \\ [-0.94; 3.59] \end{bmatrix}$	$\begin{array}{c} \textbf{0.67} \\ [-0.81; 1.85] \end{array}$	$0.28 \\ [-1.62; 1.65]$	$0.92 \\ [-0.92; 2.24]$	$\begin{array}{c} {\bf 0.38} \\ [-1.28; 2.10] \end{array}$	-0.22 [$-2.35; 1.53$]	$0.47 \\ [-1.06; 2.53]$
Carbonhydrates, E%	Р-К	$\begin{bmatrix} 2.12 \\ [0.60; 10.33] \end{bmatrix}$	$\begin{array}{c} {\bf 0.01} \\ [-3.61; 3.31] \end{array}$	-0.50 [-3.96; 3.25]	$0.33 \\ [-3.62; 3.31]$	-0.09 [-3.12; 3.70]	-0.40 [-3.32; 3.78]	$0.24 \\ [-2.99; 3.84]$	-0.42 [-4.84; 3.11]	-0.80 [-5.05; 3.11]	-0.25 $[-4.96; 3.09]$
Phosphate binder med.	P-K	1.89 [1.25; 6.13]	$\begin{array}{c} {\bf 1.01} \\ [-2.11; 2.99] \end{array}$	-0.60 $[-4.01; 3.17]$	${2.01} \\ [-1.78; 5.02]$	0.58 [-2.20; 2.63]	-0.34 [-4.75; 2.67]	${2.14} \\ [-2.67; 6.54]$	0.85 $[-1.18; 3.46]$	-0.61 $[-5.61; 4.33]$	$1.70 \\ [-1.33; 4.36]$
Blood lipid medication	fP-Pi	-0.49 [-0.10; 0.73]	-0.16 [-2.09; 1.28]	-0.26 [-2.12; 1.30]	-0.07 [-2.08; 1.55]	-0.23 [-1.13; 0.54]	-0.44 $[-1.27; 0.51]$	-0.09 [-1.22; 0.67]	0.18 [-1.65; 1.80]	0.11 [-1.74; 1.82]	0.22 [-1.67; 1.98]
Protein, E%	fP-Pi	-0.27 $[-0.26; 1.07]$	0.06 $[-0.87; 0.70]$	-0.07 $[-0.96; 0.70]$	0.15 $[-0.86; 0.83]$	0.16 $[-0.43; 1.15]$	0.08 [-0.59; 1.19]	$0.33 \\ [-0.37; 1.21]$	0.11 [-0.75; 1.38]	0.02 [-1.01; 1.49]	0.19 $[-0.67; 1.46]$
Calsium	P-K	0.04 [0.18; 2.18] -0.05	-0.17 [-1.88; 2.04] -0.18	-0.48 [-2.60; 2.34] -0.53	0.24 $[-1.00; 2.30]$ 0.56	0.50 [-0.69; 1.75] 0.10	-0.16 [-1.44; 1.22] -0.35	0.84 $[-0.63; 2.88]$ 0.58	0.26 [-0.83; 2.27] -0.21	-0.22 [-1.53; 1.82] -0.36	0.63 $[-1.01; 2.61]$ 0.04
Phosphate binder med.	fP-Pi	[-0.23; 1.67]	[-1.40; 1.40]	[-2.78; 1.76]	[-1.48; 1.86]	[-1.26; 1.40]	[-1.78; 1.72]	[-1.56; 2.12]	[-1.34; 1.04]	[-1.53; 1.18]	[-1.88; 1.24]
Protein, g/kg	P-K	$ \begin{array}{c} 0.43 \\ [-0.26; 4.73] \\ 0.95 \end{array} $	-0.93 [-5.97; 2.43] 0.36	-1.03 [-6.08; 2.43] 0.12	-0.85 [-5.87; 2.44] 0.67	-0.01 [-5.03; 2.51] 0.55	-0.18 [-5.04; 2.62] 0.33	0.14 $[-4.87; 2.60]$ 0.79	0.42 [-2.78; 3.61] 0.06	0.29 $[-2.77; 3.55]$ -0.08	0.54 $[-2.82; 3.50]$ 0.23
Fat E% Monounsaturated	fP-Pi	[0.68; 5.36] -0.07	[-2.04; 3.66] - 0.04	[-2.17; 3.65] -0.15	[-2.21; 3.87] -0.04	[-1.09; 3.21] - 0.14	[-1.34; 3.28] -0.33	[-1.12; 3.23] 0.01	[-2.57; 2.91] - 0.08	[-2.51; 3.07] -0.08	[-2.59; 3.16] 0.03
Fatty Acids, E%	Ir-ri	[0.19; 1.09]	[-1.96; 1.01]	[-2.07; 1.06]	[-2.04; 1.05]	[-1.25; 0.73]	[-1.63; 0.76]	[-1.11; 0.97]	[-1.04; 1.19]	[-1.01; 1.28]	[-1.02; 1.46]
Saturated Fatty Acids, E%	fP-Pi	-1.13 [-0.33; 1.61]	-0.15 [-1.88; 1.22]	-0.20 [-1.95; 1.16]	-0.12 [-1.82; 1.30]	-0.14 [-1.02; 1.12]	-0.19 [-1.10; 1.09]	-0.08 [-1.00; 1.24]	-0.02 [-1.20; 1.72]	-0.03 $[-1.21; 1.64]$	0.03 $[-1.14; 2.00]$
Calsium	fP-Pi	-0.01 [-0.39; 2.45]	-0.18 [-0.94; 0.74]	-0.26 $[-0.91; 0.99]$	0.00 $[-0.94; 0.88]$	-0.20 [-0.64; 0.20]	-0.41 [-0.98; 0.18]	$\begin{bmatrix} 0.01 \\ [-0.63; 0.50] \end{bmatrix}$	-0.01 [-0.98; 1.08]	-0.04 [-1.09; 1.13]	0.18 [-0.95; 1.32]
Phosphorous	fP-Pi	0.02 [0.03; 2.03] -0.24	0.00 [-1.12; 1.54] -0.45	-0.12 [-1.35; 1.40] -0.66	0.09 $[-1.01; 1.56]$ -0.14	0.03 [-1.00; 0.78] 0.09	-0.05 [-1.15; 0.81] -0.17	$\begin{bmatrix} 0.13 \\ [-0.88; 0.97] \\ 0.22 \end{bmatrix}$	-0.12 [-1.60; 1.44] 0.64	-0.16 $[-1.49; 1.37]$ 0.60	-0.09 [-1.56; 1.47] 0.85
Diabetes medication	fP-Pi	[-0.31; 1.53]	$\left[-2.01; 1.01\right]$	[-2.46; 1.09]	[-1.85; 1.16]	[-0.73; 1.09]	[-1.06; 1.14]	[-0.87; 1.09]	[-1.26; 2.88] -2.77	[-1.32; 2.86]	[-1.13; 3.00]
Renavit	fP-Pi	$ \begin{array}{r} -3.72 \\ [-1.64; 2.92] \\ -0.05 \end{array} $	-1.90 [-10.81; 3.65] 0.13	-2.01 [-11.83; 3.68] 0.01	-1.70 [-9.90; 3.83] 0.25	-0.54 [-2.69; 2.10] -0.07	-0.66 [-2.90; 2.11] -0.18	-0.43 $[-2.12; 2.23]$ 0.15	[-14.84; 3.19] 0.17	-2.88 [-15.22; 3.15] 0.15	-2.71 [-14.52; 3.19] 0.27
Potassium Energy, kcal/kg	fP-Pi fP-Pi	[-0.22; 0.72] 0.20	[-0.65; 1.08] 0.30	[-0.81; 1.01] 0.21	[-0.66; 1.58] 0.43	[-0.58; 0.48] 0.63	[-0.81; 0.47] 0.53	[-0.45; 1.47] 0.77	[-0.46; 0.90] 0.48	[-0.63; 1.06] 0.42	[-0.39; 1.37] 0.57
Protein, g/kg	fP-Pi	[0.39; 2.00]	[-1.74; 1.79] - 0.55	[-1.83; 1.99] -0.61	[-1.63; 2.09] -0.49	[-1.09; 1.71] -0.60	[-1.25; 1.60] -0.75	-0.46	[-2.37; 2.65] - 0.77	[-2.55; 2.62] -0.88	[-2.27; 2.65]
Vitamin D	P-K	[-1.19; 2.13] -0.04 [-0.15; 0.89]	[-1.93; 1.48] -0.06 [-1.10; 0.72]	[-1.89; 1.52] -0.14 [-1.18; 0.49]	[-1.84; 1.58] 0.22 [-0.85; 1.15]	[-1.74; 1.19] -0.31 [-0.82; 0.19]	[-2.09; 1.13] -0.49 [-1.61; 0.19]	[-1.68; 1.19] -0.10 [-0.67; 0.57]	[-2.30; 1.62] -0.06 [-0.73; 0.60]	[-2.51; 1.56] -0.16 [-1.02; 0.53]	[-2.41; 1.70] 0.12 [-0.75; 0.80]
Fiber	P-K	0.46 [0.54; 2.53]	0.31 [-0.77; 1.04]	0.25 [-0.92; 1.07]	0.37 [-0.70; 1.08]	0.17 [-0.72; 1.26]	0.01 [-1.36; 0.94]	0.29 [-0.52; 1.84]	0.59 [-1.38; 1.93]	0.47 [-1.70; 1.81]	0.66 [-1.55; 2.12]
Potassium	P-K	0.02 [-0.15; 1.95]	-0.03 [-1.40; 1.53] 0.09	-0.25 [-1.91; 1.01] -0.09	$\begin{bmatrix} 0.01 \\ [-1.34; 1.30] \\ 0.20 \end{bmatrix}$	0.17 [-0.91; 0.83] 0.27	-0.17 [-1.11; 0.55] 0.16	0.40 [-1.05; 1.45]	0.00 [-1.09; 2.00] 0.61	-0.10 [-1.17; 1.81]	0.20 [-1.08; 1.67]
Saturated Fatty Acids, E%	P-K	0.44 [0.61; 2.10]	[-2.07; 1.52]	[-2.67; 1.49]	[-1.99; 1.60]	[-1.88; 1.67]	[-2.14; 1.74]	$ \begin{array}{c} 0.39 \\ [-1.71; 1.80] \end{array} $	[-1.16; 1.99]	0.54 $[-1.32; 2.00]$	0.64 [-1.20; 2.08]
Water	fP-Pi	-0.08 [0.19; 0.89]	0.16 [-0.49; 0.81]	0.04 [-0.61; 0.85]	$\begin{bmatrix} 0.24 \\ [-0.57; 1.22] \\ 0.19 \end{bmatrix}$	0.16 [-0.15; 0.58]	-0.05 [-0.54; 0.66]	0.28 [-0.23; 0.99]	0.12 [-1.01; 0.88]	0.04 [-1.21; 0.84]	0.26 [-1.00; 1.17]
Gender	fP-Pi	-0.10 [0.08; 1.79] -1.19	0.10 [-1.41; 1.42] -0.23	-0.05 [-1.73; 1.38] -0.27	[-1.40; 1.43] -0.15	-0.30 [-1.13; 0.78] -0.19	-0.50 [-2.01; 0.64] -0.26	-0.19 [-1.13; 1.14] -0.10	-0.58 [-1.89; 0.93] -0.08	-0.63 [-2.16; 1.00] -0.10	-0.51 [-2.02; 1.35] -0.04
Polyunsaturated Fatty Acids, E%	tP-Pi	[-0.21; 0.62]	[-1.36; 0.89]	[-1.47; 0.90]	[-1.24; 1.25]	[-0.59; 0.35]	[-0.87; 0.35]	[-0.63; 0.60]	[-0.88; 0.92]	[-0.93; 0.95]	[-0.88; 0.95]
Protein, E%	Р-К	0.45 [0.74; 2.36]	0.39 [-1.22; 1.84]	0.34 $[-1.25; 1.74]$ 0.08	0.52 $[-1.10; 2.38]$	-0.24 [-1.24; 1.60] 0.39	-0.37 [-1.46; 1.35]	-0.14 $[-1.17; 2.11]$ 0.50	-0.36 [-1.92; 2.03] 0.22	-0.46 [-1.78; 1.80]	-0.27 [-1.89; 2.14]
Natrium	fP-Pi	0.20 [0.58; 1.47]	0.13 [-1.71; 1.14]	[-1.82; 1.15]	0.26 [-1.64; 1.44]	[-0.52; 1.13]	0.30 [-0.66; 0.93]	[-0.48; 1.39]	[-1.50; 1.89]	0.15 [-1.63; 1.74]	0.27 [-1.53; 2.08]
Salt	P-K	0.26 [0.58; 2.59] -0.13	1.90 [-0.98; 8.85] -0.10	1.68 [-0.90; 8.76] -0.17	$\begin{bmatrix} 2.14 \\ [-0.92; 9.03] \\ 0.08 \end{bmatrix}$	0.42 [-0.61; 1.28] 0.08	0.19 $[-0.73; 1.37]$ -0.09	0.72 $[-0.51; 1.59]$ 0.29	0.81 $[-2.20; 4.45]$ 0.12	0.57 $[-2.43; 4.29]$ -0.03	$\begin{bmatrix} 1.04 \\ [-2.17; 4.50] \\ 0.22 \end{bmatrix}$
Vitamin D Salt	fP-Pi fP-Pi	[0.02; 0.36] -0.08	[-0.69; 0.32] -0.16	[-0.81; 0.30] -0.30	[-0.62; 0.73] -0.05	[-0.23; 0.38] -0.34	[-0.57; 0.43] -0.48	[-0.18; 0.67] -0.15	[-0.38; 0.71] - 0.26	[-0.51; 0.77] -0.42	[-0.50; 0.86] -0.17
Jan	11L 1	[-0.42; 1.70]	[-1.11; 1.58]	[-1.15; 1.53]	[-1.15; 1.57]	[-0.96; 0.47]	[-1.27; 0.50]	[-0.89; 0.51]	[-1.68; 1.38]	[-1.70; 1.47]	[-1.59; 1.52]

Supplementary Table S5: Table shows 20 effects that have highest variation between patients by comparing minimum and maximum of effect strength expected values.

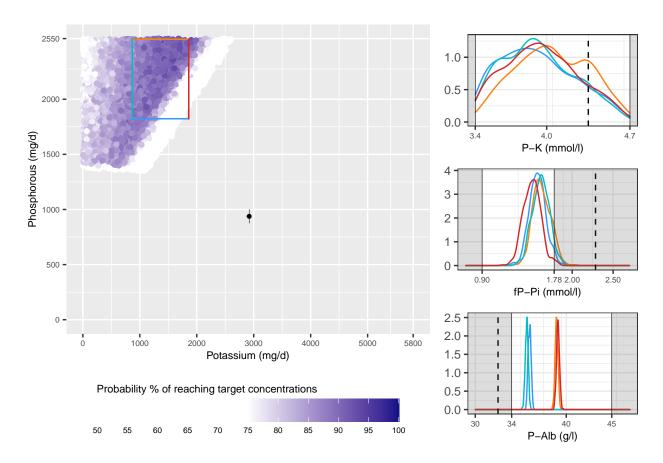
	Expected personal effect strength		
Effect	Min	Max	
Natrium -> P-Alb	-7.969	1.340	
$Gender \rightarrow P-Alb$	-3.392	4.308	
Protein, $g/kg \rightarrow P-Alb$	-7.963	-1.429	
Phosphate binder med> P-Alb	-4.279	1.383	
Renavit -> P-Alb	4.281	9.723	
Blood lipid medication -> P-Alb	-2.852	2.289	
Diabetes medication -> P-Alb	-2.992	1.735	
Phosphorous -> P-Alb	-2.263	1.795	
Potassium -> P-Alb	-2.196	1.849	
Hydroxycholecalciferol -> P-Alb	0.876	4.569	
Monounsaturated Fatty Acids, E% -> P-Alb	-1.559	2.121	
Salt -> P-Alb	0.765	4.372	
Energy, $kcal/kg -> P-Alb$	1.073	4.156	
Phosphate binder med> P-K	-0.607	2.144	
Carbon hydrates, E% -> P-Alb	-1.565	0.971	
Water -> P-Alb	-2.092	0.361	
Renavit -> fP-Pi	-2.875	-0.432	
Polyunsaturated Fatty Acids, E% -> P-Alb	-3.494	-1.117	
Fat E% \rightarrow P-Alb	1.021	3.213	
Energy, kcal/kg -> $P-K$	-0.960	1.165	

Overview of personal recommendations



Supplementary Figure S 5: The figure shows in two left-most panels personal recommendations of potassium and phosphorous intake $(\hat{Q}^{min} - \hat{Q}^{max})$ from Algorithm (1) with predictive distributions of \hat{Q} in the background. Each row gives a numeric label of the patient and the type of patient's dialysis treatment (HD = hospital hemodialysis, HHD = home hemodialysis, PD = peritoneal dialysis). Personal recommendations are given for those patients whose resulting plasma concentration levels could be predicted in either over 90% or 80% probability. Three right-most panels show the estimated concentrations that match the recommended intake. In these panels, grey bars indicate the estimated concentration without the effect of potassium and phosphorous intake, μ_{q0} . Blue bars indicate the range of concentration that is resulted by modifying potassium and phosphorous intake. It is required that these simulated concentrations stay within the personal target ranges denoted with vertical black lines. The light blue bar indicates satisfying this requirement in $P^{max} > 80\%$ confidence and dark blue $P^{max} > 90\%$ confidence. The best exact probabilities P^{max}_m are shown with percentage figures. Red bars indicate that even the best concentration estimation has $P^{max} < 80\%$ confidence and personal recommendations are not given for these patients. For these patients, the red and blue bars show the whole reachable ranges. The figure is plotted with ggplot2 package for R language (v 3.3.5, https://ggplot2.tidyverse.org)

Personal recommendation for a patient



Supplementary Figure S 6: Figure shows detailed intake recommendation for patient 10 from the previous recommendation table. The intake plot on the left shows the posterior samples of diet configurations that result concentrations of plasma potassium (P-K), fasting plasma phosphate (fP-Pi) and plasma albumin (P-Alb) to stay within their recommended limits. These levels are marked with vertical solid lines in the concentration panels. The black point in the middle of intake plot represents the patient's current potassium and phosphorous intake. Current concentrations matching this intake are shown with dashed vertical lines. Reported recommendation is shown with a rectangle that contains 95% of diet proposals that result recommended concentrations over 90% accuracy. Colouring of the rectangle sides match the concentration estimates in the right hand panels. The figure is plotted with ggplot2 package for R language (v 3.3.5, https://ggplot2.tidyverse.org).