On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages. Any revealing of identification, appeal to evaluator and for equations written eg, 42+8=50, will be treated as malpractice.

portant Note: 1. (



USN

15CS/IS54

Fifth Semester B.E. Degree Examination, Dec.2017/Jan.2018 Automata Theory & Compatibility

Time: 3 hrs.

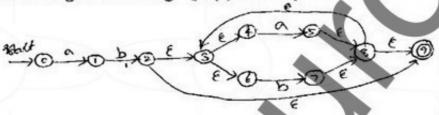
Max. Marks: 80

Note: Answer FIVE full questions, choosing one full question from each module.

Module-1

- a. Define the following terms with examples: (i) Alphabet
 (iii) Concatenation (iv) Languages
- (ii) Power of an alphabet (04 Marks)
- b. Draw a DFA to accept strings of a's and b's ending with 'bab'.
- (03 Marks)
- c. Convert the following NDFSM Fig. Q1 (c) to its equivalent DFSM.

(09 Marks)



OR

Fig. Q1 (c)

2 a. Draw a DFSM to accept the language,

 $L = \left\{ \omega \in \left\{ a, b \right\}^* : \forall x, y \in \left\{ a, b \right\}^* \left(\left(\omega = x \text{ abbaay} \right) \vee \left(\omega = x \text{ babay} \right) \right) \right\}$

(03 Marks)

b. Define distinguishable and indistinguishable states. Minimize the following DFSM,

S	0	1
A	В	A
В	A	C
C	D	В
*D	D	A
F	D	F
F	G	E
G	F	G
Н	G	D

- Draw the table of distinguishable and indistinguishable state for the automata.
- (ii) Construct minimum state equivalent of automata.

(09 Marks)

Write differences between DFA, NFA and ε-NFA.

(04 Marks)

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Module-2

3 a. Consider the DFA shown below:

States	0	1
→q1	q ₂	qı
q_2	q ₃	q ₁
*q3	q ₃	q ₂

Obtain the regular expressions $R_{ij}^{(0)}$, $R_{ij}^{(1)}$ and simplify the regular expressions as much as possible. (09 Marks)

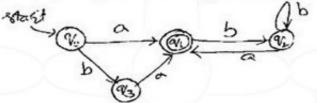
- b. Give Regular expressions for the following languages on $\sum = \{a, b, c\}$
 - (i) all strings containing exactly one a
 - (ii) all strings containing no more than 3 a's.
 - (iii) all strings that contain at least one occurance of each symbol in \(\sum_{\text{(03 Marks)}} \)

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3 c. Let L be the language accepted by the following finite state machine.

(04 Marks)



Indicate for each of the following regular expressions, whether it correctly describes L:

- (i) (a ∪ ba)bb*a
- (ii) $(\varepsilon \cup b)a(bb*a)*$
- (iii) ba∪ab*a
- $(a \cup ba)(bb*a)*$ (iv)

OR

- a. Prove that the following language in not regular: $L = \{0^n\}^n \mid n > 0$ (05 Marks)
 - b. If L_1 and L_2 are regular languages then prove that $L_1 \cup L_2$, $L_1.L_2$ and L_1 are regular languages. (05 Marks)
 - c. Is the following grammar is ambiguous?

 $S \rightarrow iC + S | iC + SeS | a$

 $C \rightarrow b$

Module-3

- a. Define Grammar, Derivation, Sentential forms and give one example for each. (03 Marks)
 - b. What is CNF? Obtain the following grammar in CNF

S→ASB|ε

 $A \rightarrow aAS \mid a$

 $B \rightarrow SbS | A | bb$

(09 Marks)

(06 Marks)

- Let G be the grammar,
 - $S \rightarrow aB \mid bA$

 $A \rightarrow a \mid aS \mid bAA$

 $B \rightarrow b|bS|aBB$

For the string aaabbabbba find a

- Left most derivation. (i)
- (ii) Right most derivation.
- (iii) Parse tree.

(04 Marks)

OR

- a. Explain the following terms:
 - Pushdown automata (PDA).
 - Languages of a PDA.
 - (iii) Instantaneous description of a PDA.

(03 Marks)

Construct a PDA to accept the language $L = \{\omega \omega^R \mid \omega \in \{a, b\}^*\}$. Draw the graphical representation of this PDA. Show the moves made by this PDA for the string aabbaa.

(10 Marks)

Convert the following CFG to PDA

S → aABB | aAA

 $A \rightarrow aBB \mid a$

 $B \rightarrow bBB \mid A$

 $C \rightarrow a$

(03 Marks)

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Module-4

- a. If L₁ and L₂ are context free languages then prove that L₁ ∪ L₂, L₁ · L₂ and L₁ are context free languages.
 (04 Marks)
 - b. Give a decision procedure to answer each of the following questions:
 - (i) Given a regular expression α and a PDA M, the language accepted by M a subset of the language generated by α?
 - (ii) Given a context-free Grammar G and two strings S₁ and S₂, does G generate S₁S₂?
 - (iii) Given a context free Grammar G, does G generate any even length strings.
 - (iv) Given a Regular Grammar G, is L(G) context-free?

OR

- 8 a. Explain with neat diagram, the working of a Turing Machine model. (05 Marks)
 - b. Design a Turing machine to accept the language $L = \{a^nb^nc^n \mid n >= 1\}$. Draw the transition diagram. Show the moves made by this turing machine for the string aabbcc. (11 Marks)

Module-5

9 Write short notes on:

10

- a. Multi-tape turing machine.
- b. Non-deterministic turing machine.
- c. Linear Bounded automata.

(16 Marks)

(12 Marks)

- Write short notes on: a. Undecidable languages.
- b. Halting problem of turing machine.
- c. The post correspondence problem.

(16 Marks)

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