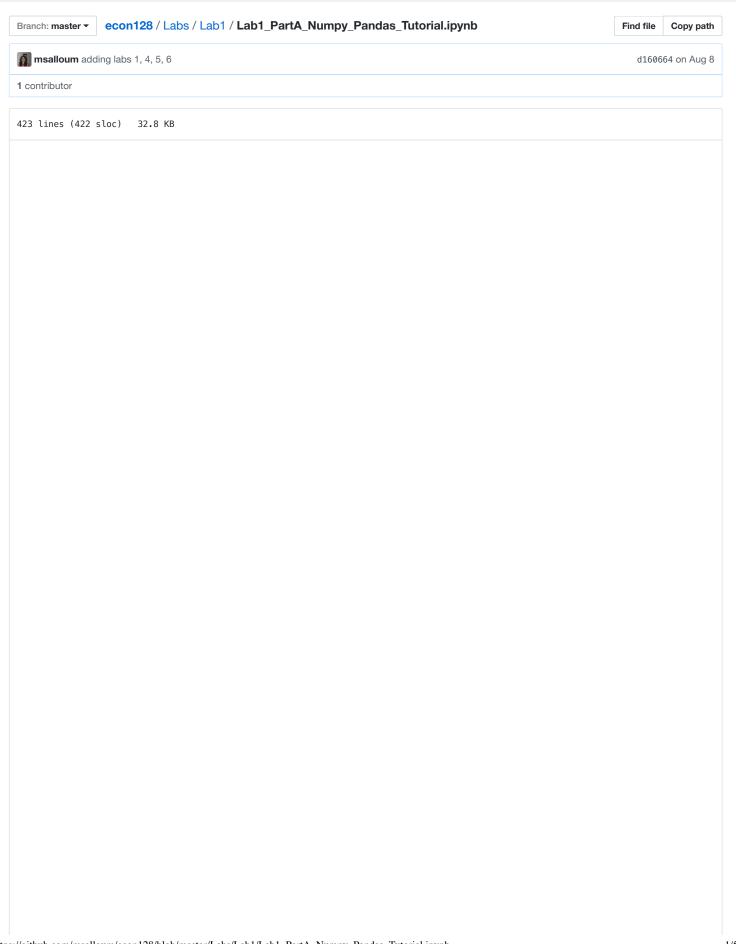
msalloum / econ128



Numpy

Provides various utilities functions on top of N-dimensional array such statistical calculation (.mean(), .std()) and vectorized operation.

A numpy array is a N-dimensional array, all of the same type, and is indexed by nonnegative integers. The number of dimensions is the rank of the array; the shape of an array is a tuple of integers giving the size of the array along each dimension.

We can initialize numpy arrays from nested Python lists, and access elements using square brackets:

```
In [16]: from numpy import *
          a = arange(15).reshape(3, 5)
          print a
          print "Type of a:", type(a)
          print "Shape of a:", a.shape
print "# dimensions:", a.ndim
          print "datatype of elements in a:", a.dtype.name
          print "# of elements:", a.size
          b = array([6,7,8])
          print "Type of b:", type(b)
          print "1st elem in b:", b[0] # print first element in b
          [[ 0 1 2 3 4]
[ 5 6 7 8 9]
           [10 11 12 13 14]]
          Shape of a: (3, 5)
          # dimensions: 2
          datatype of elements in a: int64
          # of elements: 15
          Type of a: <type 'numpy.ndarray'>
          Type of b: <type 'numpy.ndarray'>
```

Array creation

Numpy also provides many functions to create arrays. You can also read more about array creation here : https://docs.scipy.org/doc/numpy/user/basics.creation.html#arrays-creation (https://docs.scipy.org/doc/numpy/user/basics.creation.html#arrays-creation)

```
In [39]: a = np.zeros((2,2)) # Create an array of all zeros
         print "a:\n", a
         b = np.ones((1,2)) # Create an array of all ones
         print "b:\n", b
         c = np.full((2,2), 7) # Create an array with a constant
         print "c:\n", c
                              # Create a 2x2 identity matrix
         d = np.eye(2)
         print "d:\n", d
         e = np.random.random((2,2)) # Create an array filled with random values
         print "e:\n", e
         a:
         [[ 0. 0.]
          [ 0. 0.]]
         b:
         [[ 1. 1.]]
         [[ 7. 7.]
         [ 7. 7.]]
         d:
         [[ 1. 0.]
         [ 0. 1.]]
         [[ 0.06939502  0.98031338]
          [ 0.71210968  0.31308969]]
```

Array indexing

Numpy offers several ways to index into arrays.

Slicing: Similar to Python lists, numpy arrays can be sliced. Since arrays may be multidimensional, you must specify a slice for each dimension of the array:

```
In [ ]: # Create the following rank 2 array with shape (3, 4)
        #[[1 2 3 4]
          [5 6 7 8]
        # [ 9 10 11 12]]
        a = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
        # Use slicing to pull out the subarray consisting of the first 2 rows
        # and columns 1 and 2; b is the following array of shape (2, 2):
        # [[2 3]
        # [6 7]]
        b = a[:2, 1:3]
        # A slice of an array is a view into the same data, so modifying it
        # will modify the original array.
        print(a[0, 1]) # Prints "2"
        b[0, 0] = 77
                        # b[0, 0] is the same piece of data as a[0, 1]
        print(a[0, 1]) # Prints "77"
```

You can also mix integer indexing with slice indexing. However, doing so will yield an array of lower rank than the original array.

```
In [ ]: # Create the following rank 2 array with shape (3, 4)
        # [[ 1 2 3 4]
        # [5 6 7 8]
        # [ 9 10 11 12]]
        a = np.array([[1,2,3,4], [5,6,7,8], [9,10,11,12]])
        # Two ways of accessing the data in the middle row of the array.
        # Mixing integer indexing with slices yields an array of lower rank,
        # while using only slices yields an array of the same rank as the
        # original array:
        row r1 = a[1, :]
                           # Rank 1 view of the second row of a
        row_r2 = a[1:2, :] # Rank 2 view of the second row of a
        print(row_r1, row_r1.shape) # Prints "[5 6 7 8] (4,)"
        print(row r2, row r2.shape) # Prints "[[5 6 7 8]] (1, 4)"
        # We can make the same distinction when accessing columns of an array:
        col_r1 = a[:, 1]
        col_r2 = a[:, 1:2]
        print(col_r1, col_r1.shape) # Prints "[ 2 6 10] (3,)"
        print(col_r2, col_r2.shape) # Prints "[[ 2]
                                               [ 61
                                               [10]] (3, 1)"
```

Array math

Basic mathematical functions operate elementwise on arrays, and are available both as operator overloads and as functions in the numpy module:

```
In [42]: x = np.array([[1,2],[3,4]], dtype=np.float64)
         y = np.array([[5,6],[7,8]], dtype=np.float64)
         # Elementwise sum; both produce the array
         print "matrix sum:\n", x + y
         print "matrix sum:\n", add(x, y)
         # Elementwise difference; both produce the array
         print "matrix difference:\n", x - y
         print "matrix difference:\n", subtract(x, y)
         # Elementwise product; both produce the array
         print "matrix prodcut:\n", x * y
         print "matrix prodcut:\n", multiply(x, y)
         # Elementwise division; both produce the array
         print "matrix division:\n", x / y
         print "matrix division:\n", divide(x, y)
         # Elementwise square root; produces the array
         print "square root:\n", sqrt(x)
         # Elementwise product by scaler
         noint "matrix by goalor.\n" v * 3
```

```
print "matrix by scaler: \n", x ^ 2
matrix sum:
[[ 6. 8.]
[ 10. 12.]]
matrix sum:
[[ 6. 8.]
[ 10. 12.]]
matrix difference:
[[-4. -4.]
[-4. -4.]]
matrix difference:
[[-4. -4.]
 [-4. -4.]
matrix prodcut:
[[ 5. 12.]
[ 21. 32.]]
matrix prodcut:
[[ 5. 12.]
[ 21. 32.]]
matrix division:
[[ 0.2
             0.33333333]
[ 0.42857143 0.5
                    ]]
matrix division:
               0.333333331
[[ 0.2
[ 0.42857143 0.5
square root:
[[ 1.
               1.41421356]
 [ 1.73205081 2.
matrix by scaler:
[[ 2. 4.]
 [ 6. 8.]]
```

Linear algebra operations

```
In [30]: A = array([[1,1], [0,1]])
         B = array([[2,0],[3,4]])
         print "A*B:\n", A*B # elementwise product
         print "dot(A,B):\n", dot(A,B) # matrix product
         a = ones((2,3), dtype=int) # create matrix all 1s of size 2 x 3
         b = random.random((2,3)) # create matrix of size 2 x 3, randomly
          a *= 3 # multiply each element by 3
         print "a:\n", a
         b \mathrel{+=} a \mathrel{\#} add \; two \; matrices, \; and \; assign \; to \; matrix \; b
         print "b\n:", b
         A*B:
         [[2 0]
          [0 4]]
         dot(A,B):
         [[5 4]
          [3 4]]
         a:
         [[3 3 3]
          [3 3 3]]
         : [[ 3.51665755  3.15221622  3.896464 ]
          [ 3.42767488  3.25868986  3.42485715]]
In [43]: a = random.random((2,3))
         print "matrix a:\n", a
         print "sum:\n", a.sum()
         print "min:\n",a.min()
         print "max:\n",a.max()
         matrix a:
         [[ 0.59257921 0.72241258 0.32824592]
          [ 0.67982578  0.71641435  0.02639753]]
         sum:
         3.06587536152
         min:
         0.0263975324349
```

max: 0.722412578383 In [32]: # show histogram of elements in array import numpy import pylab # Build a vector of 10000 normal deviates with variance 0.5^2 and mean 2 mu, sigma = 2, 0.5 v = numpy.random.normal(mu,sigma,10000) print "v:", v # Plot a normalized histogram with 50 bins pylab.hist(v, bins=50, normed=1) # matplotlib version (plot) pylab.show() # Compute the histogram with numpy and then plot it (n, bins) = numpy.histogram(v, bins=50, normed=True) # NumPy version (no plot) pylab.plot(.5*(bins[1:]+bins[:-1]), n) pylab.show() 2.38886047]

