CIS 471/571 (Fall 2020): Introduction Artificial Intelligence

Lecture 6: Adversarial Search WeChat: cstutorcs

Thanh H. Nguyen

Source: http://ai.berkeley.edu/home.html

Reminders

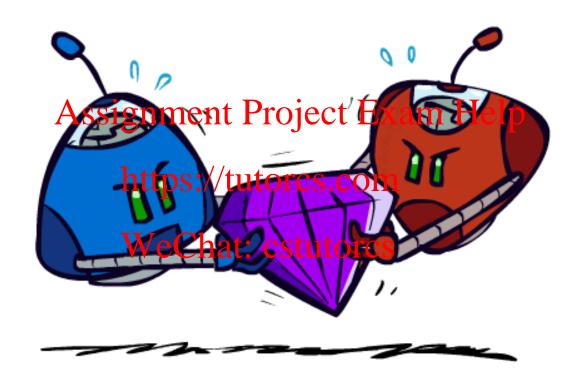
- Project 2:
 - Deadline: Oct 27th, 2020

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- Written assignmenht@s://tutorcs.com
 - Deadline: Oct 24th, 2020 chat: cstutorcs

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Adversarial Games



Types of Games

• Many different kinds of games!

•Axes:

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Deterministic or stochastic?

• One, two, or more players? https://tutorcs.com

Zero sum?

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Perfect information (can you see the state)?

• Want algorithms for calculating a strategy (policy) which recommends a move from each state

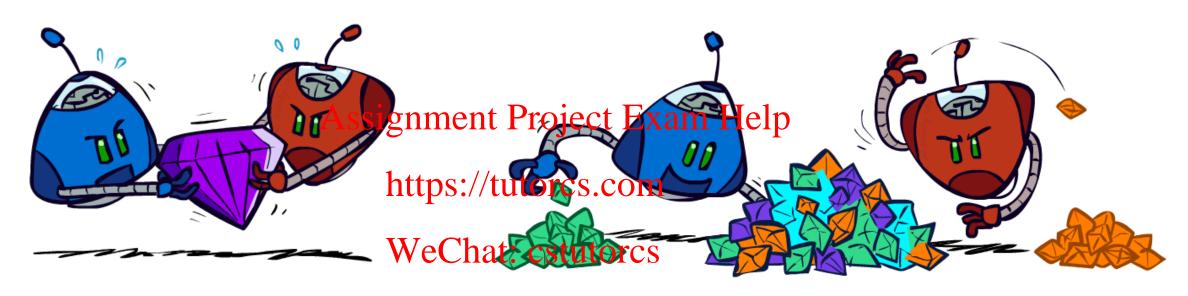
Deterministic Games

- Many possible formalizations, one is:
 - States: S (start at s₀)
 - Players: P={1...N} (uauallyntakettproject Exam Help
 - Actions: A (may depend on player / state)
 - Transition Function: SxAttps://tutorcs.com
 - Terminal Test: $S \rightarrow \{t,f\}$ WeChat: cstutorcs
 - Terminal Utilities: $SxP \rightarrow R$

• Solution for a player is a policy: $S \rightarrow A$



Zero-Sum Games



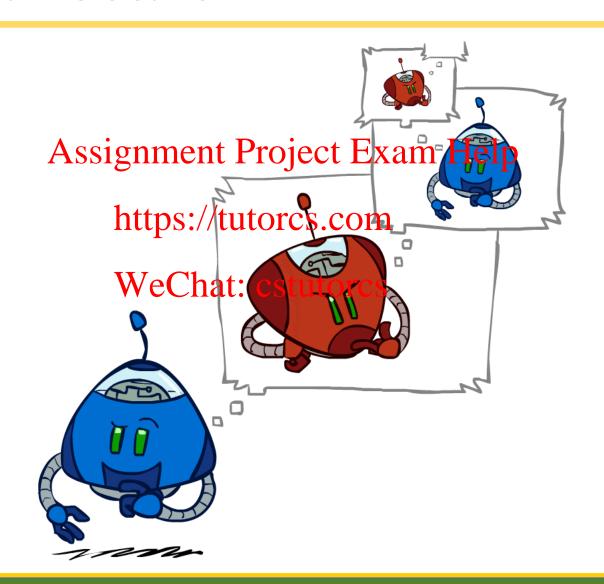
- Zero-Sum Games
 - Agents have opposite utilities (values on outcomes)
 - Lets us think of a single value that one maximizes and the other minimizes
 - Adversarial, pure competition

- General Games
 - Agents have independent utilities (values on outcomes)
 - Cooperation, indifference, competition, and more are all possible
 - More later on non-zero-sum games

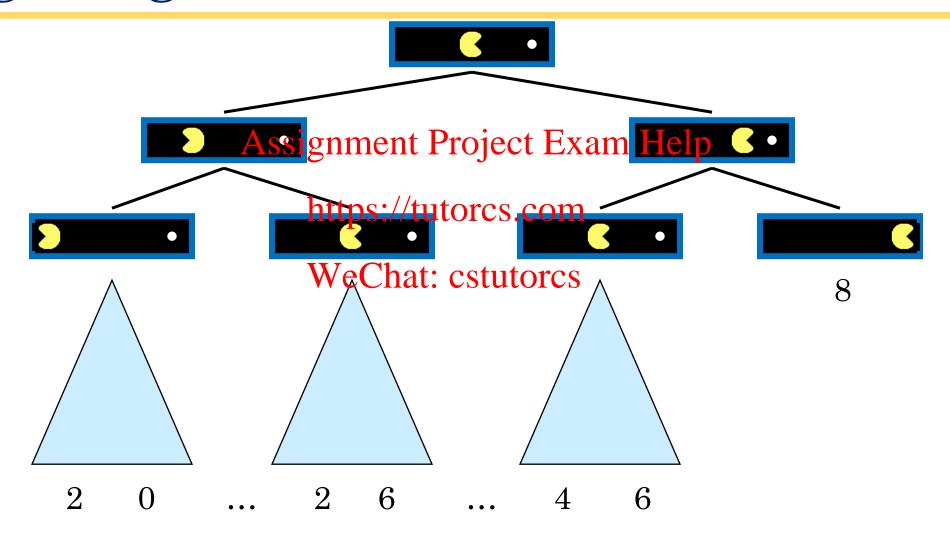
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Adversarial Search



Single-Agent Trees

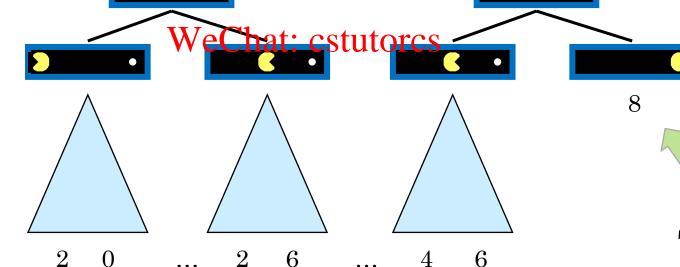


Value of a State

Value of a state:
The best achievable
outcome (utility)
from that state

Non-Terminal States:





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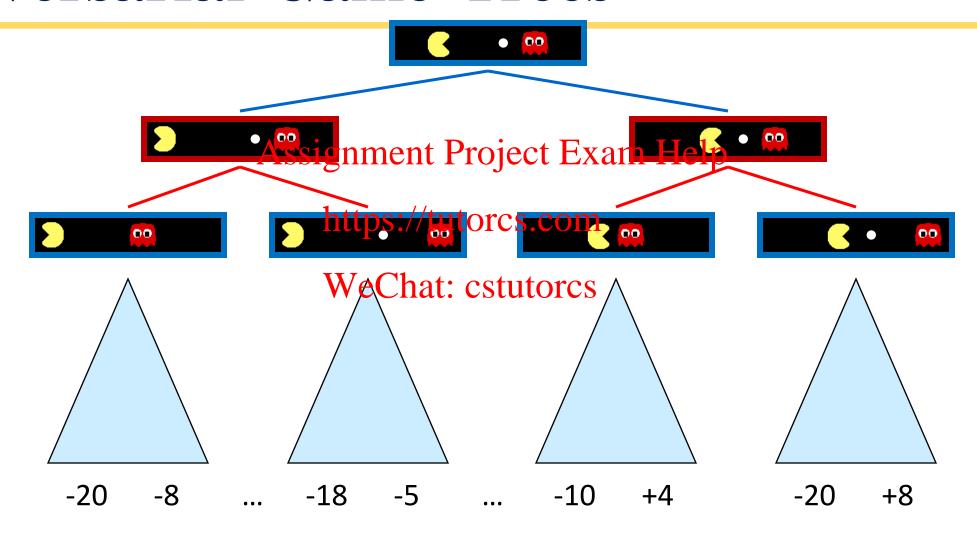
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Terminal States:

$$V(s) = \text{known}$$



Adversarial Game Trees



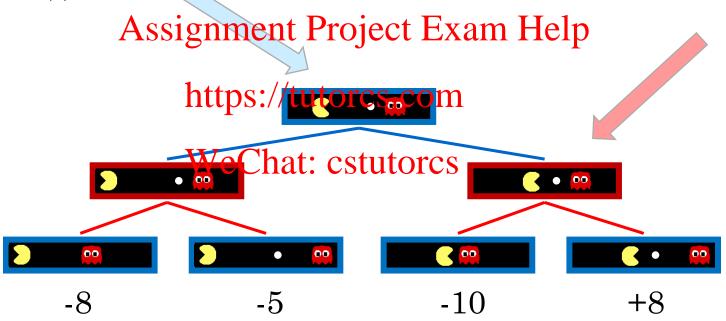
Minimax Values

States Under Agent's Control:

$$V(s) = \max_{s' \in \text{successors}(s)} V(s')$$

States Under Opponent's Control:

$$V(s') = \min_{s \in \text{successors}(s')} V(s)$$



Terminal States:

$$V(s) = \text{known}$$



Tic-Tac-Toe Game Tree



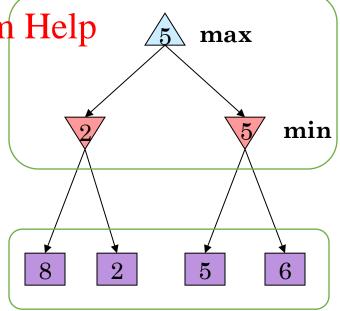
Adversarial Search (Minimax)

- Deterministic, zero-sum games:
 - Tic-tac-toe, chess, checkers
 - One player maximizes gresult Project Exam Help
 - The other minimizes result

https://tutorcs.com

- Minimax search: WeChat: cstutorcs
 - A state-space search tree
 - Players alternate turns
 - Compute each node's minimax value: the best achievable utility against a rational (optimal) adversary

Minimax values: computed recursively



Terminal values: part of the game

Minimax Implementation

```
def value(state):

if the state is a terminal state: return the state's utility

if the next agent is MIN: return min-value(state)

if the next agent is MIN: return min-value(state)

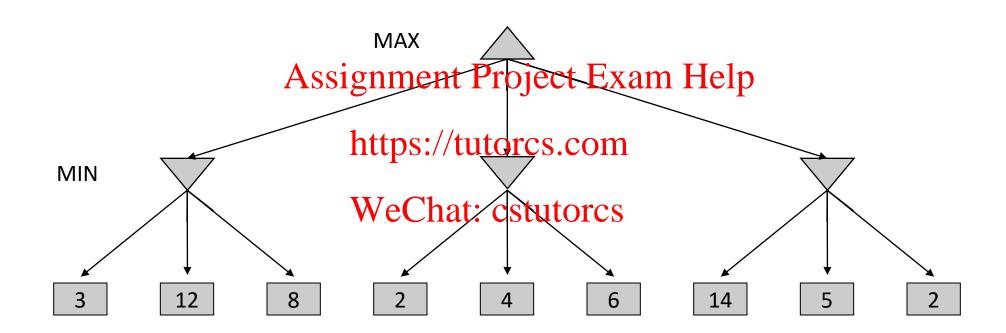
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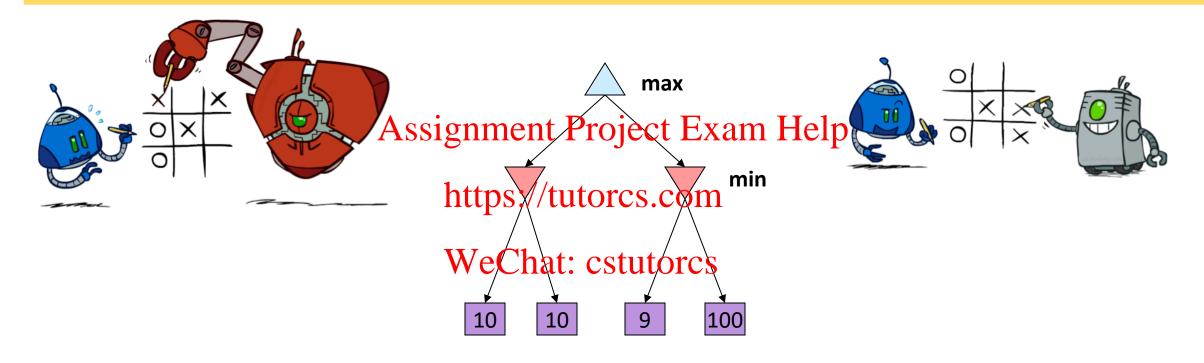
def max-value(state): initialize v = -∞ for each successor of state: v = max(v, value(successor)) return v

def min-value(state):
 initialize v = +∞
 for each successor of state:
 v = min(v, value(successor))
 return v

Minimax Example



Minimax Properties



Optimal against a perfect player. Otherwise?

Minimax Efficiency

• How efficient is minimax?

Just like (exhaustive) DFS

■ Time: O(b^m)

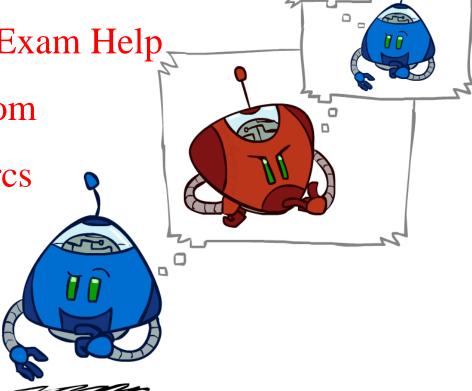
Space: O(bm)

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Exact solution is completely infeasible

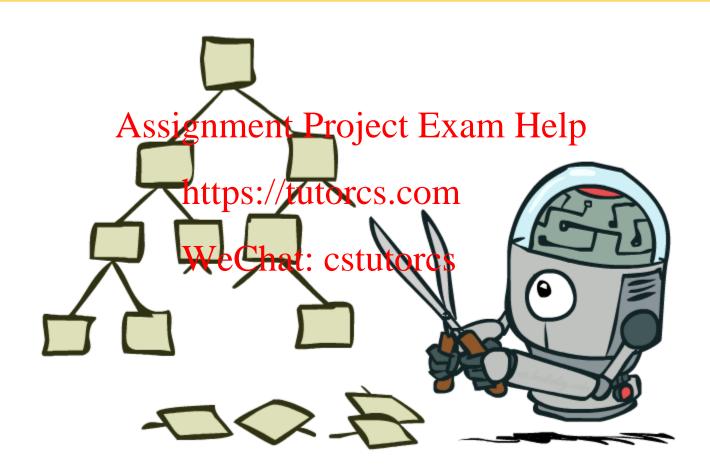
• But, do we need to explore the whole tree?



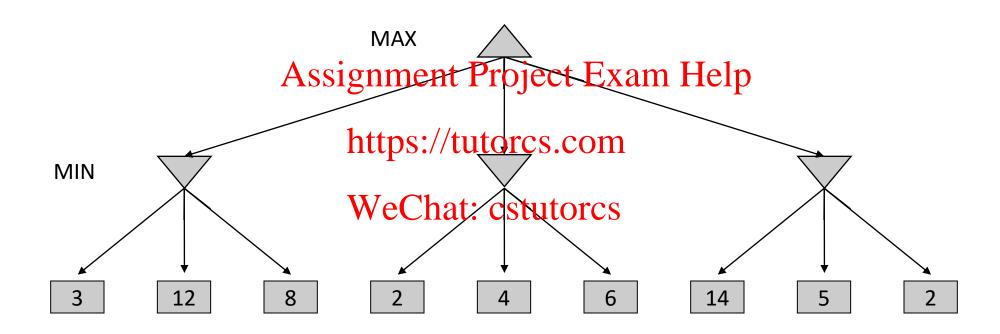
Resource Limits



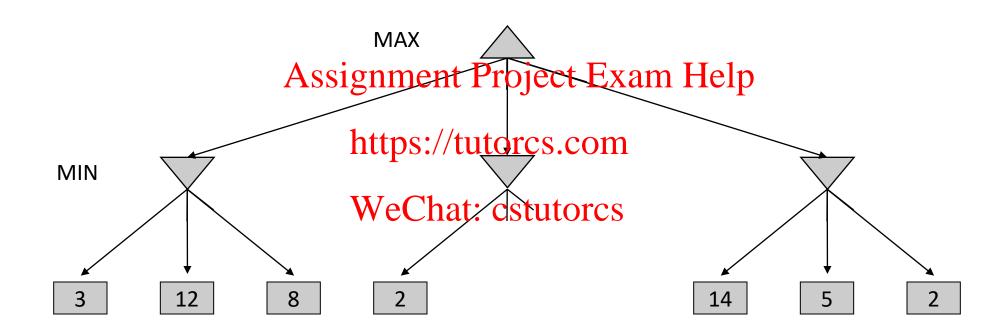
Game Tree Pruning



Minimax Example



Minimax Pruning



Alpha-Beta Pruning

- Alpha α: value of the best choice so far for MAX (lower bound of Max utility)
- Beta β: value of the best choice so far for MIN (upper bound of Min utility)
- Expanding at MAX nodesignmente Project Exam Help
 - If a child of **n** has value greater than β, stop expanding the MAX node **n**
 - Reason: MIN parent of **n** would not choose the action which leads to **n**

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- At MIN node n: update β
 - If a child of **n** has value less than α, stop expanding the MIN node **n**
 - Reason: MAX parent of n would not choose the action which leads to n

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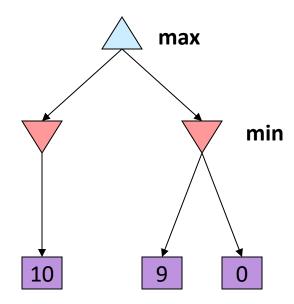


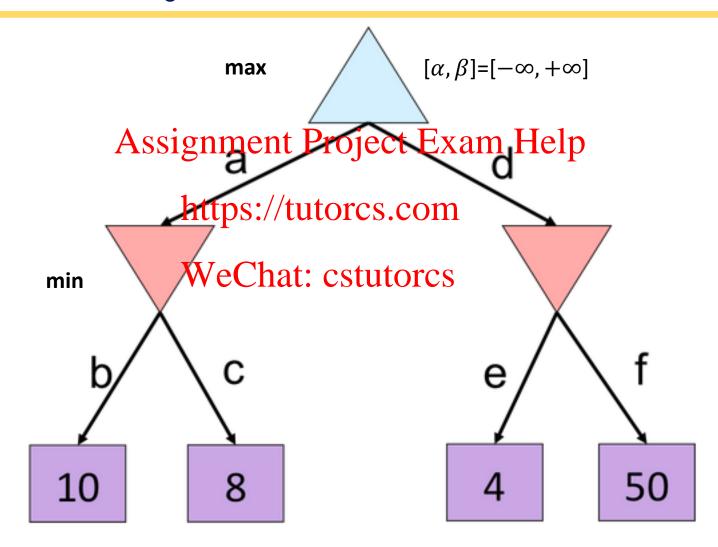
Alpha-Beta Implementation

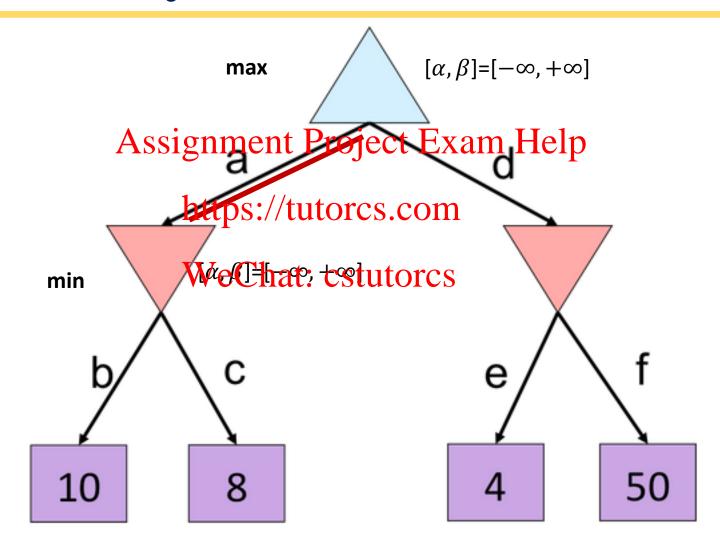
```
\begin{array}{ll} \text{def max-value(state, }\alpha, \beta): & \text{WeChat: } \text{cstudefanin-value(state, }\alpha, \beta): \\ & \text{initialize } v = -\infty \\ & \text{for each successor of state:} \\ & v = \max(v, \, \text{value(successor, }\alpha, \, \beta)) \\ & \text{if } v \geq \beta \, \, \text{return } v \\ & \alpha = \max(\alpha, \, v) \\ & \text{return } v \end{array} \qquad \begin{array}{ll} \text{initialize } v = +\infty \\ & \text{for each successor of state:} \\ & v = \min(v, \, \text{value(successor, }\alpha, \, \beta)) \\ & \text{if } v \leq \alpha \, \, \text{return } v \\ & \beta = \min(\beta, \, v) \\ & \text{return } v \end{array}
```

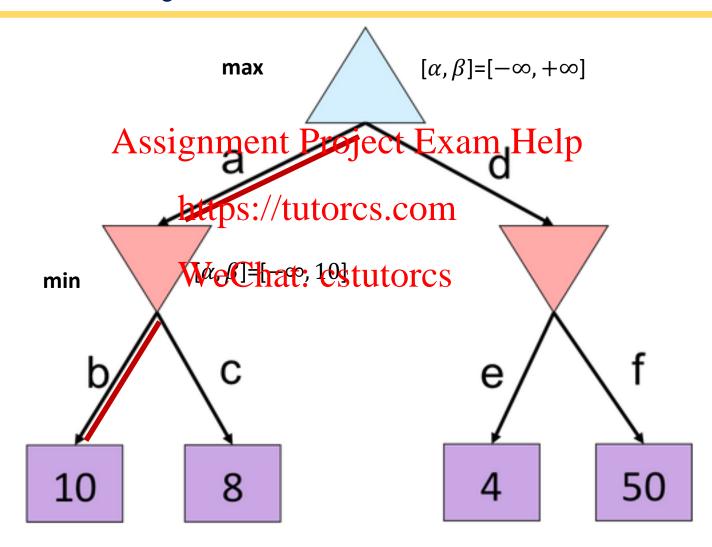
Alpha-Beta Pruning Properties

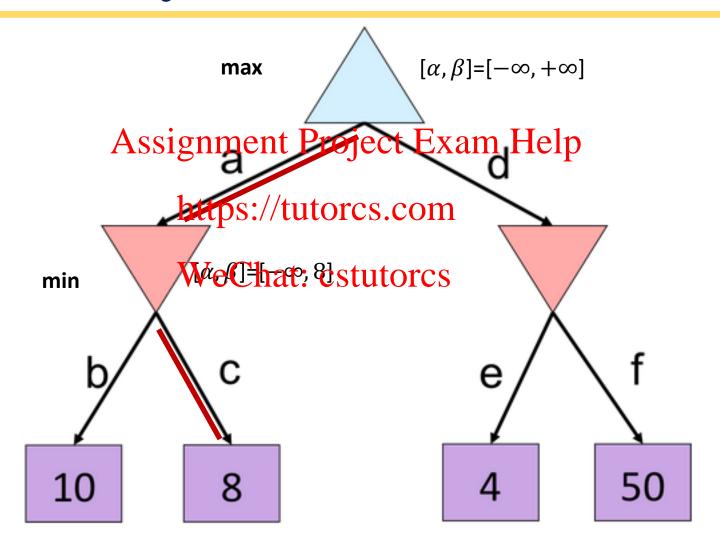
- This pruning has no effect on minimax value computed for the root!
- Values of intermediate no description of intermediate no des
 - Important: children of the root may have the wrong value
 - So the most naïve version workthets yout the action extension
- Good child ordering improves effectiveness of pruning

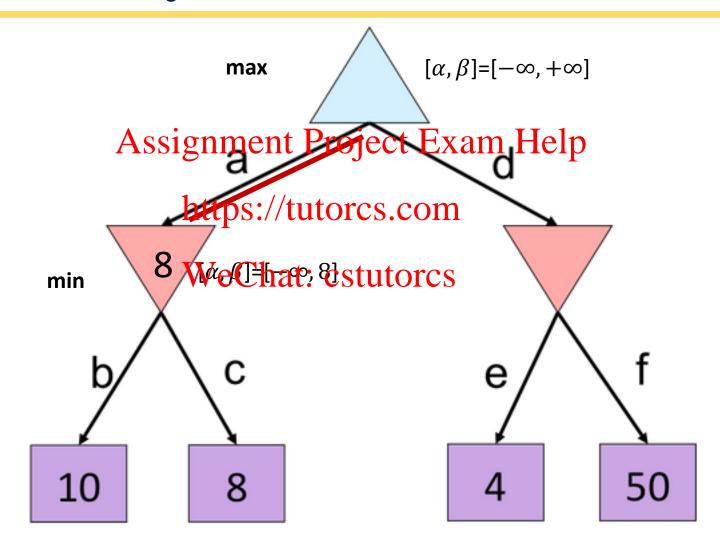


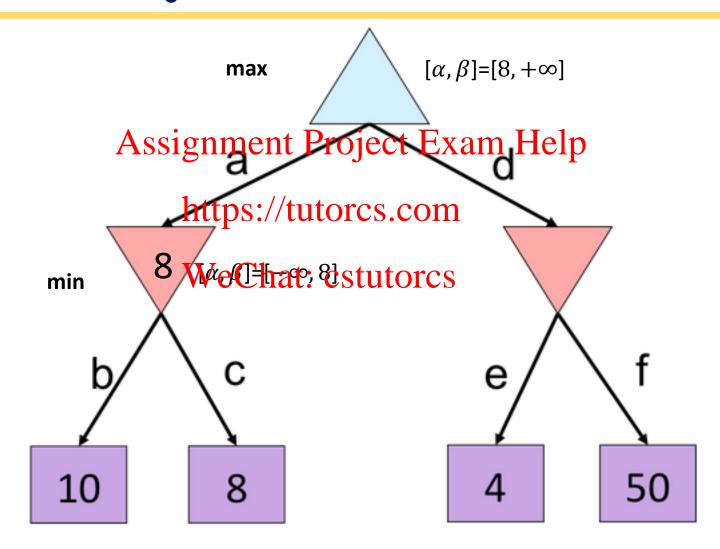


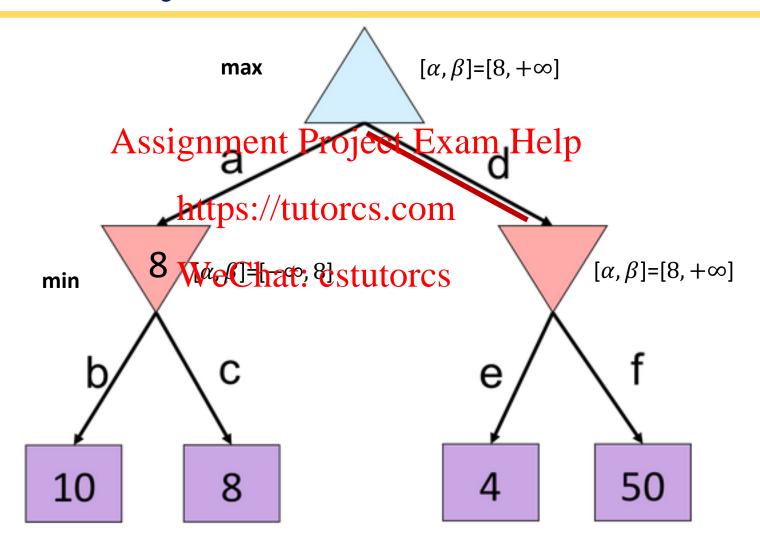


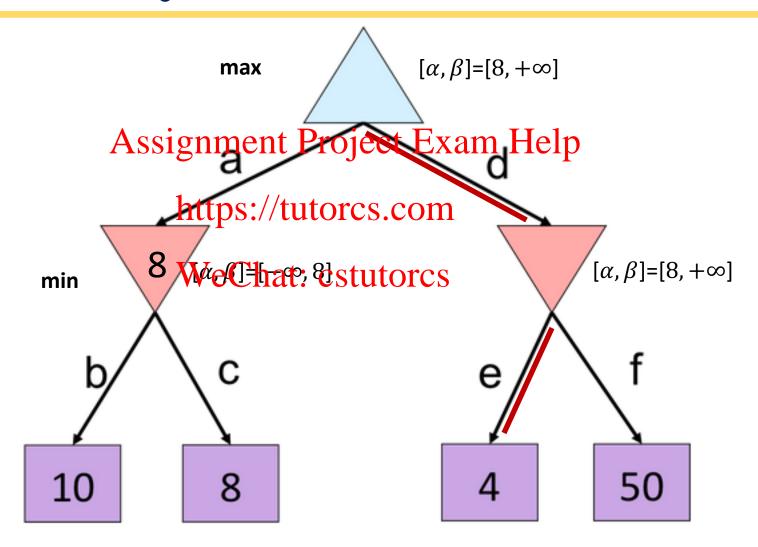


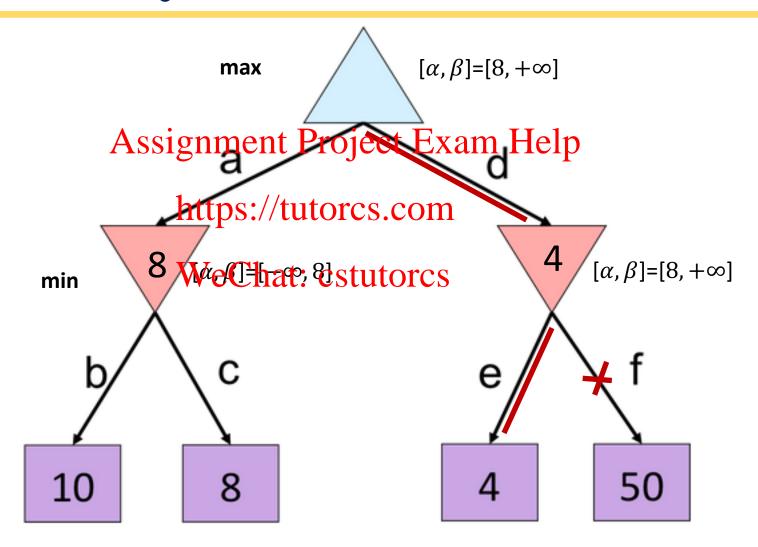


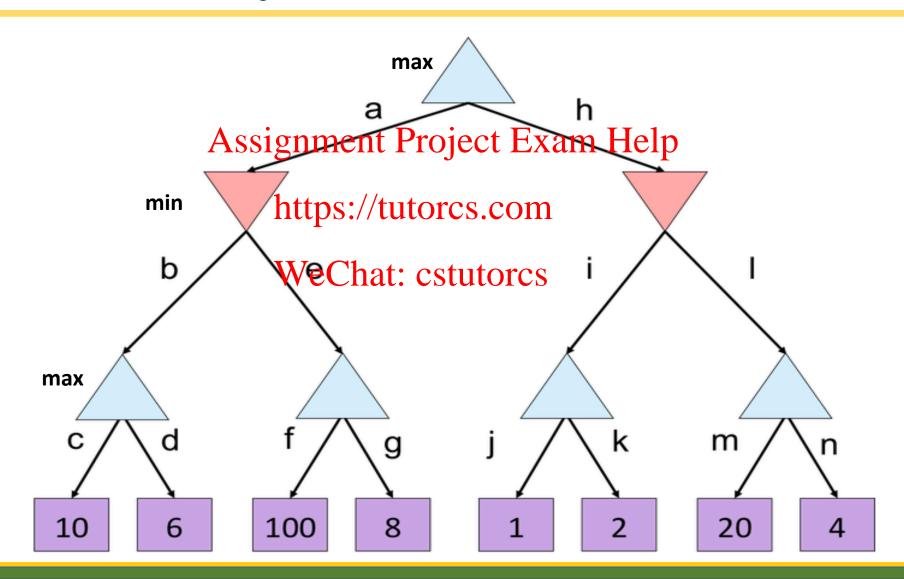


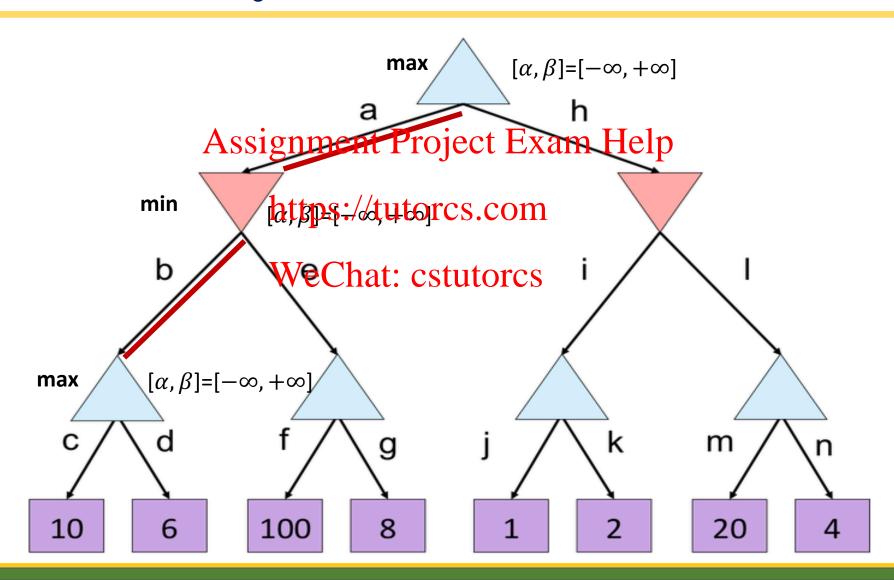


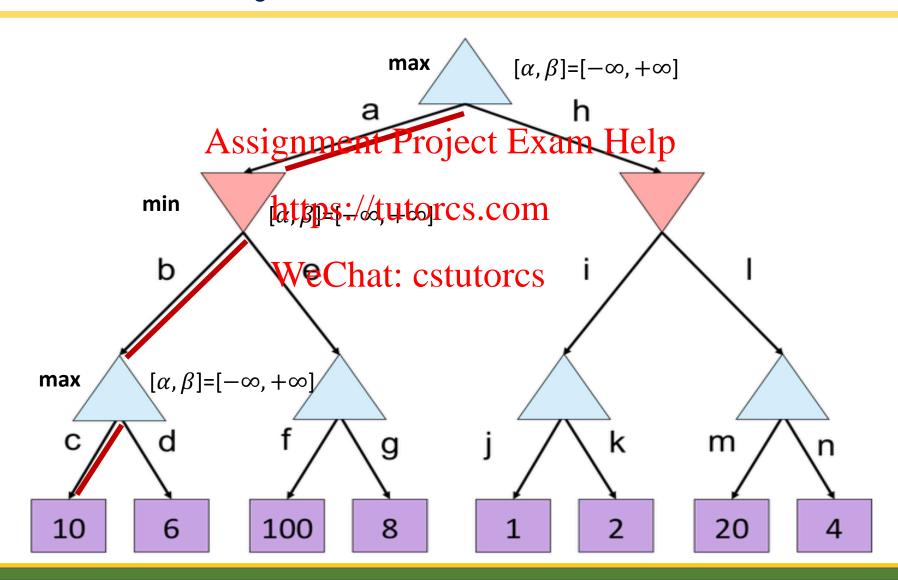


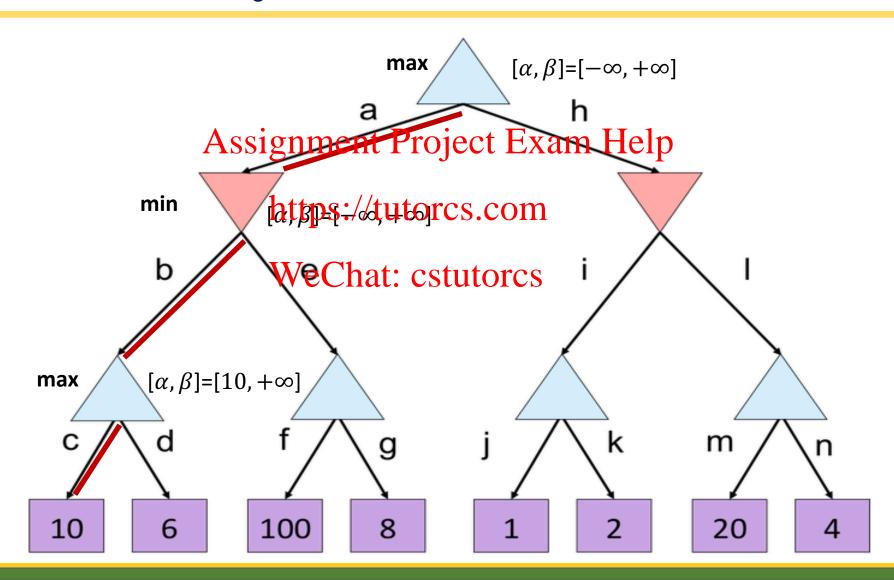


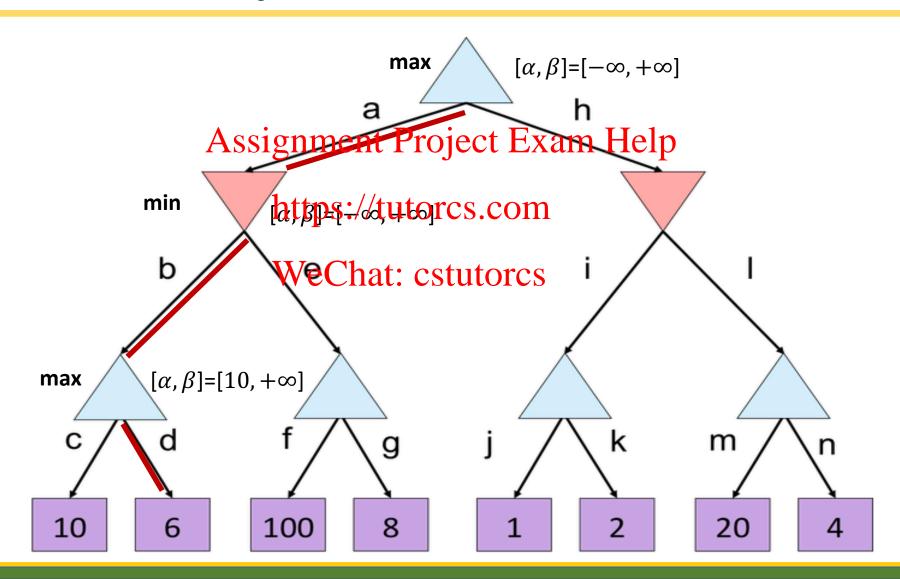


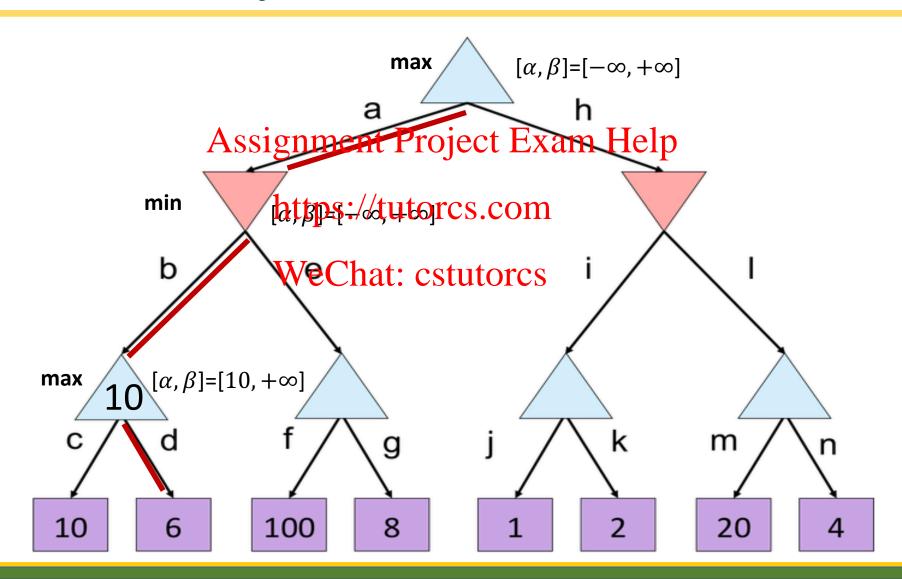


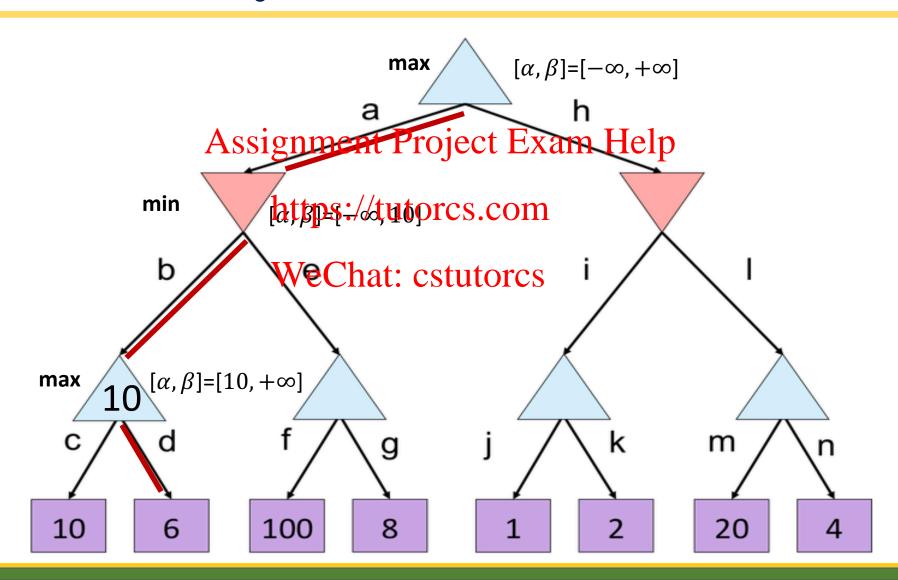


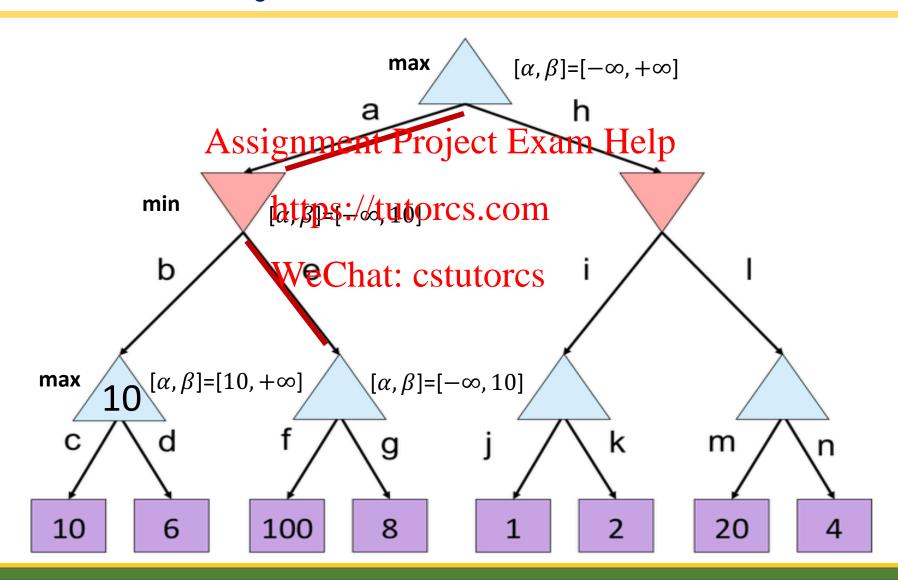


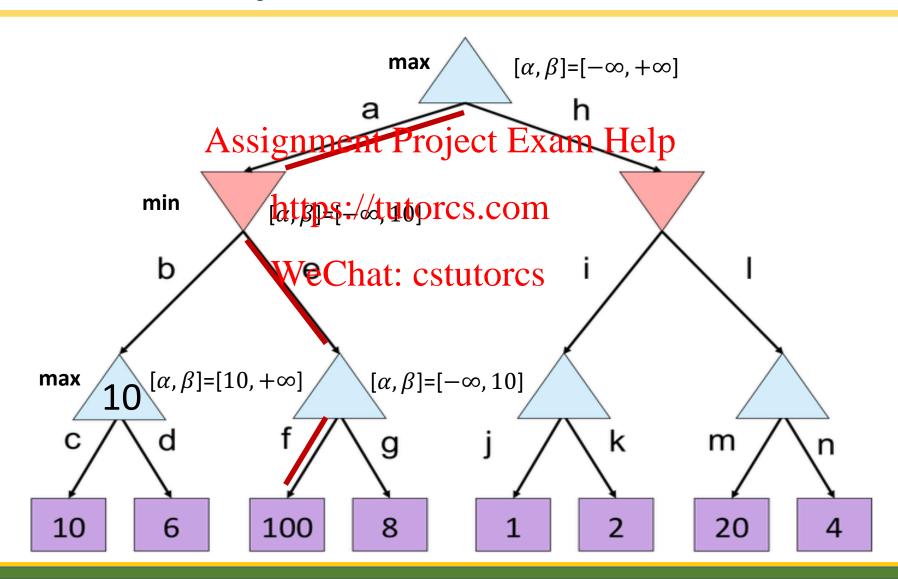


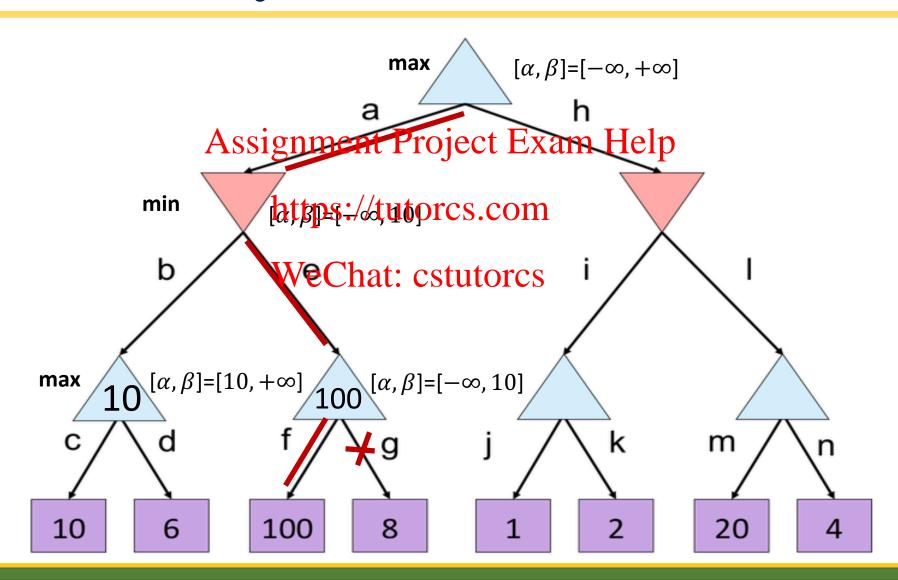


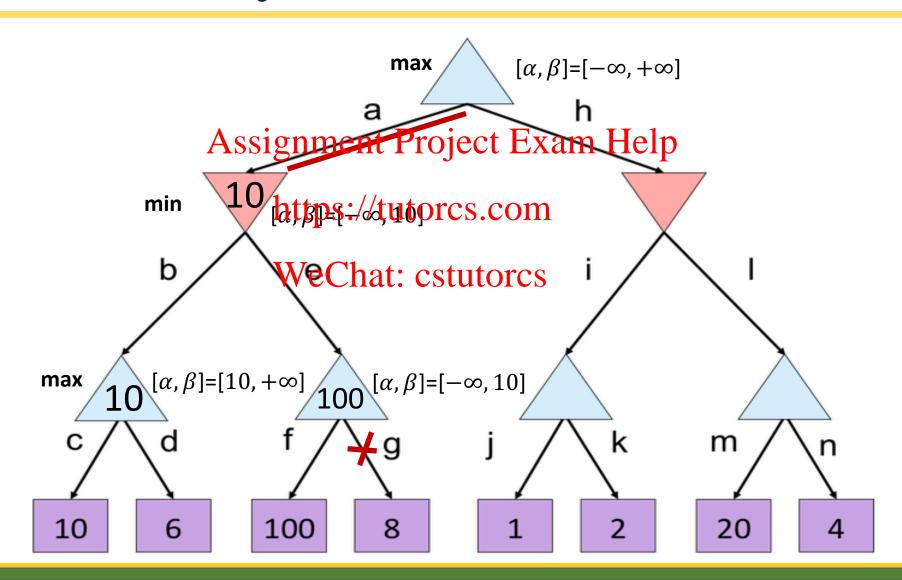


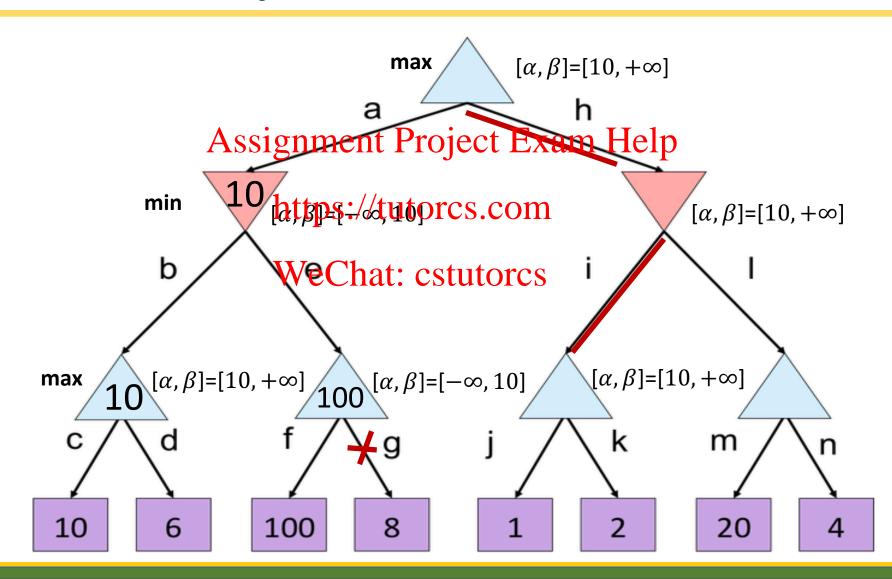


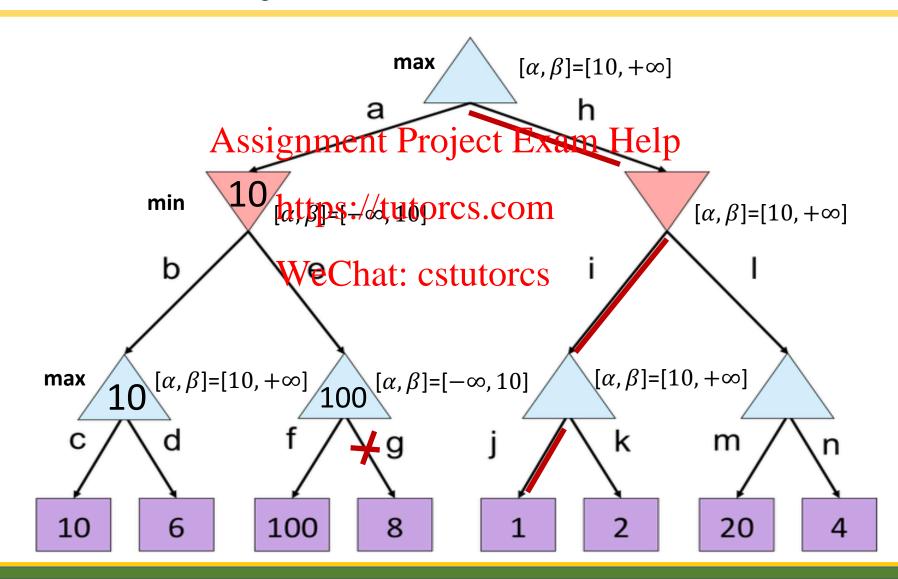


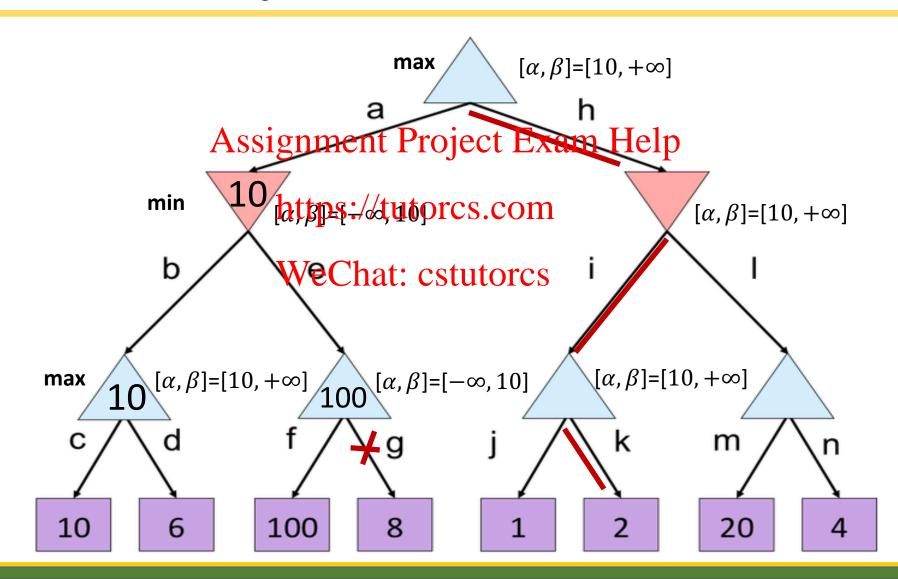


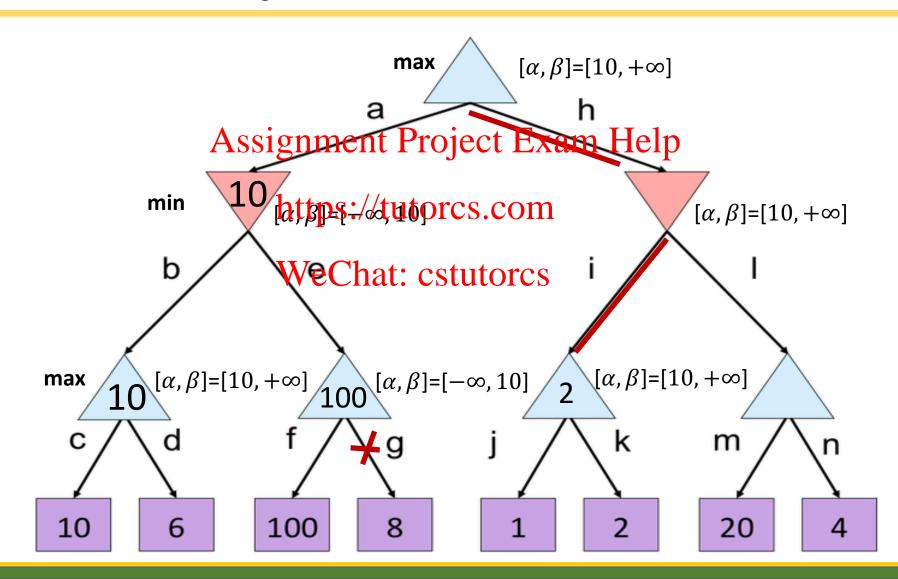


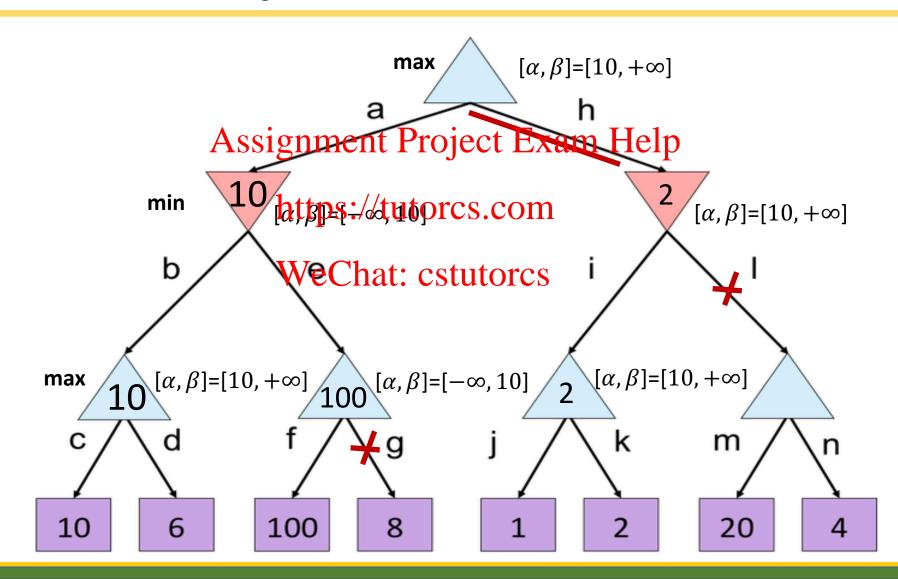


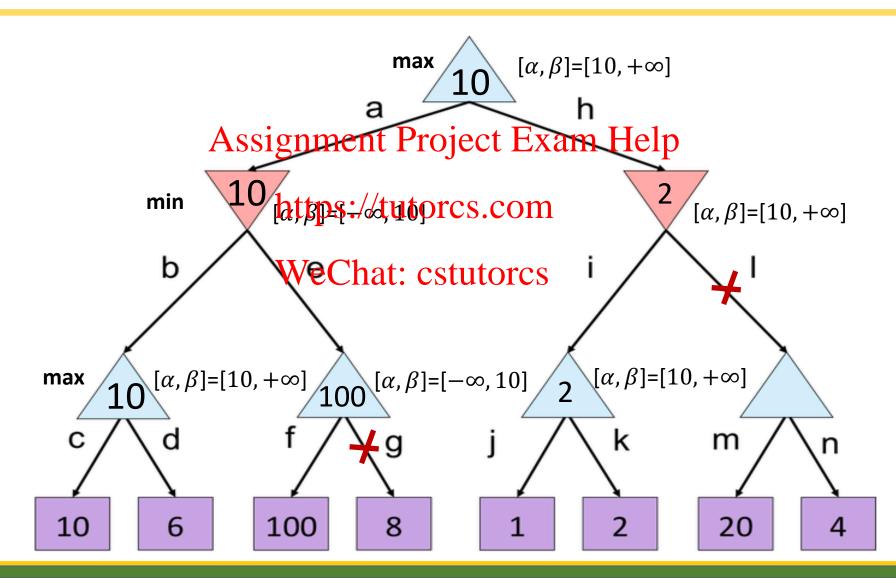












Resource Limits



Resource Limits

• Problem: In realistic games, cannot search to leaves!

• Solution: Depth-limited search

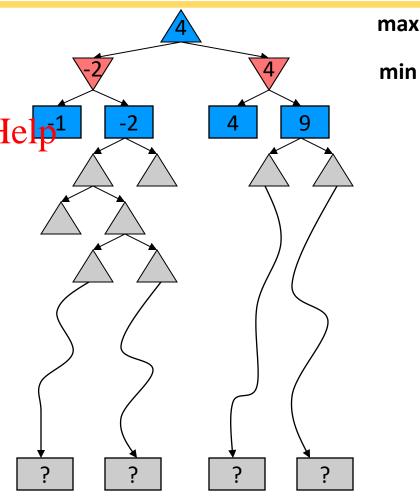
• Instead, search only to a limites signment recoject Exam Help1

Replace terminal utilities with an evaluation function for non-terminal positions
 https://tutorcs.com

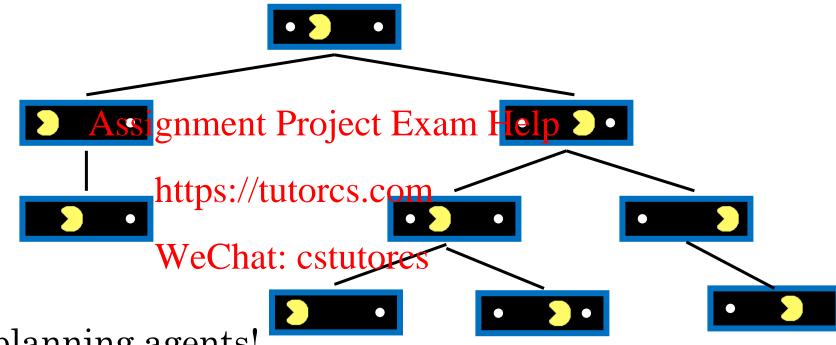
• Example:

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- Suppose we have 100 seconds, can explore 10K nodes / sec
- So can check 1M nodes per move
- α-β reaches about depth 8 decent chess program
- Guarantee of optimal play is gone
- More plies makes a BIG difference
- Use iterative deepening for an anytime algorithm

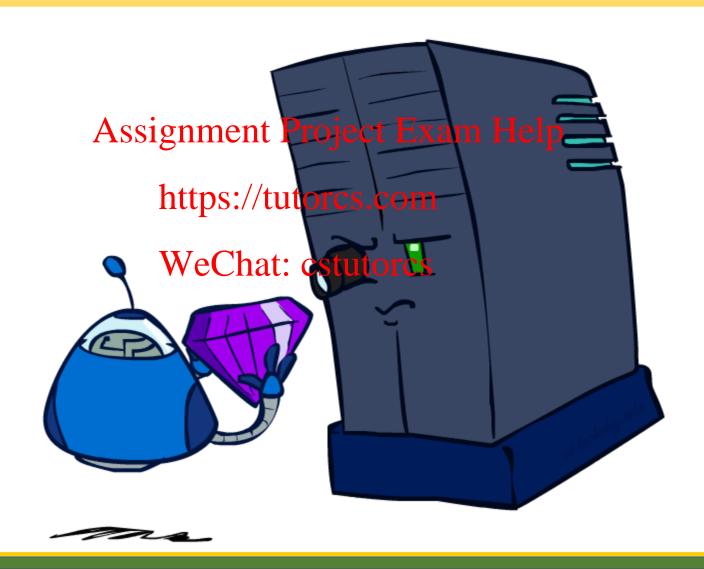


Why Pacman Starves



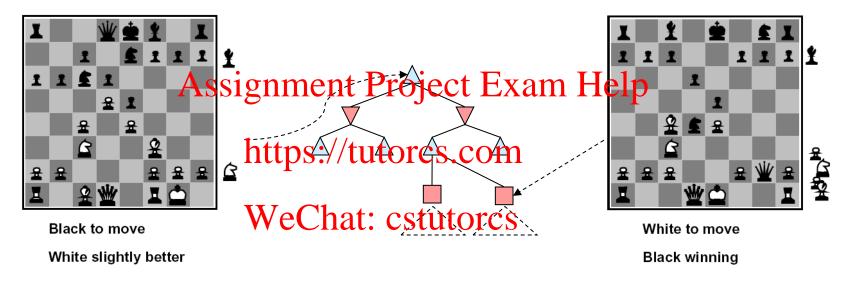
- A danger of replanning agents!
 - He knows his score will go up by eating the dot now (west, east)
 - He knows his score will go up just as much by eating the dot later (east, west)
 - There are no point-scoring opportunities after eating the dot (within the horizon, two here)
 - Therefore, waiting seems just as good as eating: he may go east, then back west in the next round of replanning!

Evaluation Functions



Evaluation Functions

• Evaluation functions score non-terminals in depth-limited search



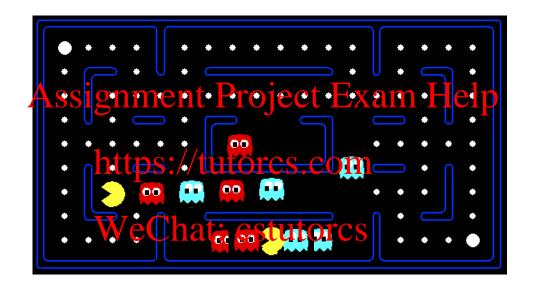
- Ideal function: returns the actual minimax value of the position
- In practice: typically weighted linear sum of features:

$$Eval(s) = w_1 f_1(s) + w_2 f_2(s) + \dots + w_n f_n(s)$$

• e.g. $f_1(s)$ = (num white queens – num black queens), etc.



Evaluation for Pacman

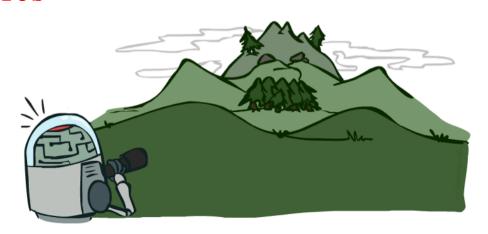


Depth Matters

 Evaluation functions are always imperfect

• The deeper in the the ighment Project Execution function is buried, the less the quality of the evaluation function matternat: cstutorcs

• An important example of the tradeoff between complexity of features and complexity of computation



Synergies between Evaluation Function and Alpha-Beta?

- Alpha-Beta: amount of pruning depends on expansion ordering
 - Evaluation function can provide guidance to expand most promising nodes first (which later makes it more likely there is already a good alternative on the path to the root)
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 - (somewhat similar to role of A* heuristic, CSPs filtering) https://tutorcs.com
- Alpha-Beta: (similar for Wodeshof: write torax swapped)
 - Value at a min-node will only keep going down
 - Once value of min-node lower than better option for max along path to root, can prune
 - Hence: IF evaluation function provides upper-bound on value at min-node, and upper-bound already lower than better option for max along path to root THEN can prune