Personalized potassium and phosphorus intake recommendations can be reasoned for end-stage renal failure patients by simulating with hierarchical Bayesian multivariate model

Supplementary Materials

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This notebook reproduces in detail the analysis of personal diet recommendations described in the main article. The notebook starts visualizing the collected raw data, prepares it for analysis and estimates personal reaction models with these data. The personal reaction models are combined with the estimation of the current personal diets for constructing personal graphical models. These personal models generate the levels of blood concentrations when a diet is given, they are used in simulating recommended personal diets for reaching predefined normal concentrations. Finally, these personal diet recommendations are compared for showing the divergence among the studied patients.

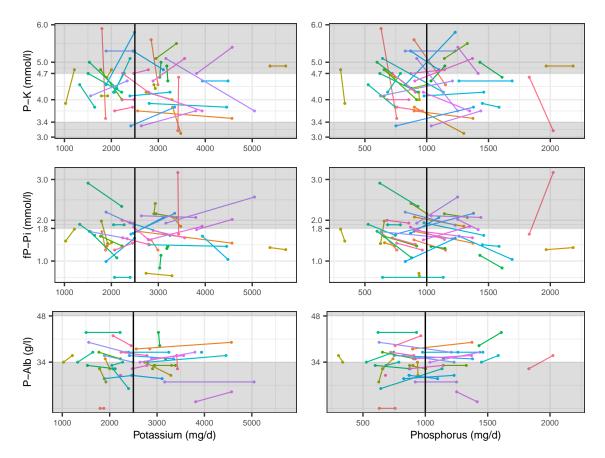
The notebook execution generates all the figures and tables that are included in the article, and produces also the referenced supplementary figures. The article is accompanied with a PDF rendetion of the notebook that shows all the supplementary figures and important parts of the program code so that the analysis can be followed in detail. The executable RMarkdown notebook with data can be found in a public Github repository of the corresponding author.

Dialysis patient data

The analyzed dataset consists of food records and laboratory measurements from end-stage renal patients in dialysis. Following nutrients are possible considered as predictors of concentrations. Note that we use energy-% of fats and protein as unit in our analysis. This is referred as Table 1 in the main article.

and also following personal details and medication are considered as predictors. This is referenced as Table 2 in the article.

Let us explore then how the intake of dietary potassium and phosphorus corresponds in data to plasma concentrations of potassium, phosphate and albumin



Supplementary Figure S 1: Figure shows the progress between two observations of plasma potassium (P-K), fasting plasma phosphate (fP-Pi) and plasma albumin (P-Alb) concentrations of the studied patients. White regions in the panels show the recommended concentration levels, P-K 3.4 - 4.7 mmol/l, fP-Pi < 1.8 mmol/l and P-Alb 34 - 48 g/l. Vertical black lines denote the commonly recommended maximum intakes of these nutrients. The goal is to find personal intake levels that keep the concentrations in recommended levels, if possible. The figure is plotted with ggplot2 package for R language (v 3.3.5, https://ggplot2.tidyverse.org).

Aim of this analysis is to find such personal levels of potassium and phosphorous intakes that keep all these concentrations in their normal levels marked with white regions, if possible.

Development of nutrition reaction model

In this work we construct personal generative models for concentrations that allow conditioning personal diet recommendations. Essential part of these models is the personal reactions to nutrients and other predictors. Simultaneous reactions on all considered concentrations are modeled as multivariate model that has all the concentrations are response variables.

For comparison, we estimate multivariate systems with and without cross-model covariance. With cross-model covariance estimated, the model corresponds to seemingly unrelated model system, and without the model is Bayesian network with separated local distributions. This simpler model is estimated first with only potassium and phosphorous concentrations as responses.

initial_graph <- mebn.fully_connected_bipartite_graph(datadesc_fat_epros)</pre>

In Bayesian network both responses were estimated separately. Next, we estimate a multivariate model where both distribution are estimated during single sampling. It does not factorize into separate distributions, but allows using more data.

Next we like to add plasma albumin concentration as a third constraint in the model, but unfortunately 8 of 37 patients have missing albumin measurements. From such a small dataset we don't want to remove any patients and so we predict the missing albumin levels and impute them to dataset.

For prediction, estimate the model without missing values in P-Alb. The rows with missing values are held out from the density estimation, but patients are kept in the model for estimating their parameters.

```
inputdata = dialysis,
targetdata = holdout_index,
predictor_columns = assumedpredictors_fat_epros,
assumed_targets = pk_fppi_palb_targets,
group_column = "potilas",
local_estimation = mebn.multivariate_sampling,
local_model_cache =
    "models/BLMM_gamma_qr_multivariate3/fat_epros_missing_palb",
stan_model_file = "mebn/v2/BLMM_gamma_qr_mv_cv.stan",
normalize_values = TRUE)
```

Personal data imputation models

Now we can create personal models for patients that have missing plasma albumin measurements. These models are then used for making personal predictions for replacing missing values.

Then we predict missing values with these data imputing models

```
# and use the data in this row to predict palb
  evidence <- rows_with_missing_palb[i, assumedpredictors_fat_epros$Name]</pre>
  posterior prediction <- mebn.personal prediction(reaction graph = personal graph,
                                   graph_dir = personal_model_dir,
                                   evidence = evidence,
                                   stan_model_file = "diet/posterior_prediction.stan")
  \# personal_predictions contains predictions multivariate predictions
  # P-K and fP-Pi are known, but P-Alb is missing
  posterior <- rstan::extract(posterior_prediction, par= "posterior[3]")</pre>
  # use predicted posterior mean for missing P-Alb value
  # - this is i:th NA value in dialysis
  predicted_palb <- mean(posterior$`posterior[3]`)</pre>
   \textit{\# rows in 'rows\_with\_missing\_palb' and 'original\_palb' are in same order } \\
  # so we can imput in the NA values at 'original_palb'
  for (m in 1:imput length)
      if (is.na(original_palb[m]))
          original_palb[m] <- predicted_palb</pre>
          break:
 }
}
dialysis2 <- dialysis
dialysis2$palb <- original_palb</pre>
saveRDS(dialysis2, "data/DIALYSIS_imputed_palb.rds")
```

With this data imputation we can estimate a cross-covariance model with three responses

```
pk_fppi_palb_targets <- datadesc_fat_epros[datadesc_fat_epros$Name %in% c('pk','fppi','palb'),]
initial_graph <- mebn.fully_connected_bipartite_graph(datadesc_fat_epros)</pre>
```

Finally, we consider also the effect of dialysis treatment type as new level of grouping in data. This allows us to estimate average effects of nutrition for each treatment type and then also personal effects within those treatments.

```
pk_fppi_palb_targets <- datadesc_fat_epros[datadesc_fat_epros$Name %in% c('pk','fppi','palb'),]
no_holdout <- rep(0, nrow(dialysis_imputed))</pre>
initial_graph <- mebn.fully_connected_bipartite_graph(datadesc_fat_epros)</pre>
dialysis_imputed <- readRDS("data/DIALYSIS_imputed_palb.rds")</pre>
# add the dialysis treatment type as a grouping factor
dialysis imputed$hoitoryhma <- as.factor(dialysis imputed$hoitomuoto)
# and sort the data by treatment/patient/observation
dialysis_imputed <- dialysis_imputed[order(dialysis_imputed$hoitoryhma,</pre>
                                            dialysis imputed$potilas, dialysis imputed$havainto),]
dialdiet_gamma_mv3_two_level <- mebn.bipartite_two_level_multivariate(</pre>
                                    reaction_graph = initial_graph,
                                    inputdata = dialysis_imputed,
                                    targetdata = no_holdout,
                                    predictor_columns = assumedpredictors_fat_epros,
                                    assumed_targets = pk_fppi_palb_targets,
                                    group_column = "hoitoryhma",
                                    subject_column = "potilas",
                                    local_estimation = mebn.two_level_multivariate_sampling,
                                    local_model_cache =
                                      "models/BLMM gamma mv cross/two levels",
                                    stan model file =
                                      "mebn/v2/BLMM_gamma_two_level_grouping.stan",
                                    normalize values = TRUE)
write.graph(dialdiet_gamma_mv3_two_level,
            "graphs/dialysis_gamma_two_level_grouping.graphml", "graphml")
```

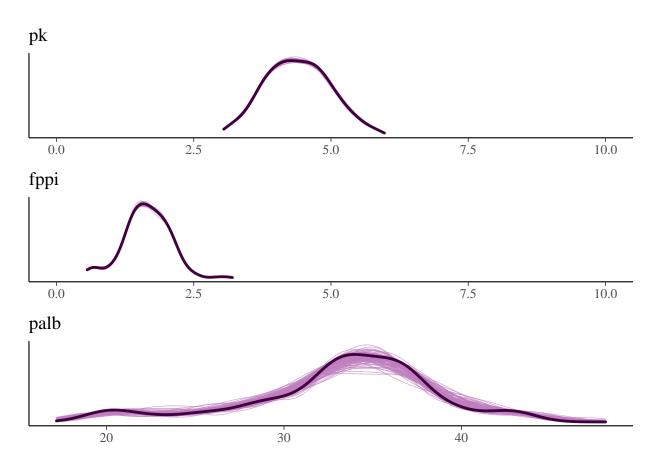
Model analysis

Here we evaluate the model's ability to repeat the measured observations with normalized root mean square error (NRMSE) and compare how adding the dialysis treatment as an explicit hierarchical layer in the model affects this error. We also assess the model's performance with visual posterior predictive check by comparing samples from the model with measured values. This would give away possible bias in the model.

Supplementary Table S 1: Supplementary Table S1: Comparison of model candidates. Personal graphical models with different reaction model candidates are evaluated with NRMSE for each modeled concentration and average model error.

	NRMSE						
Reaction model	P-K	fP-Pi	P-Alb	average error			
mv3_cross_two_levels mv3_cross_single_level			0.002 0.103	0.003 0.078			

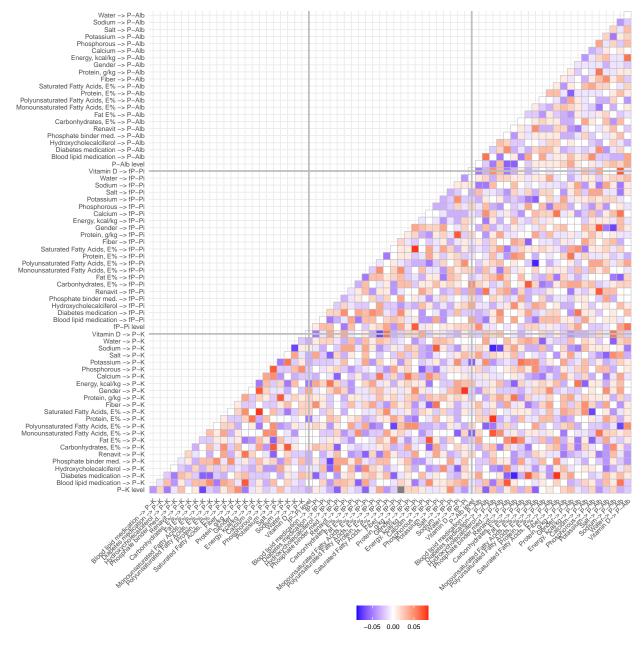
```
## [1] "pk"
## [1] "fppi"
## [1] "palb"
```



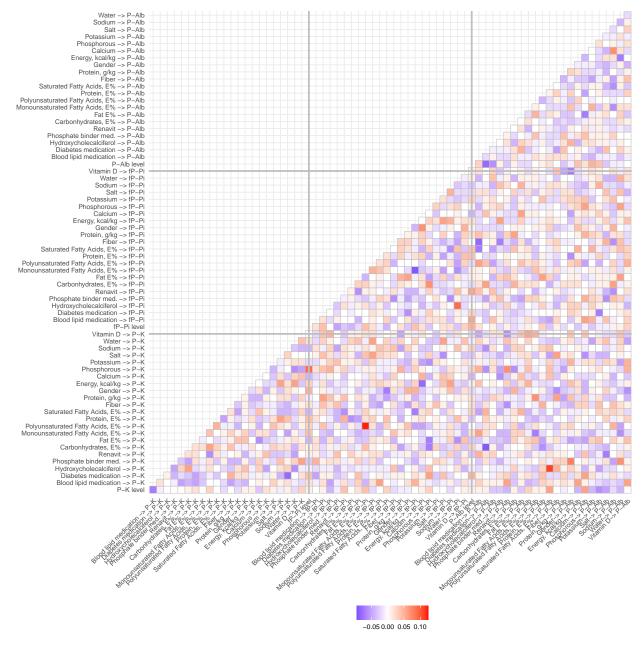
Supplementary Figure S 2: Posterior predictive check of the model where three concentrations and their parameters are stacked into one univariate model for estimating cross-model correlations.

Then we drill into the estimated correlation matrices of effects. The model estimates how much the effects of nutrients vary from general effects in dialysis treatment level and further how the effects vary personally within a treatment. These correlation plots show how the effects are correlated.

Scale for 'fill' is already present. Adding another scale for 'fill', which ## will replace the existing scale.



Supplementary Figure S 3: Correlation plot of matrix C_g that includes the estimated within-model and cross-model correlations in level of dialysis treatment



Supplementary Figure S 4: Correlation plot of matrix C_b that includes the estimated within-model and cross-model correlations of personal effects

Supplementary Table S 2: Table shows 40 highest positive or negative correlations between treatment effects of potassium and phosphorous with other treatment effects. This structure of correlations is used in estimating the personal effects based on personal intake and matching concentrations.

Treatment-level effects of nu		
Effect 1	Effect 2	Correlation
Renavit -> fP-Pi	Potassium-> P-Alb	0.074
Gender -> fP-Pi	Potassium-> P-Alb	0.071
Sodium -> P-K	Potassium -> fP-Pi	0.065
Protein, g/kg -> P-Alb	Potassium-> P-Alb	0.063
Sodium -> P-K	Potassium -> P-K	0.058
Calcium -> P-K	Potassium -> P-K	0.053
Monounsaturated Fatty Acids, E% -> P-K	Potassium -> P-K	0.052
Polyunsaturated Fatty Acids, E% -> P-Alb	Potassium -> P-K	0.050
Diabetes medication -> P-Alb	Potassium -> P-K	0.047
Vitamin D -> fP-Pi	Potassium-> P-Alb	0.045
Blood lipid medication -> fP-Pi	Potassium -> fP-Pi	0.044
Phosphorous -> P-Alb	Potassium-> P-Alb	0.043
Polyunsaturated Fatty Acids, E% -> fP-Pi	Potassium -> P-K	-0.042
Salt -> P-K	Potassium-> P-Alb	-0.043
Hydroxycholecalciferol -> P-K	Potassium -> P-K	-0.045
Sodium -> fP-Pi Sodium -> P-Alb Monounsaturated Fatty Acids, E% -> P-Alb P-Alb level Polyunsaturated Fatty Acids, E% -> P-Alb	Potassium-> P-Alb Potassium-> P-Alb Potassium-> P-K Potassium -> P-F	-0.048 -0.049 -0.051 -0.056 -0.059
Potassium -> P-K	Phosphorous -> P-K	0.066
Blood lipid medication -> P-K	Phosphorous -> fP-Pi	0.054
Calcium -> P-K	Phosphorous -> fP-Pi	0.051
Monounsaturated Fatty Acids, E% -> P-K	Phosphorous -> P-K	0.050
Protein, E% -> fP-Pi	Phosphorous -> fP-Pi	0.044
Salt -> fP-Pi Polyunsaturated Fatty Acids, E% -> fP-Pi Calcium -> P-K Saturated Fatty Acids, E% -> fP-Pi Hydroxycholecalciferol -> P-K	Phosphorous-> P-Alb Phosphorous-> P-K Phosphorous -> fP-Pi Phosphorous -> fP-Pi	0.043 0.042 0.038 0.036 -0.037
Saturated Fatty Acids, E% -> fP-Pi	Phosphorous -> P-K	-0.037
Carbonhydrates, E% -> P-K	Phosphorous -> P-K	-0.039
Phosphorous -> fP-Pi	Phosphorous-> P-Alb	-0.039
Salt -> P-Alb	Phosphorous -> fP-Pi	-0.039
Carbonhydrates, E% -> fP-Pi	Phosphorous -> P-K	-0.040
Phosphate binder med> P-Alb	Phosphorous -> fP-Pi	-0.042
Polyunsaturated Fatty Acids, E% -> fP-Pi	Phosphorous -> fP-Pi	-0.048
Saturated Fatty Acids, E% -> P-Alb	Phosphorous -> fP-Pi	-0.053
Carbonhydrates, E% -> P-K	Phosphorous -> fP-Pi	-0.060
Calcium -> fP-Pi	Phosphorous -> P-K	-0.063

Supplementary Table S 3: Table shows 40 highest positive or negative correlations between personal effects of potassium and phosphorous with other personal effects. This structure of correlations is used in estimating the personal effects based on personal intake and matching concentrations.

Personal effects of nutries		
Effect 1	Effect 2	Correlation
Sodium -> fP-Pi Gender -> P-Alb Fiber -> P-K Polyunsaturated Fatty Acids, E% -> P-K P-Alb level	Potassium-> P-Alb Potassium -> P-K Potassium -> fP-Pi Potassium -> P-K Potassium-> P-Alb	0.049 0.046 0.044 0.043 0.041
Sodium -> P-Alb Blood lipid medication -> P-K Salt -> P-Alb P-Alb level Saturated Fatty Acids, E% -> P-K	Potassium -> fP-Pi Potassium -> P-K Potassium -> P-K Potassium -> fP-Pi Potassium-> P-Alb	0.037 0.035 0.034 0.032 0.031
Water -> P-K Water -> fP-Pi Hydroxycholecalciferol -> fP-Pi Monounsaturated Fatty Acids, E% -> P-K Phosphorous -> P-K	Potassium -> fP-Pi Potassium -> fP-Pi Potassium -> fP-Pi Potassium -> P-K Potassium -> P-K	-0.030 -0.030 -0.031 -0.033 -0.035
Salt -> P-K Diabetes medication -> P-Alb Water -> P-Alb Calcium -> fP-Pi Phosphorous -> fP-Pi	Potassium-> P-Alb Potassium-> P-K Potassium -> P-K Potassium -> P-K Potassium -> P-K	-0.040 -0.040 -0.046 -0.051 -0.058
fP-Pi level Renavit -> P-Alb Diabetes medication -> P-K Hydroxycholecalciferol -> fP-Pi Saturated Fatty Acids, E% -> fP-Pi	Phosphorous -> P-K Phosphorous -> P-K Phosphorous -> fP-Pi Phosphorous -> P-K Phosphorous-> P-Alb	0.088 0.070 0.056 0.053 0.051
$\label{eq:Vitamin D -> P-Alb} $$\operatorname{Protein, g/kg -> fP-Pi}$$ Hydroxycholecalciferol -> P-K $$ Diabetes medication -> fP-Pi $$ Monounsaturated Fatty Acids, E% -> P-Alb $$$	Phosphorous -> P-K Phosphorous -> P-K Phosphorous -> fP-Pi Phosphorous -> P-K Phosphorous -> P-K	0.051 0.049 0.041 0.039 0.036
P-K level Blood lipid medication -> P-Alb Monounsaturated Fatty Acids, E% -> P-K Calcium -> P-K Hydroxycholecalciferol -> P-K	Phosphorous-> P-Alb Phosphorous-> P-Alb Phosphorous-> P-Alb Phosphorous -> fP-Pi Phosphorous -> P-K	-0.037 -0.037 -0.039 -0.044 -0.050
Fiber -> P-Alb Fat E% -> fP-Pi Water -> P-K Diabetes medication -> P-Alb Carbonhydrates, E% -> P-K	Phosphorous-> P-Alb Phosphorous -> fP-Pi Phosphorous -> P-K Phosphorous -> P-K Phosphorous -> fP-Pi	-0.051 -0.053 -0.055 -0.058 -0.069

Overview of nutritional effects

Following tables include all the estimated nutrition effects in general, dialysis treatment and personal levels.

Supplementary Table S4: Nutrition effect magnitudes from nutrients and other modeled features $(j=1,\ldots,22)$ to blood concentrations $(i=1,\ldots,3)$ for analyzed patients $(p=1,\ldots,37)$ in all three additive levels of the model. General effects $(\hat{\beta}_{ij})$ are shown to vary between patients in home hemodialysis, hospital hemodialysis, and peritoneal dialysis. First column of each dialysis type (avg) shows typical effect of the treatment $(\hat{\beta}_{ij}+\hat{g}_{ijk},k=1,\ldots,3)$ that can further vary personally. Minimum and maximum of these personal effects are shown within each treatment $(\hat{\beta}_{ij}+\hat{g}_{ijk}+\hat{b}_{ijp})$. The table is sorted in decreasing order of between-treatment variation $(\hat{\sigma}_g)$ and all the estimates include their 90%-credible intervals.

			Home hemodialysis			Hospital hemodialysis			Peritoneal dialysis		
Nutrient	Conc.	General effect	avg	min	max	avg	min	max	avg	min	max
Water Blood lipid	P-Alb	-2.04, 8.12 [-2.18; 2.97] 0.36, 0.84	-2.07 [-5.76; 1.76] 1.25	-2.60 [-8.07; 2.01] 0.24	-2.06 [-6.13; 2.47] 1.97	-0.23 [-3.21; 2.52] 0.14	-0.60 [-4.28; 2.84] -1.17	$0.11 \\ [-3.60; 3.77] \\ 1.19$	-1.19 [-5.93; 4.22] 1.14	-1.53 [-6.39; 4.00] 0.60	-1.12 [-5.86; 4.42] 1.81
medication		[0.16; 7.76] 0.50, -4.96	[-6.00; 10.22] -0.42	[-8.77; 11.01] -0.52	[-6.60; 12.07] -0.19	[-5.39; 5.61] -0.51	[-7.39; 5.64] -0.82	[-4.35; 6.96] -0.25	[-5.92; 10.13] -0.94	[-8.54; 9.56] -1.08	[-5.82; 11.07] -0.83
Hydroxycholecalci		[0.73; 3.68] -0.08, -1.43	[-5.08; 2.69] 1.85	[-5.31; 2.40] 1.22	[-5.07; 2.73] 2.25	[-2.17; 1.19] 0.88	[-2.69; 1.19] -0.32	[-2.28; 2.02] 1.59	[-3.42; 1.72] 1.64	[-3.85; 1.76] 2.03	[-3.48; 1.84] 2.60
Calcium	P-Alb P-Alb	[0.73; 6.03] 1.22, 2.89	[-2.93; 7.46] 2.23	[-3.36; 6.27] 2.00	[-3.61; 9.68] 2.80	[-3.47; 4.95] -0.87	[-5.36; 4.17] -1.39	[-3.38; 6.13] -0.28	[-2.90; 6.84] -3.02	[-3.76; 8.83] -3.28	[-3.21; 11.67] -2.60
Sodium		[0.87; 15.01] 1.60, 5.26	[-5.69; 12.83] 3.76	[-6.13; 11.84] 3.28	[-5.80; 15.93] 4.52	[-6.51; 5.45] 1.82	[-7.65; 5.06] 1.27	[-6.33; 7.10] 2.27	[-13.00; 7.48] -0.39	[-13.36; 7.35] -0.81	[-12.82; 8.02] -0.31
Salt	P-Alb	[2.14; 10.81] 1.67, 3.65	[-7.68; 12.53] 0.36	[-8.23; 11.96] -0.53	[-6.23; 12.73] 1.69	[-3.68; 6.93] 2.73	[-4.49; 6.56] 1.43	[-4.09; 9.07] 4.13	[-11.05; 8.80] 1.64	[-12.25; 8.04] 0.77	[-11.56; 8.59] 2.73
Gender	P-Alb	[1.42; 10.14] -2.78, -3.39	[-6.76; 6.92] -2.68	[-11.15; 7.42] -4.26	[-8.20; 10.28] -1.59	[-3.79; 9.68] -1.95	[-7.72; 9.22] -4.25	[-3.80; 11.67] -0.96	[-7.19; 9.96] -0.37	[-11.13; 10.90] -1.32	[-7.01; 13.42] 0.84
Phosphate binder med.	P-Alb	[-2.94; 4.87] 1.60, -8.89	[-10.50; 7.83] -0.40	[-18.77; 8.61] -1.39	[-9.86; 8.98] 0.69	[-9.93; 6.69] -1.40	[-16.99; 7.20] -2.93	[-11.15; 10.81] -0.18	[-8.93; 8.19] 1.06	[-10.67; 7.77] -0.18	[-10.26; 12.01 2.15
Ge7 7 G	P-Alb	[1.83; 15.39] 1.29, 10.10	[-12.86; 13.00] 2.67	[-13.20; 11.42] 2.28	[-12.25; 15.89] 3.71	[-12.93; 9.31] 1.80	[-14.33; 8.17] 0.91	[-12.79; 11.23] 2.33	[-11.93; 16.56] 0.82	[-13.30; 15.81] 0.16	[-12.02; 18.26 1.33
Carbonhydrates, E%	P-Alb	[1.56; 15.35]	[-13.38; 18.00]	[-13.04; 17.08]	[-11.99; 18.43]	[-13.38; 15.62]	[-15.21; 15.17]	[-11.97; 15.69]	[-15.89; 15.37]	[-16.99; 15.88]	[-15.87; 15.52
Monounsaturated Fatty Acids, E%	P-Alb	1.81, 16.22 [1.07; 13.45]	2.82 [-3.72; 12.69]	$\begin{bmatrix} 1.80 \\ [-5.70; 12.61] \end{bmatrix}$	$\begin{bmatrix} 3.92 \\ [-3.14; 13.42] \end{bmatrix}$	$\begin{bmatrix} \textbf{1.39} \\ [-4.01; 6.82] \end{bmatrix}$	$\begin{bmatrix} 0.71 \\ -5.18; 6.70 \end{bmatrix}$	[-3.10; 7.39]	$\begin{array}{c} {\bf 0.38} \\ [-7.41; 8.35] \end{array}$	-0.65 $[-9.54; 8.54]$	0.87 [-6.41; 8.64]
Saturated Fatty Acids, E%	P-Alb	-2.58, 7.16 [-2.40; 4.58]	-3.39 [-10.30; 3.85]	-4.07 [-11.26; 3.42]	-2.80 [-9.88; 5.06]	-2.23 [-9.00; 4.21]	-2.80 [-9.46; 4.27]	-1.17 $[-7.44; 4.97]$	-2.19 [-9.54; 5.17]	-2.48 [-9.24; 5.09]	$^{-1.63}$ $[-9.61; 5.69]$
Hydroxycholecalci	f ₽∙A lb	1.71, 5.40 [1.49; 10.13]	2.12 [-5.96; 12.13]	$\begin{bmatrix} 1.61 \\ [-6.54; 10.42] \end{bmatrix}$	3.09 $[-5.98; 13.35]$	0.90 [-5.30; 7.19]	0.54 $[-6.56; 8.47]$	$\begin{bmatrix} 1.68 \\ [-6.08; 9.36] \end{bmatrix}$	3.16 [-6.04; 13.07]	$\begin{bmatrix} 2.24 \\ [-7.66; 12.55] \end{bmatrix}$	3.47 $[-6.70; 13.94]$
Polyunsaturated Fatty Acids, E%	P-Alb	-0.93, 2.93 [-1.37; 5.86]	-1.21 [-5.89; 3.58]	[-6.40; 4.03]	-0.89 [-5.79; 4.35]	-2.05 [-5.86; 1.40]	[-6.01; 1.27]	[-5.96; 2.41]	-1.17 [-5.52; 3.44]	-1.27 $[-6.31; 3.49]$	-0.92 [-5.68; 3.78]
Potassium	P-Alb	-3.14, 1.90 [-1.47; 4.12]	-3.89 [-9.99; 1.30]	-5.04 [-12.20; 0.79]	-3.63 [-9.67; 2.06]	-1.06 [-4.53; 1.96]	-1.97 $[-8.76; 2.01]$	0.34 $[-3.64; 3.96]$	-0.24 [-5.53; 5.54]	[-7.02] [-7.03; 5.17]	0.27 $[-5.92; 8.05]$
Renavit	P-Alb	10.04, 18.65 [11.10; 24.48]	11.73 [-8.72; 25.68]	10.55 $[-8.97; 24.74]$	12.77 $[-7.93; 28.05]$	9.33 [-9.77; 24.03]	7.75 $[-10.19; 22.86]$	10.62 [-10.79; 25.61]	8.25 [-12.70; 22.49]	7.28 [-12.78; 21.69]	9.12 [-12.99; 23.78
Fat E%	P-Alb	3.19, -14.46 [3.56; 19.59]	2.32 [-16.46; 20.22]	1.52 [-17.42; 20.12]	3.00 [-15.81; 20.48]	3.40 [-12.94; 18.61]	2.52 [-15.43; 17.92]	4.14 [-12.29; 19.78]	3.50 [-14.06; 19.88]	2.88 [-14.63; 19.85]	3.95 [-14.63; 21.22
Phosphorous	P-Alb	-0.19, 1.31 [-0.07; 6.56]	-2.10 [-10.73; 5.28]	-3.09 [-12.68; 4.94]	-1.87 [-12.44; 7.81]	0.27 [-5.57; 5.95]	-0.41 [-6.77; 6.08]	1.73 [-4.98; 8.63]	0.80 [-7.31; 8.48]	0.10 [-8.68; 8.11]	1.22 [-6.42; 8.81]
Protein, g/kg	P-Alb	0.33, 5.63 [-0.24; 13.11] 1.60, -0.03	-1.35 [-16.07; 11.86] 1.55	-2.72 [-17.16; 10.61] 0.79	-0.19 [-15.66; 14.04] 2.39	-0.28 [-11.68; 11.80] 0.79	-0.95 [-12.82; 11.39]	0.98 $[-11.00; 15.10]$ 1.45	1.09 [-13.08; 14.12] 1.50	0.74 [-12.95; 13.72] 1.24	1.62 [-12.93; 15.03 2.22
Vitamin D	P-Alb	[1.61; 4.01]	[-1.01; 4.27]	[-3.52; 4.84]	[-0.82; 6.41]	[-1.25; 2.87]	[-3.45; 3.32]	[-1.76; 4.78]	[-1.49; 4.58]	[-2.88; 5.29]	[-1.24; 6.60]
Fiber	P-Alb	1.19, 0.44 [1.07; 7.55] 0.67, -0.62	$\begin{bmatrix} 1.43 \\ [-2.36; 5.60] \\ 0.45 \end{bmatrix}$	1.00 [-3.40; 6.23] -0.22	$\begin{bmatrix} 2.02 \\ [-2.56; 7.51] \\ 1.58 \end{bmatrix}$	1.34 [-1.91; 4.70] -0.12	0.70 $[-3.35; 4.61]$ -0.98	$\begin{bmatrix} 2.01 \\ [-2.06; 6.49] \\ 1.55 \end{bmatrix}$	$egin{array}{c} {\bf 1.60} \\ [-3.85; 6.61] \\ {\bf 0.49} \end{array}$	$\begin{bmatrix} 1.28 \\ [-4.24; 6.85] \\ 0.03 \end{bmatrix}$	$\begin{bmatrix} 1.92 \\ [-4.02; 7.59] \\ 1.40 \end{bmatrix}$
Diabetes medication	P-Alb	[0.79; 8.48]	[-6.07; 8.60]	[-8.31; 8.33]	$\left[-5.59; 9.25\right]$	[-6.22; 5.63]	[-7.54; 5.88]	[-6.13; 11.84]	[-7.22; 8.87]	$\left[-9.63; 9.68\right]$	[-8.00; 11.06]
Phosphate binder med.	P-K	0.28, 0.30 [0.16; 2.75]	0.25 $[-1.83; 2.88]$	-0.21 [-2.39; 2.53]	0.61 [-2.15; 3.88]	$\begin{bmatrix} 0.40 \\ [-1.23; 2.46] \end{bmatrix}$	0.04 $[-2.01; 2.50]$	0.68 $[-1.49; 3.63]$	0.26 $[-1.45; 2.40]$	-0.14 $[-2.83; 2.70]$	0.70 $[-1.44; 3.12]$
Phosphate binder med.	fP-Pi	0.50, 1.04 [0.17; 2.94]	0.61 $[-0.97; 2.71]$	0.33 [-2.11; 2.69]	0.82 [-1.44; 3.28]	0.41 [-0.90; 2.00]	0.15 $[-1.86; 1.99]$	0.73 $[-1.34; 3.02]$	0.12 [-1.71; 1.81]	-0.05 $[-2.23; 1.87]$	0.18 [-1.91; 2.04]
Protein, E%	P-Alb	0.64, -8.20 [0.79; 7.41]	2.08 [-4.84; 8.78]	1.70 $[-5.21; 8.26]$	2.67 $[-4.80; 10.24]$	1.72 $[-5.00; 8.28]$	$\begin{bmatrix} 1.17 \\ [-5.17; 7.86] \end{bmatrix}$	2.40 [-5.78; 9.59]	1.27 $[-5.70; 8.44]$	0.88 $[-7.16; 8.59]$	1.78 [-5.68; 8.87]
Protein, g/kg	P-K	-0.22, 2.90 [-0.41; 2.74]	0.09 $[-2.42; 2.57]$	-0.06 [-2.63; 2.54]	0.21 [-3.09; 2.96]	0.03 [-2.50; 2.41]	-0.22 [-3.16; 2.65]	0.18 [-2.37; 2.65]	-0.33 [-3.63; 2.99]	-0.36 [-3.95; 3.03]	-0.25 [-3.63; 3.12]
Carbonhydrates, E%	P-K	1.05, 2.36 [1.01; 4.69]	1.26 [-2.36; 4.61]	$\begin{bmatrix} 1.12 \\ [-2.64; 4.81] \end{bmatrix}$	$\begin{bmatrix} 1.32 \\ [-2.46; 4.82] \end{bmatrix}$	0.85 [-2.16; 3.43]	0.67 $[-2.37; 3.40]$	0.93 $[-2.40; 3.47]$	0.74 $[-2.67; 4.07]$	0.68 $[-2.99; 4.04]$	0.83 [-2.73; 4.47]
Calcium	P-K	-0.09, -0.03 [-0.18; 1.54]	-0.46 [-2.59; 0.97]	-0.63 [-3.83; 1.03]	-0.36 [-2.93; 1.41]	0.01 [-0.94; 1.17]	-0.15 [-1.92; 1.29]	0.38 [-0.76; 2.19]	-0.13 [-1.62; 1.29]	-0.37 [-2.41; 1.41]	0.05 [-1.49; 1.56]
Energy, kcal/kg	P-K	0.30, -2.52 [0.03; 4.98]	-0.19 [-2.92; 2.96]	-0.30 [-3.37; 2.87]	-0.11 [-2.54; 2.94]	-0.14 [-2.52; 2.41]	-0.24 [-2.71; 2.37]	-0.09 [-2.64; 2.53]	0.29 [-3.70; 4.70]	0.17 [-3.81; 4.57]	0.43 [-3.70; 4.95]
Salt	P-K	0.11, 1.99 [0.12; 2.50]	0.93 $[-1.37; 2.94]$	0.74 $[-1.96; 2.72]$	1.09 [-1.35; 3.42]	0.18 [-0.79; 1.10]	-0.09 [-2.57; 1.23]	0.38 [-0.64; 1.41]	-0.24 [-2.89; 1.63]	-0.50 [-3.94; 1.64]	-0.20 [-3.15; 1.68]
Gender	P-K	-0.04, 0.08 [0.06; 2.63]	0.41 [-1.36; 2.47]	0.35 [-1.54; 2.50]	0.57 [-1.36; 2.75]	0.26 [-1.17; 1.78]	0.07 [-1.57; 1.95]	0.39 [-1.40; 2.49]	0.92 [-1.97; 4.50]	0.76 [-2.39; 4.48]	1.07 [-1.90; 4.28]
Blood lipid medication	P-K	-0.65, 0.41 [-0.60; 1.82]	0.11 [-2.42; 4.45]	-0.21 [-3.88; 4.27]	0.36 [-2.46; 5.41]	-0.32 [-1.68; 0.98]	-0.61 [-2.45; 0.86]	0.10 [-1.30; 1.86]	-0.55 [-3.45; 1.73]	-0.96 [-5.15; 1.91]	-0.23 [-3.25; 3.33]

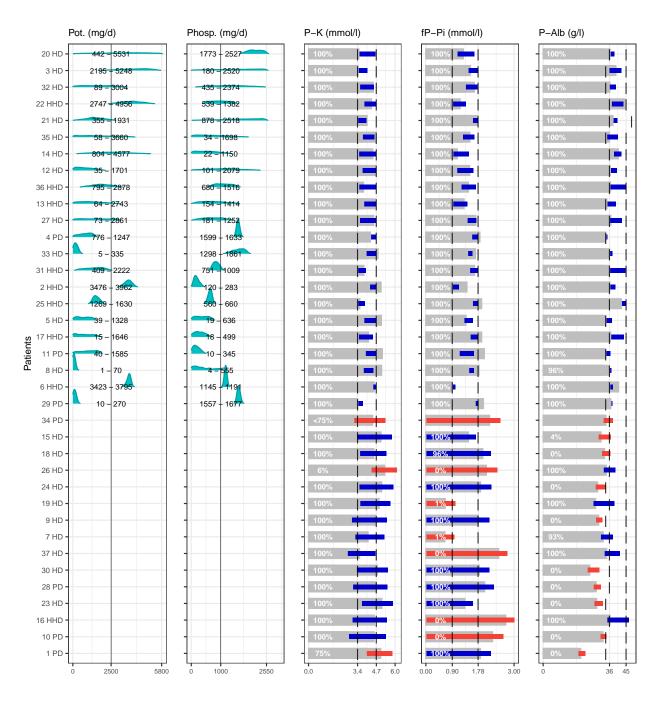
Supplementary Table S4 (continued)

			Home hemodialysis			Hospital hemodialysis			Peritoneal dialysis		
Nutrient	Conc.	General effect	avg	\mathbf{min}	max	avg	$_{ m min}$	max	avg	$_{ m min}$	max
Carbonhydrates,	fP-Pi	0.29, -1.43 [0.27; 2.87]	0.00 [-1.88; 1.73]	-0.07 [-1.88; 1.68]	0.03 [-1.82; 1.79]	0.16 [-1.40; 1.58]	0.08 [-1.66; 1.53]	0.27 [-1.08; 1.59]	0.06 [-1.90; 1.87]	0.01 [-1.89; 1.85]	0.08 [-1.99; 1.97
E% Monounsaturated Fatty Acids,	P-K	0.43, 0.61 [0.27; 3.02]	0.76 [-0.85; 3.37]	$0.72 \\ [-0.93; 3.46]$	$0.93 \\ [-0.87; 3.74]$	0.52 [-0.75; 2.02]	0.28 [-1.18; 1.77]	0.66 [-0.96; 3.02]	0.58 [-1.48; 2.81]	0.45 [-1.80; 2.80]	0.72 [-1.20; 2.68]
E% Sodium	fP-Pi	0.19, 0.01	0.63	0.57	0.70	0.12	0.05	0.20	0.41	0.36	0.47
Sodium	P-K	[0.16; 1.93] -0.15, -0.43	[-0.91; 3.46] -0.06	[-0.85; 3.26] -0.15	[-0.86; 3.47] -0.02	[-0.65; 0.72] -0.25	[-0.76; 0.68] -0.40	[-0.57; 0.85] -0.05	[-1.65; 3.99] - 0.54	[-1.60; 3.80] -0.60	[-1.68; 4.15 -0.39
Potassium	P-K	[-0.29; 2.35] -0.46, 0.05	[-1.88; 2.31] -0.06	[-1.98; 2.23] -0.32	[-1.88; 2.32] 0.14	[-1.74; 1.63] 0.14	[-1.86; 1.45] -0.11	[-1.76; 2.26] 0.50	[-2.64; 2.16] -0.21	[-2.74; 2.22] -0.51	$[-2.55; 2.47 \\ 0.16$
		[-0.13; 2.02] 0.20, 1.47	[-1.48; 1.55] 0.19	[-2.14; 1.32] 0.04	[-1.57; 1.76] 0.37	[-0.58; 1.02] 0.05	[-1.40; 1.27] -0.09	[-0.52; 1.64] 0.10	[-1.66; 0.98] 0.17	[-2.22; 1.17] 0.04	[-1.50; 2.45 0.33
Diabetes medication	fP-Pi	[0.03; 1.86]	[-0.71; 1.33]	[-1.14; 1.37]	[-0.74; 1.72]	[-0.68; 0.77]	[-1.12; 0.90]	[-0.76; 1.09]	[-0.95; 1.93]	[-1.28; 2.04]	[-1.12; 2.12]
Polyunsaturated Fatty Acids, E%	fP-Pi	0.22, -1.16 [0.03; 2.26]	-0.52 [-1.63; 0.31]	-0.53 [-1.81; 0.37]	-0.50 $[-1.62; 0.40]$	-0.34 [-0.89; 0.09]	[-0.40] $[-1.04; 0.10]$	-0.29 [-0.80; 0.16]	-0.25 [-0.97; 0.62]	-0.28 [-1.06; 0.64]	-0.21 [-0.93; 0.64]
Blood lipid medication	fP-Pi	0.02, -0.93 [-0.29; 3.27]	-0.81 [-3.36; 1.66]	-0.95 [-3.36; 2.11]	-0.67 [-3.58; 1.79]	-0.51 [-1.24; 0.19]	-0.82 [-2.45; 0.29]	-0.33 $[-1.19; 0.49]$	-0.14 [-1.96; 2.11]	-0.33 [-2.22; 1.70]	-0.07 [-2.23; 2.54
Diabetes medication	P-K	5.41, 3.13 [0.26; 23.43]	-0.17 [-1.92; 2.00]	-0.35 [-2.73; 2.46]	0.07 [-1.90; 2.35]	-0.13 [-1.29; 1.14]	-0.31 [-2.35; 1.47]	$\begin{bmatrix} 0.08 \\ [-1.18; 1.81] \end{bmatrix}$	-0.65 [-4.90; 2.38]	-0.76 [-4.82; 2.23]	-0.54 $[-5.11; 2.94]$
Energy, kcal/kg	fP-Pi	0.50, -2.57 [0.64; 2.17]	0.58 [-0.90; 2.05]	0.46 $[-0.95; 1.93]$	0.68 [-0.90; 2.25]	0.71 [-0.72; 1.96]	0.63 $[-0.76; 1.91]$	0.80 $[-0.72; 2.08]$	0.51 [-1.79; 2.22]	0.45 $[-1.83; 2.21]$	0.56 $[-1.88; 2.41]$
Fat E%	fP-Pi	0.21, -0.55 [0.24; 2.17]	0.51 [-1.48; 2.46]	0.46 $[-1.50; 2.43]$	0.57 [-1.46; 2.74]	$\begin{array}{c} {\bf 0.57} \\ [-1.22; 2.58] \end{array}$	0.50 $[-1.26; 2.55]$	0.63 [-1.25; 2.79]	$\begin{array}{c} \textbf{0.18} \\ [-1.91; 2.15] \end{array}$	$0.13 \\ [-1.82; 2.12]$	0.24 [-2.00; 2.17]
Renavit	P-K	0.94, -0.02 [-0.01; 7.50]	0.29 [-3.83; 6.53]	$\begin{bmatrix} 0.11 \\ [-4.16; 6.46] \end{bmatrix}$	0.58 [-3.46; 6.62]	0.76 $[-2.53; 5.74]$	$\begin{bmatrix} 0.49 \\ [-3.01; 5.34] \end{bmatrix}$	0.93 [-2.38; 5.89]	0.88 [-3.09; 6.47]	$\begin{bmatrix} 0.92 \\ [-3.27; 6.59] \end{bmatrix}$	1.08 [-2.84; 6.36]
Water	P-K	0.16, -1.66 [0.10; 1.79]	0.18 [-0.59; 1.08]	-0.04 [-1.81; 1.35]	0.36 $[-0.54; 1.31]$	-0.24 [-0.92; 0.44]	-0.48 [-1.67; 0.65]	$\begin{bmatrix} 0.01 \\ [-0.69; 0.56] \end{bmatrix}$	-0.10 [-1.53; 1.13]	-0.33 [-1.93; 1.27]	0.01
Water	fP-Pi	0.11, 1.70 [0.12; 0.73]	0.14 [-0.29; 0.60] 0.23	0.03 [-0.88; 0.69] -0.07	0.24 $[-0.37; 0.89]$ 0.46	0.17 [-0.13; 0.55] 0.03	0.00 [-0.30; 0.34] -0.29	0.23 [-0.20; 0.87]	0.05 [-0.81; 0.99] 0.47	-0.08 [-1.18; 0.97] 0.31	0.21 [-0.69; 1.08]
Fiber	P-K	-0.92, -0.10 [-0.10; 1.42]	[-0.72; 1.48]	[-1.45; 1.17]	$\left[-0.85; 1.85\right]$	[-0.93; 0.94]	[-1.45; 0.96]	0.28 [-1.04; 1.33]	[-1.04; 2.48]	[-1.32; 2.59]	0.62 [-1.21; 2.79]
Renavit	fP-Pi	0.14, -0.89 [-0.02; 3.06]	0.36 $[-2.03; 2.93]$	0.28 [-2.04; 2.94]	0.39 [-2.03; 2.96]	0.20 $[-1.60; 1.78]$	$\begin{bmatrix} 0.14 \\ [-1.73; 1.80] \end{bmatrix}$	0.26 $[-1.63; 1.89]$	0.77 $[-2.49; 4.08]$	0.70 [-2.59; 3.99]	0.83 [-2.47; 4.02]
Vitamin D	P-K	-0.17, -0.15 [-0.23; 1.11]	-0.15 [-0.94; 0.60]	-0.25 [-1.23; 0.78]	-0.11 [-0.91; 0.79]	-0.18 [-0.65; 0.45]	-0.33 [-1.04; 0.46]	$\begin{bmatrix} 0.02 \\ [-0.44; 0.60] \end{bmatrix}$	-0.31 [-1.24; 0.72]	-0.49 [-1.32; 0.42]	-0.22 [-1.21; 0.95
Protein, g/kg	fP-Pi	-0.80, 4.38 [-0.87; 1.10]	-0.84 [-2.37; 0.91] -0.14	-0.91 [-2.49; 0.86] -0.26	-0.78 [-2.52; 0.99] -0.06	-0.81 [-2.03; 0.65] -0.25	-0.86 [-2.16; 0.57] -0.40	-0.74 $[-2.03; 0.74]$ -0.01	-0.64 [-2.32; 1.06] -0.51	-0.65 [-2.29; 1.10] -0.65	-0.60 [-2.38; 1.12 -0.41
Fat E%	P-K	-0.38, 1.60 [-0.24; 3.29] 0.20, -2.40	[-4.80; 3.86] 0.12	[-5.16; 3.77] 0.08	[-4.85; 4.02] 0.16	[-4.41; 3.08] 0.24	[-4.67; 2.98] 0.20	[-4.12; 3.17] 0.30	[-5.07; 3.44] 0.14	[-5.50; 3.48] 0.09	[-4.82; 3.39 0.17
Protein, E%	fP-Pi	[0.19; 1.87]	[-0.65; 0.79]	[-0.70; 0.85]	[-0.68; 0.81]	[-0.49; 0.84]	[-0.56; 0.87]	[-0.39; 0.92]	[-1.03; 1.09]	[-1.04; 1.05]	[-1.05; 1.16]
Monounsaturated Fatty Acids, E%	fP-Pi	-0.10, 1.32 [-0.05; 1.77]	$\begin{bmatrix} 0.06 \\ [-0.73; 1.05] \end{bmatrix}$	[-0.80; 1.06]	$\begin{bmatrix} 0.12 \\ [-0.77; 1.21] \end{bmatrix}$	-0.13 [-0.89; 0.62]	-0.16 [-1.04; 0.63]	-0.05 [-0.88; 0.72]	-0.02 [-0.95; 0.94]	-0.06 [-1.01; 0.97]	0.02 [-0.91; 1.00
Polyunsaturated Fatty Acids, E%	P-K	$0.29, 0.87 \\ [0.23; 1.84]$	$\begin{array}{c} {\bf 0.28} \\ [-1.11; 1.73] \end{array}$	$0.21 \\ [-1.28; 1.85]$	$0.38 \\ [-1.21; 2.24]$	$\begin{array}{c} 0.15 \\ [-0.71; 1.10] \end{array}$	$\begin{bmatrix} 0.00 \\ [-1.02; 1.07] \end{bmatrix}$	$0.25 \\ [-0.76; 1.48]$	$ 0.32 \\ [-0.91; 1.86] $	$0.19 \\ [-1.05; 1.44]$	0.45 $[-0.81; 2.22]$
Phosphorous	P-K	0.39, 0.48 [0.52; 2.31]	0.25 $[-1.41; 2.02]$	0.15 [-1.57; 1.79]	0.36 [-1.54; 2.84]	0.21 [-1.20; 1.69]	0.10 [-1.37; 1.54]	0.37 [-1.30; 2.61]	0.51 [-1.42; 2.55]	0.45 $[-1.44; 2.39]$	0.59 $[-1.49; 2.61]$
Protein, E%	P-K	0.49, -0.26 [0.32; 3.27]	0.23 $[-0.93; 2.24]$	0.13 $[-1.23; 2.20]$	0.25 $[-0.99; 2.24]$	0.28 $[-1.23; 2.16]$	0.15 $[-1.46; 2.25]$	0.42 [-1.03; 2.26]	0.54 $[-1.25; 3.15]$	0.46 $[-1.49; 3.14]$	0.52 $[-1.32; 3.09]$
Saturated Fatty Acids, E%	P-K	$ \begin{array}{c} 1.01, \ 0.44 \\ [1.03; 3.03] \end{array} $	0.86 [-1.48; 3.10]	$0.77 \\ [-1.34; 2.93]$	0.95 $[-1.50; 3.18]$	$\begin{array}{c} 0.82 \\ [-0.95; 2.82] \end{array}$	$0.64 \\ [-1.47; 2.69]$	0.95 $[-0.86; 3.08]$	1.06 [-1.01; 3.19]	$ \begin{array}{c} 1.01 \\ [-1.17; 3.28] \end{array} $	1.18 [-0.85; 3.25]
Saturated Fatty Acids, E%	fP-Pi	-0.36, -1.90 [-0.29; 0.79]	-0.53 [-2.02; 0.56]	-0.58 [-2.04; 0.57]	-0.49 [$-2.07; 0.67$]	-0.32 [-1.22; 0.50]	-0.39 [-1.34; 0.50]	-0.27 $[-1.24; 0.65]$	-0.05 [-1.14; 0.96]	-0.06 [-1.19; 0.98]	-0.01 [-1.15; 1.03
Fiber	fP-Pi	-0.21, -2.12 [-0.15; 1.06]	-0.11 [-0.60; 0.37]	-0.18 [-0.79; 0.36]	-0.08 [-0.56; 0.41]	-0.11 [-0.66; 0.30]	-0.19 [-0.79; 0.21]	-0.05 [$-0.69; 0.56$]	-0.13 [-1.11; 0.96]	-0.16 $[-1.25; 0.97]$	-0.09 [-1.15; 1.09
Calcium	fP-Pi	-0.25, -0.25 [-0.14; 0.42]	-0.04 [-0.54; 0.56]	-0.11 [-0.93; 0.69]	0.17 $[-0.63; 1.12]$	-0.15 [-0.59; 0.22]	-0.30 [-1.19; 0.29]	$\begin{bmatrix} 0.01 \\ [-0.56; 0.66] \end{bmatrix}$	-0.06 [-0.96; 0.74]	-0.24 [-1.12; 0.84]	0.00 [-1.04; 1.04
Hydroxycholecalci	if €P ⊖Pi	1.51, 0.38 [0.48; 7.33]	$\begin{bmatrix} 0.52 \\ [-2.27; 3.05] \end{bmatrix}$	0.40 [-2.44; 3.08]	$\begin{bmatrix} 0.70 \\ [-2.10; 3.25] \end{bmatrix}$	0.49 [-0.30; 1.38]	$\begin{bmatrix} 0.40 \\ [-0.64; 1.38] \end{bmatrix}$	0.59 $[-0.42; 1.77]$	$\begin{bmatrix} 0.17 \\ [-2.04; 1.54] \end{bmatrix}$	-0.05 $[-2.09; 1.56]$	0.26 [-2.08; 1.65
Gender	fP-Pi	-0.13, -1.78 [-0.09; 0.88]	-0.02 [-1.32; 1.06]	-0.14 [-1.51; 1.14]	0.06 [-1.46; 1.22]	-0.14 [-1.12; 0.76]	-0.28 [-1.42; 0.95]	0.05 $[-1.04; 1.10]$	-0.04 [-1.34; 1.14]	-0.07 [-1.41; 1.22]	0.02 [-1.53; 1.54
Vitamin D	fP-Pi	0.10, -0.33 [0.15; 0.54]	0.06 $[-0.41; 0.58]$	-0.07 [$-0.69; 0.46$]	0.13 [-0.54; 1.01]	0.15 $[-0.14; 0.41]$	0.05 $[-0.44; 0.52]$	0.29 $[-0.14; 0.71]$	0.14 [-0.40; 0.64]	0.16 $[-0.52; 0.77]$	0.22 $[-0.35; 0.82]$
Potassium	fP-Pi	0.07, -0.12 [0.04; 0.88]	$\begin{bmatrix} 0.00 \\ [-0.72; 0.76] \end{bmatrix}$	-0.05 $[-0.82; 0.77]$	0.04 [-0.72; 0.78]	0.06 $[-0.34; 0.52]$	0.03 $[-0.51; 0.53]$	0.09 $[-0.35; 0.56]$	0.17 $[-0.56; 0.97]$	0.15 $[-0.68; 1.03]$	0.21 $[-0.48; 1.05]$
Phosphorous	fP-Pi	0.08, 1.81 [0.06; 1.41]	0.15 [-1.00; 1.13]	$\begin{bmatrix} 0.10 \\ [-1.19; 1.23] \end{bmatrix}$	0.21 $[-1.14; 1.21]$	-0.02 [-0.79; 0.79]	-0.09 [-0.95; 0.81]	$\begin{bmatrix} 0.08 \\ -0.63; 0.76 \end{bmatrix}$	0.16 [-0.91; 1.43]	0.05 $[-1.22; 1.43]$	0.20 [-0.90; 1.45
Salt	fP-Pi	0.61, 0.66 [0.12; 3.65]	-0.66 [-3.44; 0.90]	-0.71 [-3.64; 0.86]	-0.62 [-3.37; 0.96]	-0.11 [-0.52; 0.39]	-0.16 [-0.91; 0.42]	-0.04 [-0.54; 0.56]	-0.66 [-3.86; 1.21]	-0.73 [-4.08; 1.25]	-0.64 [-3.74; 1.22

Supplementary Table S5: Table shows 20 effects that have highest variation between patients by comparing minimum and maximum of effect strength expected values.

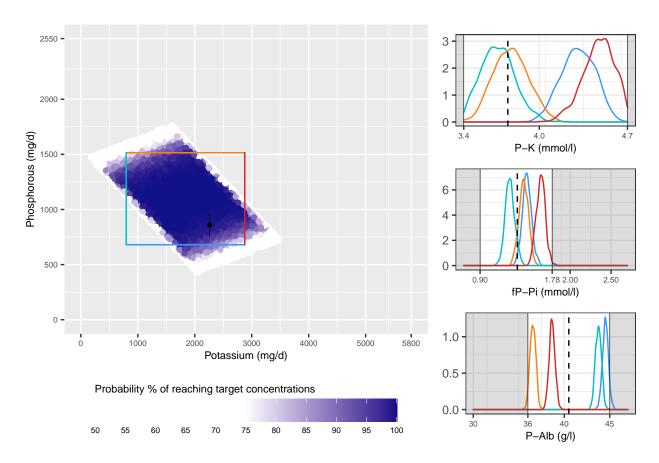
	Expected personal effect strength				
Effect	Min	Max			
Sodium -> P-Alb	-3.279	2.801			
Renavit -> P-Alb	7.283	12.771			
Potassium -> P-Alb	-5.035	0.338			
Salt -> P-Alb	-0.809	4.521			
Phosphate binder med> P-Alb	-4.258	0.839			
Energy, kcal/kg -> P-Alb	-2.934	2.153			
Phosphorous -> P-Alb	-3.089	1.726			
Gender -> P-Alb	-0.535	4.131			
Monounsaturated Fatty Acids, E% -> P-Alb	-0.653	3.919			
Protein, $g/kg \rightarrow P-Alb$	-2.724	1.617			
Carbonhydrates, E% -> P-Alb	0.160	3.712			
Blood lipid medication -> P-Alb	-1.167	1.970			
Hydroxycholecalciferol -> P-Alb	0.545	3.469			
Calcium -> P-Alb	-0.323	2.600			
Saturated Fatty Acids, E% -> P-Alb	-4.068	-1.166			
Water -> P-Alb	-2.602	0.106			
Fat E% -> P-Alb	1.525	4.145			
Diabetes medication -> P-Alb	-0.981	1.580			
$Vitamin\ D -> P-Alb$	0.111	2.385			
Protein, E% -> P-Alb	0.881	2.670			

Overview of personal recommendations



Supplementary Figure S 5: The figure shows in two left-most panels personal recommendations of potassium and phosphorous intake $(\hat{Q}^{min} - \hat{Q}^{max})$ from Algorithm (1) with predictive distributions of \hat{Q} in the background. Each row gives a numeric label of the patient and the type of patient's dialysis treatment (HD = hospital hemodialysis, HHD = home hemodialysis, PD = peritoneal dialysis). Personal recommendations are given for those patients whose resulting plasma concentration levels could be predicted in either over 90% or 80% probability. Three right-most panels show the estimated concentrations that match the recommended intake. In these panels, grey bars indicate the estimated concentration without the effect of potassium and phosphorous intake, μ_{q0} . Blue bars indicate the range of concentration that is resulted by modifying potassium and phosphorous intake. It is required that these simulated concentrations stay within the personal target ranges denoted with vertical black lines. The best exact probabilities P_m^{max} are shown with percentage figures. Red bars indicate that even the best concentration estimation has $P^{max} < 80\%$ confidence and personal recommendations are not given for these patients. For these patients, the red and blue bars show the whole reachable ranges. The figure is plotted with ggplot2 package for R language (v 3.3.5, https://ggplot2.tidyverse.org)

Personal recommendation for a patient



Supplementary Figure S 6: Figure shows detailed intake recommendation for patient 10 from the previous recommendation table. The intake plot on the left shows the posterior samples of diet configurations that result concentrations of plasma potassium (P-K), fasting plasma phosphate (fP-Pi) and plasma albumin (P-Alb) to stay within their recommended limits. These levels are marked with vertical solid lines in the concentration panels. The black point in the middle of intake plot represents the patient's current potassium and phosphorous intake. Current concentrations matching this intake are shown with dashed vertical lines. Reported recommendation is shown with a rectangle that contains 95% of diet proposals that result recommended concentrations over 90% accuracy. Colouring of the rectangle sides match the concentration estimates in the right hand panels. The figure is plotted with ggplot2 package for R language (v 3.3.5, https://ggplot2.tidyverse.org).