

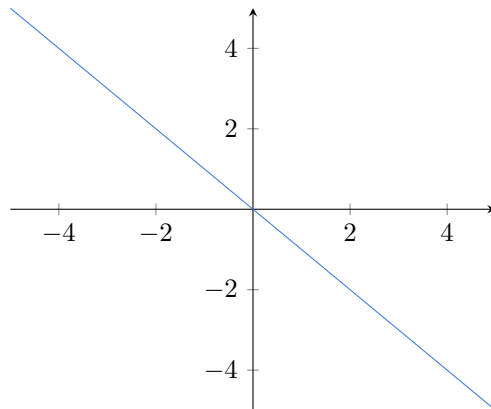
# An Investigation in Cartesian Planes

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We can make equations that represent a line on the Cartesian plane.

$$x + y = 0 \tag{1}$$



(2)

These are also called linear equations.

Let's say we do it the other way around and make a equation, who's solution is what we choose.

We want a equation, whose solution is

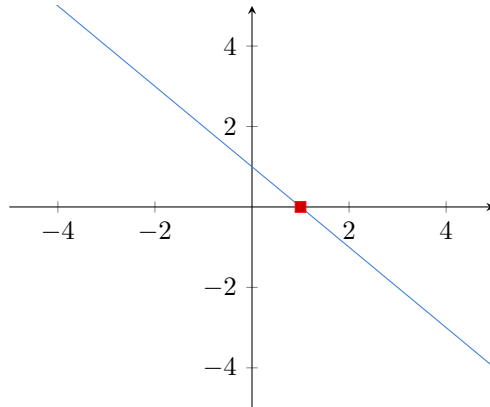
$$x = 1, y = 0 \tag{3}$$

Let's try adding the equations, so,

$$x + y = 1 + 0 \tag{4}$$

$$x + y = 1 \tag{5}$$

Let's verify it graphically,



(6)

Yay! We did it!

Now what about 2 solutions equations?

Umm, I think these equation are also called Quadratic Equations.  
Anyway, Let's say the required points are

$$x_1 = 1 \quad (7)$$

$$y_1 = 0 \quad (8)$$

$$x_2 = 2 \quad (9)$$

$$y_2 = 0 \quad (10)$$

Now to create the equation. Let's first make a equation for each point first.

$$x + y = 1 + 0 \quad (11)$$

$$x + y = 1 \quad (12)$$

$$x + y = 2 + 0 \quad (13)$$

$$x + y = 2 \quad (14)$$

Upon further rearrangement,

$$x + y - 1 = 0 \quad (15)$$

$$x + y - 2 = 0 \quad (16)$$

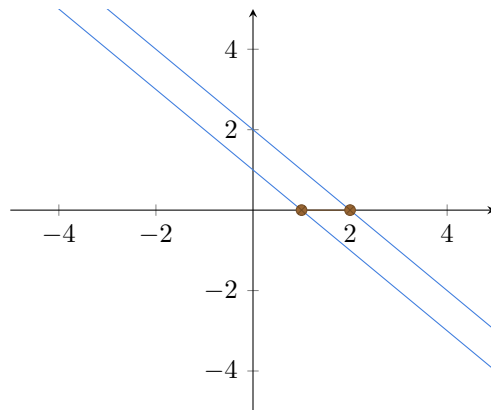
Let's use the factor theorem to make a equation

$$(x + y - 1)(x + y - 2) = 0 \quad (17)$$

$$x^2 + xy - 2x + xy + y^2 - 2y - x - y + 2 = 0 \quad (18)$$

$$x^2 + y^2 + 2xy - 3(x + y) + 2 = 0 \quad (19)$$

We have a equation now! Let's verfiy using a graph.



(20)

Damn, that's satisfying! Do you know what's even more satisfying? There are infinite solutions to our question.

Let's try finding the other solutions.

This is the factored form of the equation we had obtained.

$$(x + y - 1)(x + y - 2) = 0 \quad (21)$$

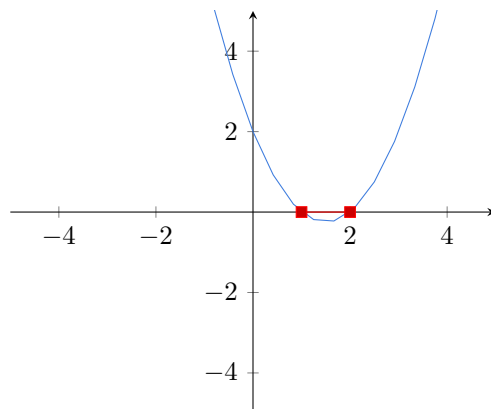
If we manipulate them and take y as the function we get,

$$f(x) = (1 - x)(2 - x) \quad (22)$$

$$f(x) = 2 - x - 2x + x^2 \quad (23)$$

$$f(x) = x^2 - 3x + 2 \quad (24)$$

Let's graph this one and try again.



(25)

We found another equation, I am sure that there are many more! But I haven't found another one yet. But if you find one email me at [tusharmaharana44674@gmail.com](mailto:tusharmaharana44674@gmail.com).