

Experiment No 3

Title: Random Forest and Parameter Tuning in R

Introduction

Random forest is a tree-based algorithm which involves building several trees (decision trees), then combining their output to improve generalization ability of the model. The method of combining trees is known as an ensemble method. Ensembling is nothing but a combination of weak learners (individual trees) to produce a strong learner.

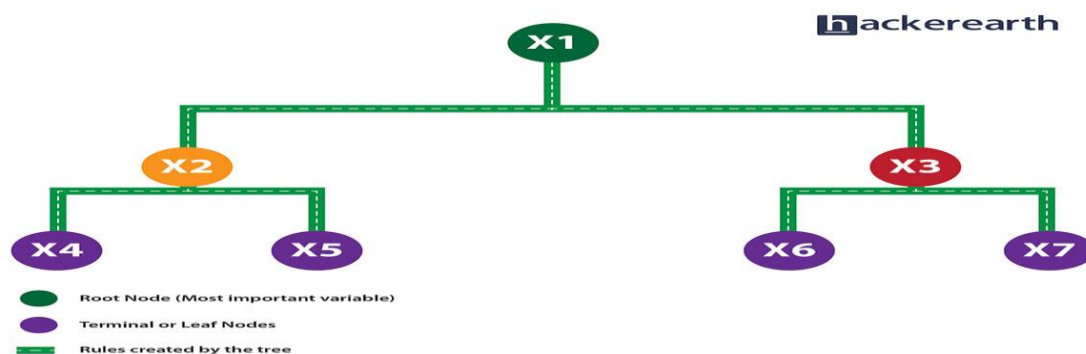
Say, you want to watch a movie. But you are uncertain of its reviews. You ask 10 people who have watched the movie. 8 of them said "the movie is fantastic." Since the majority is in favor, you decide to watch the movie. This is how we use ensemble techniques in our daily life too.

Random Forest can be used to solve regression and classification problems. In regression problems, the dependent variable is continuous. In classification problems, the dependent variable is categorical.

The random Forest algorithm was created by [Leo Brieman](#) and [Adele Cutler](#) in 2001.

How does it work? (Decision Tree, Random Forest)

To understand the working of a random forest, it's crucial to understand a **tree**. A tree works in the following way:



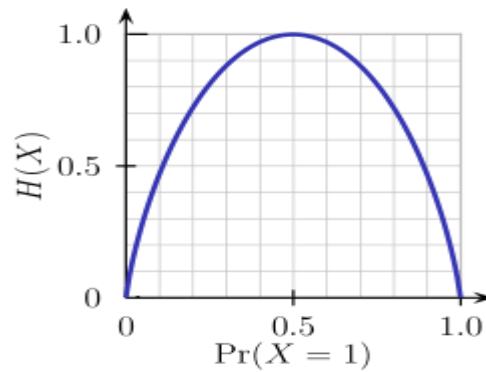
1. Given a data frame ($n \times p$), a tree stratifies or partitions the data based on rules (if-else). Yes, a tree creates rules. These rules divide the data set into distinct and non-overlapping regions. These rules are determined by a variable's contribution to the homogeneity or pureness of the resultant child nodes (X_2, X_3).

2. In the image above, the variable X_1 resulted in highest homogeneity in child nodes, hence it became the root node. A variable at root node is also seen as the most important variable in the data set.

3. But how is this homogeneity or pureness determined? In other words, how does the tree decide at which variable to split?

- In **regression trees** (where the output is predicted using the mean of observations in the terminal nodes), the splitting decision is based on minimizing RSS. The variable which leads to the greatest possible reduction in RSS is chosen as the root node. The tree splitting takes a **top-down greedy** approach, also known as *recursive binary splitting*. We call it "greedy" because the algorithm cares to make the best split at the current step rather than saving a split for better results on future nodes.
- In **classification trees** (where the output is predicted using mode of observations in the terminal nodes), the splitting decision is based on the following methods:
 - **Gini Index** - It's a measure of node purity. If the Gini index takes on a smaller value, it suggests that the node is pure. For a split to take place, the Gini index for a child node should be less than that for the parent node.
 - **Entropy** - Entropy is a measure of node impurity. For a binary class (a,b), the formula to calculate it is shown below. Entropy is maximum at $p = 0.5$. For $p(X=a)=0.5$ or $p(X=b)=0.5$ means, a new observation has a 50%-50% chance of getting classified in either classes. The entropy is minimum when the probability is 0 or 1.

$$\text{Entropy} = - p(a) \cdot \log(p(a)) - p(b) \cdot \log(p(b))$$



In a nutshell, every tree attempts to create rules in such a way that the resultant terminal nodes could be as pure as possible. Higher the purity, lesser the uncertainty to make the decision. But a decision tree suffers from high variance. "High Variance" means getting high prediction error on unseen data. We can overcome the variance problem by using more data for training. But since the data set available is limited to us, we can use resampling techniques like bagging and random forest to generate more data.

Building many **decision trees** results in a **forest**. A random forest works the following way:

1. First, it uses the Bagging (Bootstrap Aggregating) algorithm to create random samples. Given a data set D1 (n rows and p columns), it creates a new dataset (D2) by sampling n cases at random with replacement from the original data. About 1/3 of the rows from D1 are left out, known as Out of Bag(OOB) samples.
2. Then, the model trains on D2. OOB sample is used to determine unbiased estimate of the error.
3. Out of p columns, $P \ll p$ columns are selected at each node in the data set. The P columns are selected at random. Usually, the default choice of P is $p/3$ for regression tree and P is \sqrt{p} for classification tree.
4. Unlike a tree, no pruning takes place in random forest; i.e, each tree is grown fully. In decision trees, pruning is a method to avoid overfitting. Pruning means selecting a subtree that leads to the lowest test error rate. We can use cross validation to determine the test error rate of a subtree.
5. Several trees are grown and the final prediction is obtained by averaging or voting.

Each tree is grown on a different sample of original data. Since random forest has the feature to calculate OOB error internally, cross validation doesn't make much sense in random forest.

Advantages and Disadvantages of Random Forest

Advantages are as follows:

1. It is robust to correlated predictors.
2. It is used to solve both regression and classification problems.
3. It can be also used to solve unsupervised ML problems.
4. It can handle thousands of input variables without variable selection.
5. It can be used as a feature selection tool using its variable importance plot.
6. It takes care of missing data internally in an effective manner.

Disadvantages are as follows:

1. The Random Forest model is difficult to interpret.
2. It tends to return erratic predictions for observations out of range of training data. For example, the training data contains two variable x and y. The range of x variable is 30 to 70. If the test data has $x = 200$, random forest would give an unreliable prediction.
3. It can take longer than expected time to computer a large number of trees.

R Program

```
install.packages("randomForest")  
  
library(randomForest)  
  
data1 <- read.csv(file.choose(), header = TRUE)  
  
head(data1)  
  
str(data1)  
  
summary(data1)  
  
# Split into Train and Validation sets  
  
# Training Set : Validation Set = 70 : 30 (random)
```

```
set.seed(100)

train <- sample(nrow(data1), 0.7*nrow(data1), replace = FALSE)

TrainSet <- data1[train,]

ValidSet <- data1[-train,]

summary(TrainSet)

summary(ValidSet)

# Create a Random Forest model with default parameters

model1 <- randomForest(Condition ~ ., data = TrainSet, importance = TRUE)

model1

# Fine tuning parameters of Random Forest model

model2 <- randomForest(Condition ~ ., data = TrainSet, ntree = 500, mtry = 6, importance = TRUE)

model2

# Predicting on train set

predTrain <- predict(model2, TrainSet, type = "class")

# Checking classification accuracy

table(predTrain, TrainSet$Condition)

# Predicting on Validation set

predValid <- predict(model2, ValidSet, type = "class")

# Checking classification accuracy

mean(predValid == ValidSet$Condition)

table(predValid, ValidSet$Condition)

# To check important variables

importance(model2)

varImpPlot(model2)
```

Output of the program and analysis

```
> library(randomForest)
randomForest 4.6-14
Type rfNews() to see new features/changes/bug fixes.
> data1 <- read.csv(file.choose(), header = TRUE)

> head(data1)
  Buying   maint  doors  persons lug_boot   safety Condition
1  vhigh   vhigh    2      2      small    low      unacc
2  vhigh   vhigh    2      2      small    med      unacc
3  vhigh   vhigh    2      2      small    high     unacc
4  vhigh   vhigh    2      2      med     low      unacc
5  vhigh   vhigh    2      2      med     med      unacc
6  vhigh   vhigh    2      2      med     high     unacc

> str(data1)
'data.frame':   1728 obs. of  7 variables:
 $ buying  : Factor w/ 4 levels "high","low","med",...: 4 4 4 4 4 4 4 4 4 4 ...
 $ maint   : Factor w/ 4 levels "high","low","med",...: 4 4 4 4 4 4 4 4 4 4 ...
 $ doors   : Factor w/ 4 levels "2","3","4","5more": 1 1 1 1 1 1 1 1 1 1 ...
 $ persons : Factor w/ 3 levels "2","4","more": 1 1 1 1 1 1 1 1 1 2 ...
 $ lug_boot: Factor w/ 3 levels "big","med","small": 3 3 3 2 2 2 1 1 1 3 ...
 $ safety  : Factor w/ 3 levels "high","low","med": 2 3 1 2 3 1 2 3 1 2 ...
 $ Condition: Factor w/ 4 levels "acc","good","unacc",...: 3 3 3 3 3 3 3 3 3 3 ...

> summary(data1)
  buying   maint   doors  persons  lug_boot
high:432  high:432  2 :432  2 :576  big :576
low :432  low :432  3 :432  4 :576  med :576
med :432  med :432  4 :432  more:576  small:576
vhigh:432 vhigh:432 5more:432

  safety  Condition
high:576  acc : 384
low :576  good:  69
med :576  unacc:1210
          vgood:  65

> set.seed(100)
> train <- sample(nrow(data1), 0.7*nrow(data1), replace = FALSE)
> TrainSet <- data1[train,]
> ValidSet <- data1[-train,]
> summary(TrainSet)
  buying   maint   doors  persons  lug_boot
high:298  high:303  2 :312  2 :407  big :406
low :300  low :302  3 :298  4 :409  med :393
```

```

med :306 med :312 4 :299 more:393 small:410
vhigh:305 vhigh:292 5more:300
safety Condition
high:396 acc :260
low :412 good : 46
med :401 unacc:856
vgood: 47

```

```
> summary(ValidSet)
```

```

buying maint doors persons lug_boot
high:134 high:129 2 :120 2 :169 big :170
low :132 low :130 3 :134 4 :167 med :183
med :126 med :120 4 :133 more:183 small:166
vhigh:127 vhigh:140 5more:132
safety Condition
high:180 acc :124
low :164 good : 23
med :175 unacc:354
vgood: 18

```

```
> model1 <- randomForest(Condition ~ ., data = TrainSet, importance = TRUE)
```

```
> model1
```

Call:

```
randomForest(formula = Condition ~ ., data = TrainSet, importance = TRUE)
```

```
  Type of random forest: classification
```

```
    Number of trees: 500
```

```
No. of variables tried at each split: 2
```

```
  OOB estimate of error rate: 3.64%
```

```
Confusion matrix:
```

	acc	good	unacc	vgood	class.error
acc	255	2	2	1	0.01923077
good	7	35	0	4	0.23913043
unacc	20	2	834	0	0.02570093
vgood	6	0	0	41	0.12765957

By default, number of trees is 500 and number of variables tried at each split is 2 in this case. Error rate is 3.6%

```
> model2 <- randomForest(Condition ~ ., data = TrainSet, ntree = 500, mtry = 6, importance = TRUE)
```

```
> model2
```

Ntree: Number of trees to grow. This should not be set to too small a number, to ensure that every input row gets predicted at least a few times.

Mtry: Number of variables randomly sampled as candidates at each split. Note that the default values are different for classification (\sqrt{p}) where p is number of variables in x) and regression ($p/3$)

Call:

```
randomForest(formula = Condition ~ ., data = TrainSet, ntree = 500, mtry = 6, importance = TRUE)
```

Type of random forest: classification

Number of trees: 500

No. of variables tried at each split: 6

OOB estimate of error rate: 2.32%

Confusion matrix:

	acc	good	unacc	vgood	class.error
acc	248	6	5	1	0.04615385
good	4	42	0	0	0.08695652
unacc	8	2	846	0	0.01168224
vgood	2	0	0	45	0.04255319

When we have increased the mtry to 6 from 2, error rate has reduced from 3.6% to 2.32%. We will now predict on the train dataset first and then predict on validation dataset.

```
> predTrain <- predict(model2, TrainSet, type = "class")
> table(predTrain, TrainSet$Condition)
```

predTrain	acc	good	unacc	vgood
acc	260	0	0	0
good	0	46	0	0
unacc	0	0	856	0
vgood	0	0	0	47

```
> predValid <- predict(model2, ValidSet, type = "class")
> mean(predValid == ValidSet$Condition)
[1] 0.9845857
> table(predValid, ValidSet$Condition)
```

predValid	acc	good	unacc	vgood
acc	120	1	2	1
good	1	22	0	0
unacc	3	0	352	0
vgood	0	0	0	17

In case of prediction on train dataset, there is zero misclassification; however, in the case of validation dataset, 6 data points are misclassified and accuracy is 98.84%. We can also use function to check important variables. The below functions show the drop in mean accuracy for each of the variables.

```
> importance(model2)
```


	acc	good	unacc	vgood
buying	144.13929	75.96633	111.10092	80.70126
maint	134.88327	69.62648	104.31162	50.07345
doors	32.35052	17.55486	47.57988	20.17438
persons	150.37837	50.89904	186.53684	57.04931
lug_boot	85.05941	55.85293	83.13938	63.39719
safety	176.85992	82.14649	201.91053	110.32306

	MeanDecreaseAccuracy	MeanDecreaseGini
buying	200.4809	68.49384
maint	182.8435	91.02632
doors	57.3249	33.93850
persons	237.0746	122.51556
lug_boot	144.7800	75.31990
safety	277.8490	151.59471

```
> varImpPlot(model2)
```

model2

