

SMAI

For parent node D:

No. of positive review = 5

No. " negative " = 5

$$\text{Parent entropy} = H(D) = - \sum_{i \in \text{class}} P_i \log(P_i)$$

$$= - 2 \times \frac{1}{2} \times \log\left(\frac{1}{2}\right)$$

$$= 1$$

If we divide along smell

→ For node "woody"

No. of positive = 2

" " negative = 3

$$P(D_i) = (2+3)/10 = 1/2$$

$$H(D_i) = \frac{-2 \log\left(\frac{2}{5}\right) - 3 \log\left(\frac{3}{5}\right)}{5} = 0.97$$

→ For node "fruity"

No. of positive = 3

No. of negative = 2

$$P(D_i) = (3+2)/10 = 1/2$$

$$H(D_i) = \frac{-3 \log\left(\frac{3}{5}\right) - 2 \log\left(\frac{2}{5}\right)}{5} = 0.97$$

$$\text{Info gain} = 1 - \frac{1}{2} \times 0.97 - \frac{1}{2} \times 0.97 = 0.03$$

If we divide along taste

→ For node 'sweet'

No. of positive = 0

No. of negative = 3

$$P(D_i) = 3/10$$

$$H(D_i) = -\frac{3}{3} \log\left(\frac{3}{3}\right) = 0$$

→ For node 'sour'

No. of positive = 3

No. of negative = 0

$$P(D_i) = 3/10$$

$$H(D_i) = -\frac{3}{3} \log\left(\frac{3}{3}\right) = 0$$

→ For node 'salty'

No. of positive = 2

" " negative = 2

$$P(D_i) = 4/10$$

$$H(D_i) = 2 \times -\frac{2}{4} \log\left(\frac{2}{4}\right) = 1$$

$$\text{Info gain} = 1 - \frac{4}{10} = 0.6$$

If we divide along position

• For node 'small'

No. of negative = 1

No. of positive = 4

$$P(D_i) = (1+4)/10 = 1/2$$

$$H(D_i) = -\frac{1}{5} \log(1/5) - \frac{4}{5} \log(4/5) = 0.72$$

• For node 'large'

No. of negative = 4

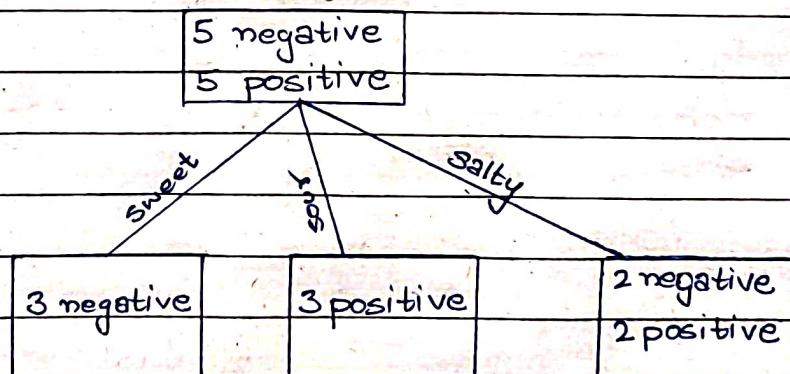
No. of positive = 1

$$P(D_i) = (4+1)/10 = 1/2$$

$$H(D_i) = -\frac{4}{5} \log(4/5) - \frac{1}{5} \log(1/5) = 0.72$$

$$\text{Info gain} = 1 - \frac{2 \times 1}{2} \times 0.72 = 0.28$$

As info gain is maximum for taste, we will split along taste.



Now if the taste is salty, the table will be -

Review	Smell	Taste	Portion
Negative	Fruity	Salty	Large
Negative	Fruity	Salty	Large
Positive	Fruity	Salty	Small
Positive	Fruity	Salty	Small

From the above table it is clear that portion is the only feature with positive info gain and we can directly classify after splitting along portion.

So the decision tree obtained is -

