

Lecture 1: January 12, 2015
cs 573: Probabilistic Reasoning
Professor Nevatia
Spring 2015

Introduction

- Course name: Probabilistic Reasoning
 - csci 573
- Instructor: Prof. Ram Nevatia
 - My background, interests
- Attendance sheet, in class students only
- Today's objective
 - Describe course content
 - Conduct of the class
 - Required work, grading
 - Pre-requisites

General Information

- Course web page <https://courses.uscden.net>
 - Must be registered for class to have access
 - Usually, a preliminary version of slides will be posted prior to class, complete version after the class.
 - Lecture videos, course notes....
- Office hours:
 - Instructor: MW 1:30-3:00 P.M., PHE 204, 213-740-6427, nevatia AT usc.edu
 - This week only: Today, 1- 2 P.M., none on Wednesday
 - TA: Tom Collins, collinst AT usc.edu , office hours and place TBD
- Book:
 - Required: *Probabilistic Graphical Models* by Koller and Friedman, MIT Press 2010. Note: errata for early printings may be found at <http://pgm.stanford.edu/errata/>
- Koller video lectures available at:
<https://class.coursera.org/pgm/lecture/preview>

About Enrollment

- On-campus section is fully subscribed
- Capacity limited by physical space and ability to provide individual attention to students
 - Not possible to add another section due to non-availability of a qualified instructor
- Heavy demand is a surprise to us
 - Previous years have seen much lower demand and enrollments
- Common for students to drop in first 1-2 weeks of class
 - Will fill in if and as students drop

Prerequisites

- Undergraduate level course in probability theory
- Good skills with basic mathematics such as calculus and linear algebra
- Programming skills: ability to convert algorithms into programs
- May have some overlap with cs561 (basic AI course) and cs567 (Machine Learning).
 - Neither is a pre-requisite

Requirements and Grading

- Assignments: 7-8 assignments, mostly written (mathematical) but 1-2 programming assignments may be included. *Large* projects are not planned.
- Grading:
 - Assignments 30%,
 - Exams 1 and 2: 30% each
 - Class attendance and participation 10% (does not apply to DEN students)
- Exams:
 - Exam 1, during 7th or 8th week of classes; exact date will be announced at least 1 week in advance
 - Exam 2, April 29, 2015; last day of scheduled classes
- Programming
 - No programming projects are planned but some programming may be necessary to solve numerical problems
 - Students may choose their own language but some packages may be specific to some languages

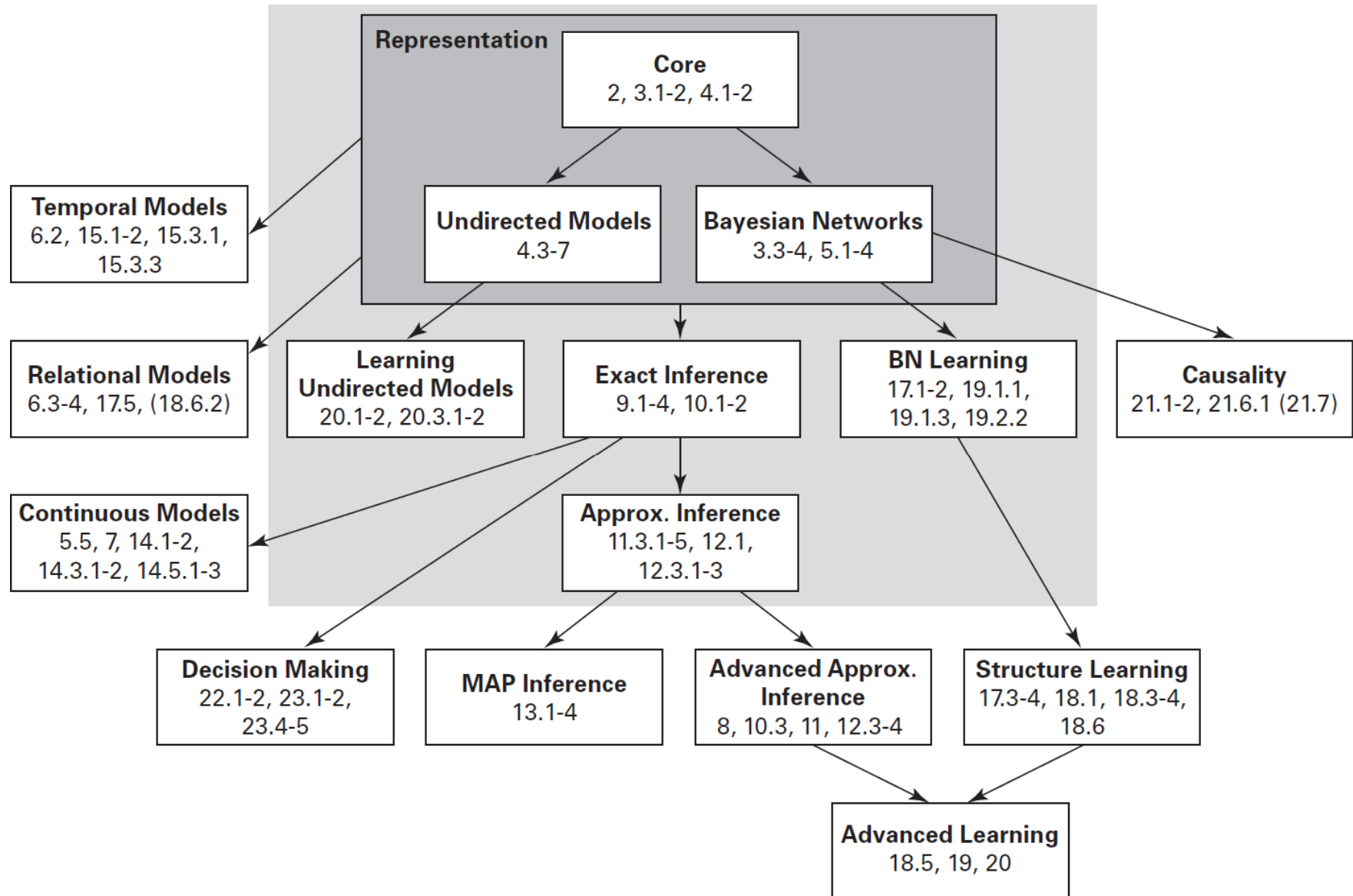
Course Objectives

- In-depth coverage of issues related to probabilistic reasoning. These include:
 - Probabilistic Representations (~ 4 Weeks)
 - Bayesian networks, undirected graphs, dynamic networks
 - Probabilistic inference (~ 4 Weeks)
 - Exact and approximate, including for temporal graphs
 - Learning of parameters and structure of probabilistic graphical models (~ 3 Weeks)
 - Decision making under uncertainty (~ 2 Weeks)
- First two topics will get the most attention. There are other courses that cover learning and planning in more detail.
- Focus on concepts and algorithms, not applications or commercial systems

Syllabus in terms of Book Sections

- Note: This is only a plan, actual coverage may vary some. Not all material in each section may be covered and some external material may be included.
- Representations: Chapters 2-5 all except sections marked with “*” in the book, Chapter 6: 6.1, 6.2 only
- Inference: Chapter 9 (except 9.5 and 9.6), 10, 11.1 to 11.3, 12.1 to 12.3, 13.1 to 13.3, 15.1, 15.2; additional notes
- Parameter Estimation: 17.1, 17.2 (exclude 17.2.4, 17.2.5), 19.2.2 (exclude 19.2.2.5, 19.2.2.6), Additional Notes
- Decision Theory: Ch. 22
- Selected parts of Ch. 7, 14, 11.4, 23

Book Plan



Course Style

- Interactive to the extent possible
- Will follow book closely; however, we will skip some details such as proofs of most theorems.
 - Assignments may require more detailed knowledge than covered in class
 - Preliminary version of lecture slides will be posted in advance of the lectures
- We will discuss algorithms at a relatively high level, almost never at the code or data structure levels
 - In English, in pseudo-code, by examples
 - Ability to convert high level descriptions to code is assumed

Reasoning under Uncertainty

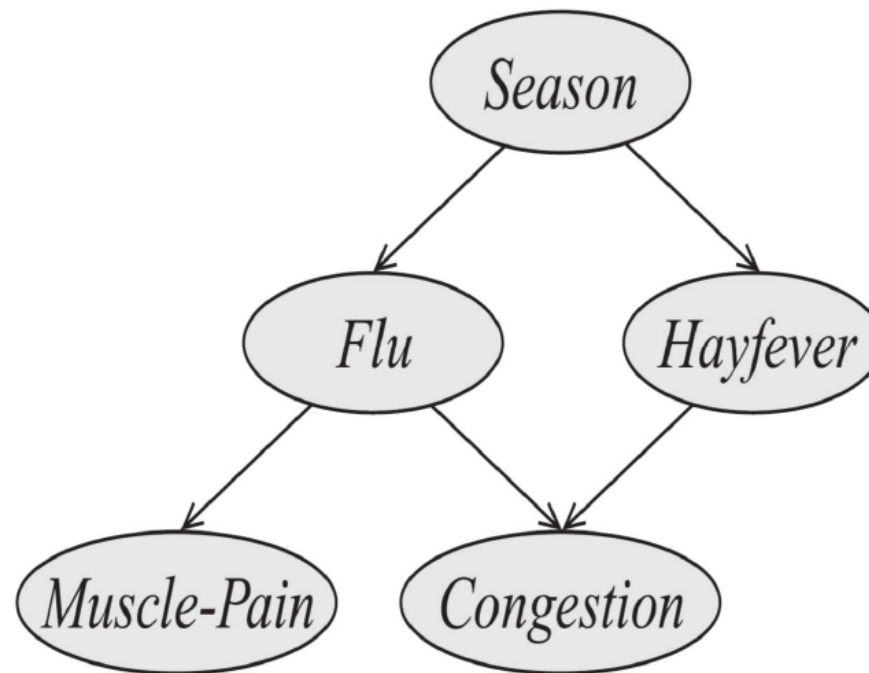
- Uncertainty is almost always present in solving real problems
 - State of the world is not known precisely or not even knowable in principle
 - Some aspects of the state can't be measured directly (*e.g.* cause of some types of sickness)
 - Effects of actions are uncertain
 - *e.g.* What route to take to go to the airport? When to start?
What courses to take to succeed in a cs career?
- Rational decision (under uncertainty)
 - Consider the relative importance of various goals and the *likelihood* that they will be achieved.
 - Rationality does not *guarantee* success

Possible Application Areas

- Originally developed for “expert systems”
 - Medical diagnosis (Pathfinder), Prospector...
 - Attempt to systematize reasoning about uncertain knowledge
- Now, virtually all aspects of computer science
 - AI, robotics, vision, speech
 - e-commerce, search....
 - Networks, OS, software engineering...
- Outside CS
 - Economics, finance, weather prediction, political science....
- Likely to become as important in CS study as discrete algorithms taught in courses such as cs570/670

An Example Graph

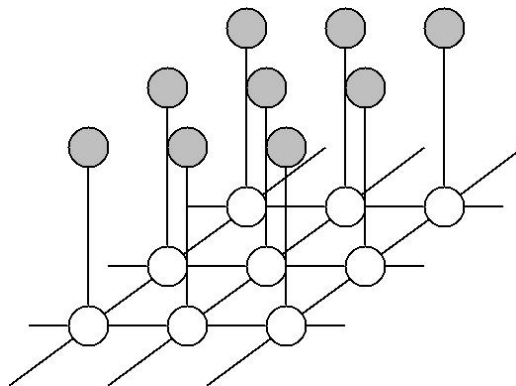
- Note: only the *structure* of relations is shown
- Methodology attempts to combine rule-based representations with probabilistic reasoning



Denoising an Image



Observed, noisy image



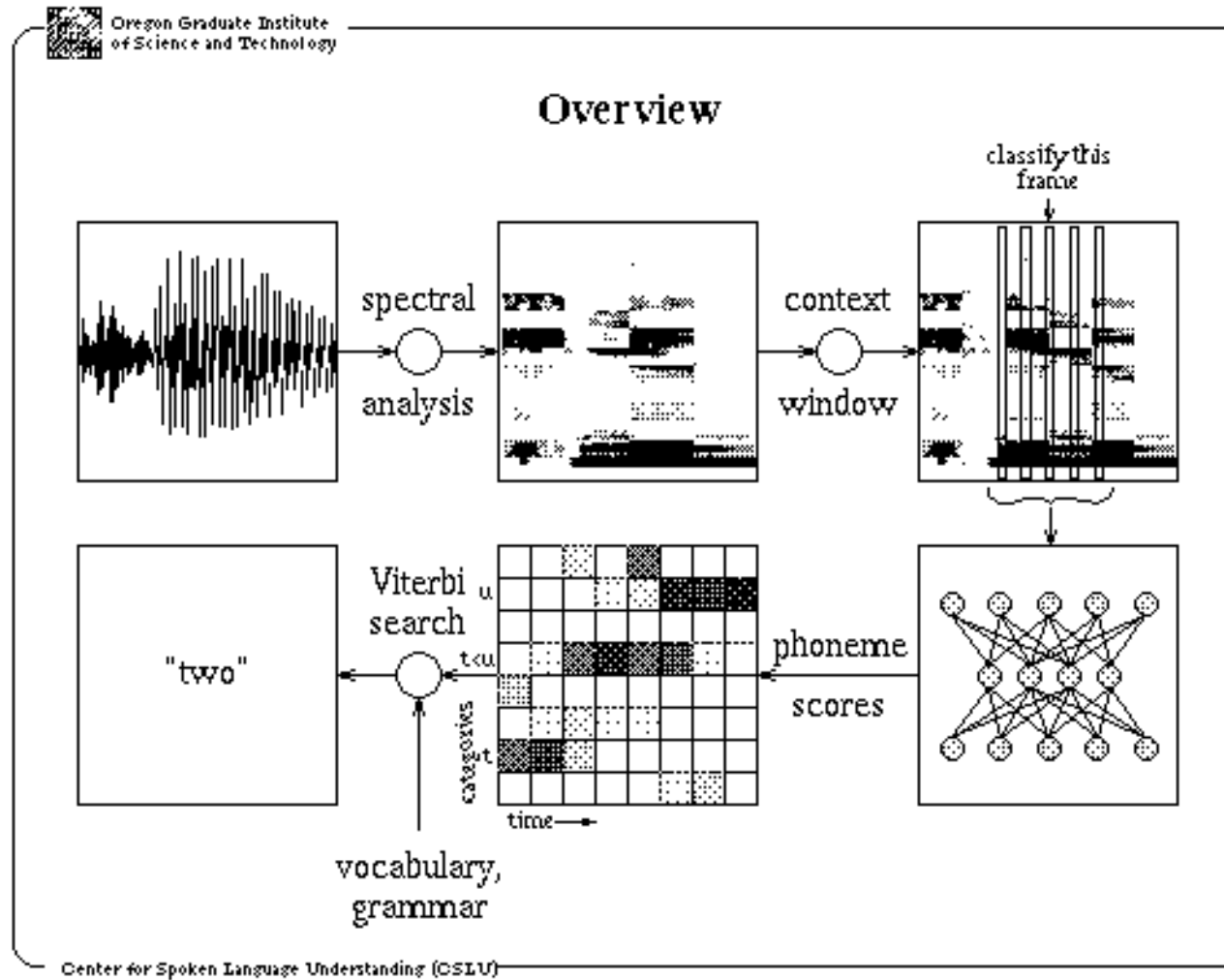
Model



Estimated Image

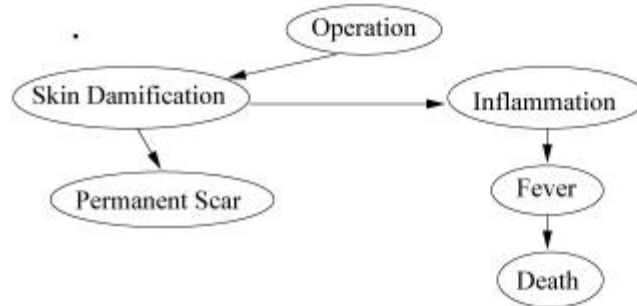
From: http://homepages.inf.ed.ac.uk/rbf/CVonline/LOCAL_COPIES/AV0809/ORCHARD/

Speech Recognition

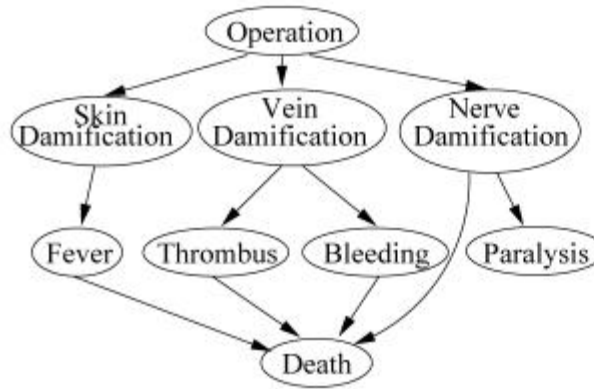


http://www.cslu.ogi.edu/tutordemos/nnet_recog/overview.gif

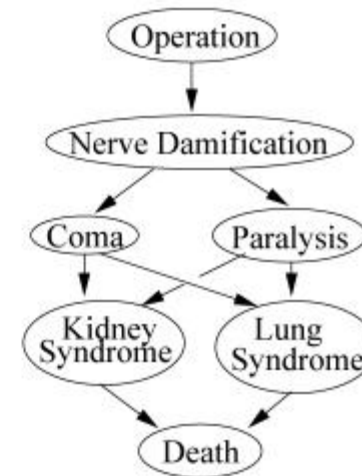
Medical Diagnosis



(a) From dermatology textbook



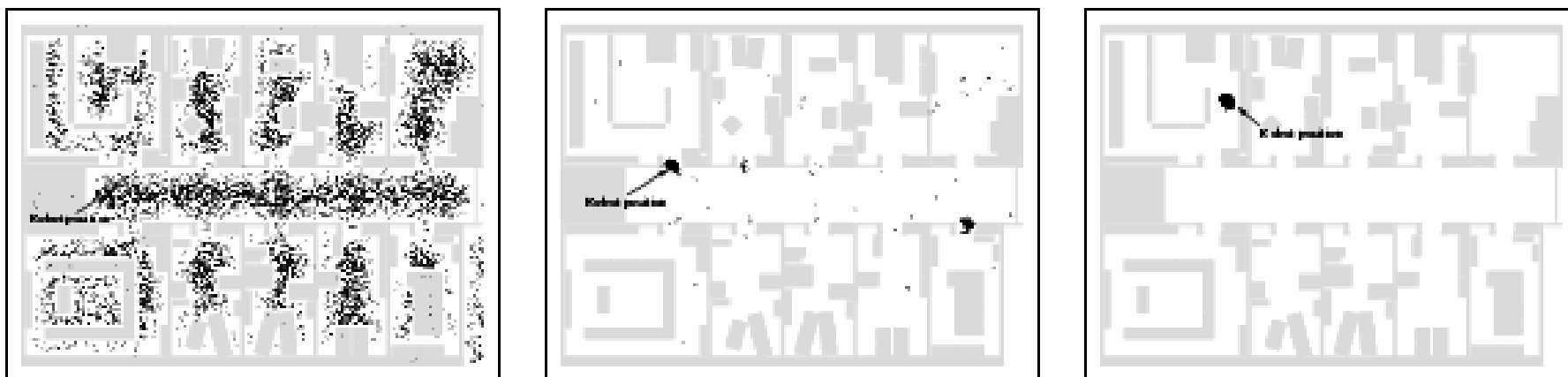
(b) From neurology data set



(c) From domain expert

From C. Jiang et al: AMIA Annual Proceedings 2005, 370-374

Robot Localization



http://www.cc.gatech.edu/~dellaert/assets/images/autogen/a_sonar.gif

Nature of Study

- Develop a representation for a problem domain
 - We will not study specific domains, just the methodologies
 - Will normally consist of choice of *random variables* and relations between them, represented in a graph
- Given values of some variables, compute probability distributions of others. Some types of *queries*:
 - *Forensic/diagnostic*: causes given evidence
 - *Predictions*: observables given cause
 - *Explanations*: of observed phenomenon
 - *Actions*: optimal actions given a model and observations
- Learning of the parameters (sometimes also the structure) of the graph from examples

Basic Probability: Informal concepts

- *Unconditional* or *prior* probability that a proposition A is true
 - Let P (the event of rain falling on jan 12 in L.A. is True) = 0.2
 - $P(\text{fair_coin_toss:head}) = 0.5$
- *Conditional* probability $P(\text{rain_today}|\text{cloudy_today})$
- *Joint* probability $P(\text{rain_Jan12}, \text{cloudy_Jan12})$
- *Independence* of variables: coin toss and weather

Probability Theory: Some notations

- Event *space*, space of all possible outcomes, Ω
 - For outcome of roll of dice: $\Omega = \{1,2,3,4,5,6\}$
 - Each event is a subset of Ω , e.g. $\{3\}$, $\{2,4,6\}$ (even outcome)
- Set of measurable events: S
 - We assign probabilities to elements of S
 - Contains *empty event* 0 and *trivial event* Ω
 - Closed under union (if α and $\beta \in S$, then so is $\alpha \cup \beta$)
 - If $\alpha \in S$, so is $\Omega - \alpha$

Probability Distributions

- Probability distribution P defined over (Ω, S) :
 - Mapping from events in S to real values (probabilities)
$$P(\alpha) \geq 0 \text{ for all } \alpha \in S$$
$$P(\Omega) = 1$$

If $\alpha, \beta \in S$, and $\alpha \cap \beta = \emptyset$, then $P(\alpha \cup \beta) = P(\alpha) + P(\beta)$
- It follows that $P(\emptyset) = 0$ and
$$P(\alpha \cup \beta) = P(\alpha) + P(\beta) - P(\alpha \cap \beta)$$
- Common interpretation of probability is as frequency of events
 - Examples: coin toss, dice roll, weather (how many outcomes?)

Conditional Probability, Bayes' Rule

- Conditional probability: $P(\beta | \alpha)$
 - Probability that β is true, given that α is true
 - *e.g.* $P(\text{rain}|\text{cloudy})$, $P(\text{gradeA}|\text{high_intell})$
 - $P(\beta | \alpha) = P(\alpha \cap \beta) / P(\alpha)$
- Chain rule: $P(\alpha \cap \beta) = P(\alpha) P(\beta | \alpha)$

$$P(\alpha_1 \cap \dots \cap \alpha_k) = P(\alpha_1)P(\alpha_2 | \alpha_1) \cdots P(\alpha_k | \alpha_1 \cap \dots \cap \alpha_{k-1}).$$

- Bayes' rule $P(\alpha | \beta) = P(\beta | \alpha) P(\alpha) / P(\beta)$
 - It may be easier to gather $P(\beta | \alpha)$ than $P(\alpha | \beta)$, for some situations (*e.g.* probability of symptoms given disease rather than the disease given symptoms)

$$P(\alpha | \beta \cap \gamma) = \frac{P(\beta | \alpha \cap \gamma)P(\alpha | \gamma)}{P(\beta | \gamma)}$$

Random Variables

- Random variables take on different values with probabilities given by a distribution function
 - *e.g.* coin toss, roll of dice, grades in a course *etc*
 - Formally, defined by function that associates a real value to each outcome in Ω .
 - Random variables normally denoted by upper case letters $X, Y, Z...$
- Discrete random variable: takes one of a finite set of values: $Val(X)$ denotes the set of values of X
- $P(X = x^i)$ denotes the probability that X takes value x^i
- Often abbreviated to $P(x^i)$
 - \sum_x denotes summation over all possible values of X
 - Sum over all possible values must equal 1 for a discrete variable, *i.e.* $\sum_x P(x) = 1$
 - Distribution is called multinomial
 - Binomial or Bernoulli for a binary variable
- Bold letters used to denote a *set* of variables, *e.g.* $\mathbf{X}, \mathbf{Y}, \mathbf{Z}...$
 - $\mathbf{x}, \mathbf{y}, \mathbf{z}$ denote values of variable in these sets

Marginal and Joint Distributions

- *Joint distribution*: probabilities for each combination of values of the random variables.
- $P(x, y)$ is used to denote joint probability of $X = x$ and $Y = y$

Figure 2.1, example of $P(\text{Intelligence}, \text{grade})$

		<i>Intelligence</i>		
		<i>low</i>	<i>high</i>	
<i>Grade</i>	<i>A</i>	0.07	0.18	0.25
	<i>B</i>	0.28	0.09	0.37
	<i>C</i>	0.35	0.03	0.38
		0.7	0.3	1

- *Marginal distribution*: Distribution of one variable, regardless of the values of others;
 - obtained by summing over all other variables from the joint distribution, *e.g.* $P(\text{Intelligence} = \text{high})$ or $P(\text{grade} = A)$;

Conditional Distribution

- $P(X | Y)$:
 - for each value of Y , assign a distribution over values of X .
- Chain rule: $P(X, Y) = P(X) P(Y | X)$

$$P(X_1, \dots, X_k) = P(X_1)P(X_2 | X_1) \cdots P(X_k | X_1, \dots, X_{k-1})$$

- Bayes' rule $P(X | Y) = P(X) P(Y | X) / P(Y)$

⊥

Independence

- Event α is independent of event β in P , denoted as $P \models \alpha \perp \beta$,
if $P(\alpha \mid \beta) = P(\alpha)$, or if $P(\beta) = 0$
- Follows that $P(\alpha \cap \beta) = P(\alpha) P(\beta)$
- Examples: toss two coins; coin toss and weather...
- Full independence is rare, *conditional independence* where two events are independent, given a third event
- Conditional independence
 - $P(\text{USC} \mid \text{UCLA}, \text{GradeA}) = P(\text{USC} \mid \text{GradeA})$
(USC means admitted to USC, similar for UCLA)
 - $P(\text{Congestion} \mid \text{Flu}, \text{Hayfever}, \text{Season}) = P(\text{Congestion} \mid \text{Flu}, \text{Hayfever})$
- Event α is independent of event β in P , given event γ , denoted as $P \models (\alpha \perp \beta \mid \gamma)$ if $P(\alpha \mid \beta \cap \gamma) = P(\alpha \mid \gamma)$, or if $P(\beta \mid \gamma) = 0$
- Follows that $P(\alpha \cap \beta \mid \gamma) = P(\alpha \mid \gamma) P(\beta \mid \gamma)$

Next Class

- Read sections 2.1, 2.2 and 3.1 of the KF book