Assignment 1: Chapters 1, 2, Game Theory. (Solutions)

NB: The clarity of your answers was considered when grading.

Chapter 1. Al Foundations. 21 points total.

1. (5 points) Consider these two statements.

A symptom who the tell hex am Help

"Therefore animals cannot be intelligent"

Is the first statement/type, and does it imply the second? nups://tutores.com

The point of this exercise is to notice the parallel with the next one. Whatever you decide about whether computers could be intelligent in 2, you are committed to making the same conclusion about animal (including humans); will syryour reasons for deciding whether something is intelligent take into account the mechanism (programming via genes versus programming via a human programmer). Note that Searle makes this appeal to mechanism in his Chinese Room argument (see Chapter 26).

- 2. (5 points) Consider these two statements.
 - "Computers can do only what their programmers tell them".
 - "Therefore computers cannot be intelligent"

Is the first statement true, and does it imply the second?

This depends on your definition of "intelligent" and "tell." In one sense computers only do what the programmers command them to do, but in another sense what the programmers consciously tells the computer to do often has very little to do with what the computer actually does. Anyone who has written a program with an ornery bug knows this, as does anyone who has written a successful machine learning program. So in one sense Samuel "told" the computer "learn to play checkers better than I do, and then play that way," but in another sense he told the computer "follow this learning algorithm" and it learned to play. So we're left in the situation where you may or may not consider learning to play checkers to be a sign of intelligence (or you may think that learning to play in the right way requires intelligence, but not in this way), and you may think the intelligence resides in the programmer or in the computer.

NB: For questions 1 and 2, you were given full grade if your reasoning about intelligence was consistent for both animals and computers or at least if you clearly explained that you assume the mechanism (genes vs computer) matters.

3. (5 points) For a given agent function, is there at most one agent program that implements a given agent function? If you answer "yes", show why there is at most one agent program, or if you answer "no", give an example of how there can be two or more.

The answer is "no" and you could provide any reasonable example. For instance, assume we are given an agent function whose actions only depend on the previous p percepts. One program can remember the previous p percepts to implement the agent function, while another could remember greater than p percepts and still implement the same agent function.

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4. (6 points) Match the following concepts/statements with a discipline related to AI. Give your answer by filling in letters in the table provided. For example, if you think that "Statistics" best that the "Decision Theory" put a "b" into the empty square next to "Decision Theory".

W. C	a. Philosophy
WeC	Balither Basci Utores
	c. Economics
	d. Statistics
	e. Psychology
	f. Homeostasis
The mind operates	a
according to rules.	
Decision Theory	c
Laws of probability	d
Behaviourism	e
Computation Theory	Ъ
Control Theory	f

4. a. (6 points) Fill in the table below for Watson to describe its environment when Watson plays Jeopardy. This question refers to Watson as we observed the system in the Youtube video. Briefly explain your answer.

Observable	Agents	Deterministic	Episodic	Static	Discrete

Observable	Agents	Deterministic	Episodic	Static	Discrete
Partially	multi	Yes (answer is	Yes	Semi	Yes
(don't know		either right or	Question by	Time ticks	But potentially
what		wrong).	question.	down.	very large set of
questions		Nondetermistic	No if taking	Dynamic	possible answers.
are hidden)		responses from	into account	when other	(Could also be
		other players	accumulated	players may	continuous if you
			money from	move first.	consider bets as
			previous		continuous, or
			bets.		probabilities as
					outputs).

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4.b. (8 points) Specify a PEAS model for IBM's Watson system.

Performance: win het pains tisutores.com Environment: questions to solve, other players' actions.

Actuator: output answers, amounts to bet on screen.

Sensors: reads questions via text message, sees other players' bets. WeChat: CStutorCS

Game Types. 10 points total.

Summary. Different payoff numbers can represent the same type of game. What matters is not so much the exact numbers, but qualitative relationships, like which numbers are bigger than others, what the equilibria and dominant strategies are. To transform a game matrix into another equivalent one, you can always change a player's utility function u by a positive linear transformation: add constants or multiply by a positive number. For example, if u is the utility function of a rational agent, then the linear transformation

$$u'(x) = -5 + 3u(x)$$

defines a new utility function. If you can transform one game matrix into another using a positive linear transformation, then they represent the same game.

1. (5 points) What type of game (i.e., BoS, PD, etc. – see lecture notes) does the following game matrix represent? Write down a positive linear transformation for each player that transforms the same matrix shown into the one shown in the lecture potes.

Ī	1.44	L ₁	R
	T NUDS	!/¼-tutores.com	-3,1
	В	1,-3	-2,-2

Solution: Prisoner When hat: cstutorcs
(ii) game matrix from lecture notes

	L	R
T	0,0	-2,2
В	2,-2	-1,-1

Linear transformations that transform game matrix (i) into (ii):

- Row player: $U_r'(x) = a*U_r(x) + b$ where $U_r'(x)$ is the utility function for the row player obtained from matrix (i) and $U_r(x)$ is the utility function for the row player obtained from matrix (ii).

Solve the linear system for constants a and b:

$$0 = a*(-1) + b \rightarrow a = b$$

 $2 = a*(1) + b \rightarrow b = 1$
 $\rightarrow U_r'(x) = U_r(x)+1$

- Column player: same reasoning as above
- \rightarrow U_c'(x) = U_c(x)+1

<u>NB:</u> you were given full grade if you explained the steps leading to finding the linear transformation.

2. (5 points) What type of game (i.e., BoS, PD, etc. – see lecture notes) does the following game matrix represent? Write down a positive linear transformation for each player that transforms the game matrix shown into the one shown in the lecture notes.

	L	R
T	2,2	-1,-4
В	-1,-4	5,-1

BoS

(ii)

	L	R
T	1,2	0,0
В	0,0	2,1

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1) Row:
$$U_r'(x) = a*U_r(x)+b$$
-1 $a+b=0 \rightarrow a=b$
5 a **Ttps**/rtutorcs.com

$$\rightarrow U_r'(x) = 1/3*U_r(x)+1$$

$$-4 a + b = 0 \Rightarrow a = 1/3, b = 4/3$$

$$\rightarrow U_r'(x) = 1/3*U_r(x)+4/3$$

Nash Equilibrium Analysis. 16 points.

Summary. Finding the Nash equilibria of a game is the first step in game-theoretic analysis.

1. (8 points) BoS: Find all deterministic Nash Equilibria, and at least one mixed Nash equilibrium.

	L	R
T	2,4	0,0
В	0,0	4,2

Sample Answer (not necessarily the solution):

[T,L] is the only deterministic Nash equilibrium.

 $[p(T) = \frac{1}{2}, p(L) = \frac{1}{2}]$ is a mixed Nash equilbirum.

Reminder:

- 1. A pure or deterministic Nash Equilibria (NE) is a pure or deterministic pair of strategies (s1, s2) such that s1 is a best response (maximizes payoff) against s2 and s2 is a best response against s1. In the case of a single move game, a pure strategy is a single action.
- 2. A mixed NE is a pair of mixed strategies that are each the best response to the other. A mixed strategy is a randomized strategy that selects actions according to a probability distribution.

BoS deterministic NE: (T, L) and (B,R)*.

If row player chooses T, best solution for column player is to choose L and vice versa.

If row player chooses B, best solution for column player is R and vice yersa.

*These ard Storing in The Charles of In Opin Control and The Storing in The Charles of In Opin Control and In C

Bos Mixed NE: https://tutorcs.com

- Mixed strategy for row player = p
- Mixed strategy for col player = q

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		L q	$R \qquad (1-q)$
T	p	2,4	0,0
В	(1-p)	0,0	4,2

- If row chooses T with probability p, the optimal strategies for Col are:

 - Expected Payoff(R, p) = $p \times 0 + (1-p) \times 2 = 2-2p$
- According to the support theorem (if Col player randomizes, both L and R are equally good strategies):
 - o Payoff(L,p) = Payoff(R,p) \Leftrightarrow 2p = 1-p \Leftrightarrow p = 1/3
 - o In any mixed equilibrium, row player chooses T or B with P(T) = 1/3 and P(B) = 2/3
- If col chooses L with probability q, the optimal strategies for row are:
 - o Payoff $(T,q) = q \times 2 + (1-q) \times 0 = 2q$
 - \circ Payoff(B,q) = q x 0 + (1-q) x 4 = 4-4q
- Support theorem:
 - \circ Payoff(T,q) = Payoff(B,q) \Leftrightarrow q = 2-2q \Leftrightarrow q = 2/3
- → Mixed NE is P(L) = P(B) = 2/3 and P(T) = P(R)=1/3

2. (4 points) The Game of Chicken (featured in movies "Rebel Without a Cause", and "Charlie's Angels".). Two drivers are heading towards each other. Whoever turns away first, loses. A historical example is the Cuba crisis between the USSR and the USA.

	Turn	Keep Going
Keep Going	3, 1	-15, -15
Turn	0, 0	1, 3

- a. (2) Find all deterministic Nash Equilibria.
- b. (2) Find at least one mixed Nash equilibrium in the Game of Chicken.

Deterministic Nash Equilibria.

(Keep Going, Turn), (Turn, Keep Going)

Mixed Nash Equilibrium:

P(row Assignment Project Exam Help

NB: full grade if you explained the steps to find a deterministic and mixed NE.

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3. (4 points) An issue that arises in technology industries is that an inferior standard may become entrenched even if a better one is available. A historical example is the use of VHS tapes vs. Betay Or Facebook vs. GooglePlus? This illustrates network effects: users like to use technology and by thers. Cets contider a simple game-theoretic model of this situation.

	User 2	
<u>User 1</u>	Superior technology	Inferior technology
Superior technology	3, 3	1, 1
Inferior technology	1, 1	2, 2

- a. (2) Find all deterministic Nash Equilibria.
- b. (2) Find at least one mixed Nash equilibrium in this game.

Deterministic Nash Equilibria: These are cases where neither side randomizes, (Superior, Superior), (Inferior, Inferior)

Mixed Nash Equilibrium:

When col randomizes, p = 1/3

When row randomizes, q = 1/3

NB: full grade if you explained the steps to find a deterministic and mixed NE.

Assignment 2: Chapters 4, 3, 5. (SOLUTIONS)

NB: clarity of your answers is considered in the final grade.

Chapter 4. Local Search in Continuous Spaces. 26 points.

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a. (3) Write down the gradient (derivative) of the function you chose. (Hint: this 1.

is probably easier for *l*.)

$$\frac{\partial l}{\partial p} = \frac{\text{https:}}{p} / \text{tutorcs.com}$$

b. (10) Try to get close to the minimum in 5 gradient descent steps. Use as your initial gwes of 1/2 thatoin is faith and for the first 3 step sizes, use 0.04, 0.02, 0.01. The last 2 step sizes you can choose for yourself. For your answer fill in the table below.

step	р	step
		size
0	0.5	0.04
1	0.66	0.02
2	0.607	0.01
3	0.604	0.005
4	0.603	0.0025
5	0.603	

Step size of 4 and 5 can be other reasonable values (e.g. both 0.1).

2.

a. (3) Write down the second-order gradient (derivative) of the function you chose. (Hint: this is probably easier for *l*.)

$$\frac{\partial^2 l}{\partial p^2} = (\frac{6}{p^2} + \frac{4}{(1-p)^2})$$

b. (10) Show the results of 5 Newton-Raphson steps. Use as your initial guess p=1/2 (the coin is fair).

step	р
0	0.5
1	0.6
2	0.6
3	0.6
4	0.6
5	0.6

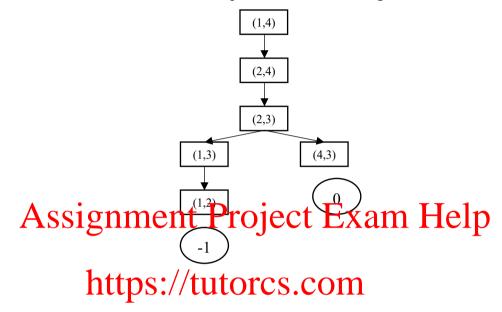
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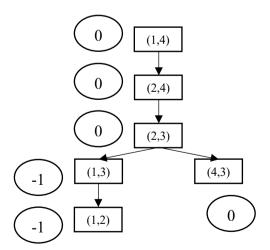
Chapter 5. Adversarial Search. 26 points totals.

- 1. (10) Draw the complete game tree, using the following conventions.
 - a. Write each state as (s_A, s_B) , where s_A and s_b denote the token locations.
 - b. Put each terminal state in a square box and write its game value in a circle.



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2. (10) Now mark each node with its backed-up minimax value (also in a circle).



- 3. (6) Suppose that we allowed repeated states and otherwise kept the rules the same.
 - a. Describe the optimal strategy for each player (informally but precisely).

For Player A, she should keep herself moving in right direction.

For Player B, she should keep herself moving in left direction.

b. Does the standard minimax algorithm terminate with a strategy for each player? If yes, does it find the optimal strategy (from part a)? If not, how could you modify the standard minimax algorithm so that it terminates after finding the optimal strategy for each player in this game? The modification should be general in the sense that the modified algorithm can be applied to any game tree, not just this game.

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Standard minimax is depth-first and would go into an infinite loop. It can be fixed by comparing the current state against the stack; and if the state is repeated, then return a "? Null Dropagation of Case Gs bahnled as above. Although it works in this case, it does not always work because it is not clear how to compare "?" with a drawn position; nor is it clear how to handle the comparison when there are wins of afternadgree (astilling transn). Finally, in games with chance nodes, it is unclear how to compute the average of a number and a "?". Note that it is not correct to treat repeated states automatically as drawn positions; in this example, both (1,4) and (2,4) repeat in the tree but they are won positions.

What is really happening is that each state has a well-defined but initially unknown value. These unknown values are related by the minimax equation at the bottom of 164. If the game tree is acyclic, then the minimax algorithm solves these equations by propagating from the leaves. If the game tree has cycles, then a dynamic programming method must be used, as explained in Chapter 17. These algorithms can determine whether each node has a well-determined value (as in this example) or is really an infinite loop in that both players prefer to stay in the loop (or have no choice). In such a case, the rules of the game will need to define the value (otherwise the game will never end). In chess, for example, a state that occurs 3 times (and hence is assumed to be desirable for both players) is a draw.

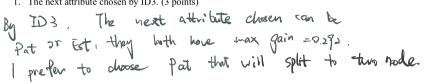
Other modifications, like using a iterative depth first search, are also acceptable.

Decision Tree Learning. 9 points total.

Summary. The purpose of this assignment is to give you practice with computing expected information gain and how the ID3 algorithm uses it to construct a decision tree.

Figure 1 provides data about whether a customer will wait for a table in a restaurant or not. Assume that ID3 splits first on the Hun(gry) attribute. Show the following for the branch Hun(gry)=T.

1. The next attribute chosen by ID3. (3 points)



2. The expected information gain associated with the next attribute. There may be more than one attribute with the same information gain, finding one is sufficient.

(3 points) ===== · log2(==) - = log2(==) = 0.86>1 $E(some) = -\frac{3}{5} \log_3(\frac{5}{5}) - 0 = 0.$

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Gain (Pat) = 9.8631 - 3-0-4-1

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3. How you calculated the expected information gain. (3 points)

I cal culated the Entropy of every attributes first Entropy = $\frac{7}{4}$ - Pilogipi. Then I generated P(x) for each attribute. Information Gain = El Hungry) - [average entropy (dildren). I used mattab to help calculate each expected Entropy= 0.863121 infornation gain. Gain(Alt) = 0.169584 Gain(Bar) = 0.005978 Gain(Fri) = 0.005978 Gain(Pat) = 0.291692 Gain(Price) = 0.183851

Gain(Rain) = 0.169584 Gain(Res) = 0.005978 Gain(Type) = 0.183851 Gain(Est) = 0.291692

Trace Backpropagation. 13 points total.

	a	b	d
X 1	1	0	1
X 2	0	1	0

Table 1. The Sigmoid Function

Definition	Derivative
$\sigma(x) = 1/(1 + \exp(-x))$	$d\sigma/dx = \sigma(x)(1-\sigma(x))$

- 1. Using the notation in the text, show the formulas for computing the following quantities, for any node *i*: (4 points)
 - ini
 - a_i
 - Δ[i]
 - · Weight update for Wijnt Project Exam Help

• $in_i = \sum_{i=1}^{n} W_{i}i a_{j}$.

•
$$a_i = \frac{https://tutorcs.com}{= ((ini))}$$

•
$$\Delta[i] = WeChat: cstutorcs$$

- Weight update for w_{ij} $W_{ij} = W_{ij} + \alpha \times \alpha_{i} + \Delta_{j}$.
- 2. Fill in the following table using the formulas from above. You can expand this to include more information (e.g. derivatives of activation functions) if you like. (9 points)

	Iteration	ac	Δ[c]	ad	Δ[d]	W0c	Wac	Wbc	Wcd	W0d	
	X 1	05787	0.0049	595793	25 01.0	2103.0	2105.8	0.\\\ \)	0.484	0.2508	
	X 2	662.0	2506.0-	0.3994	-0.1426	0.1992	D. 2015	9. 1978	0.1928	0.1880	
$\times_{\mathfrak{l}_i}$	inc = Wac . a	o twas . as	+W= at	1	L L	a) · (1-1	(xp (-ind))	. (d - ad			40.3Qb.6E
	ind = wod .a	0 + Wcd·a	.c -	△(c)	, ,		<u> </u>			cd = Wed	+0.30e.2[d]
	ac = + exp(-inc)	Od = 1+0	exp(-ind)	Woc	= Woc + 0.					d = Wod	10.3 ad .s[d]
				Wac	= Wac + 0	.3 - aa - a	Sicl				

Assignment 4: Probabilistic Reasoning and Learning

Instructions: The university policy on academic dishonesty and plagiarism (cheating) will be taken very seriously in this course. Everything submitted should be your own writing or coding. You must not let other students copy your work. On your assignment, put down your **name**, the number of the assignment and the number of the course. Spelling and grammar count. You should show your work to get the result in order to get the full mark.

Group Work: Discussions of the assignment is okay, for example to understand the doncepts involved. If you work in a group, paradwritte name of all members of your group. There should be no group submissions. Each group member should write up their own solution to show their own understanding.

For the <u>due date</u> please septil pusse management er er <u>the Murses.cs.sfu.ca</u>. The time when you upload your assignment is the official time stamp. If your assignment is late because you did not figure this out soon enough, you will lose marks according to the syllabus policy.

Terminology: The questions are not self-explanatory. Even ordinary English words (e.g., "rationality") may not have their ordinary meaning in an AI context. Part of your task is to learn the AI terminology required to understand the questions. You will likely not understand the questions if you have not studied the course material.

Getting Help. Check the syllabus for communication policy. You have the textbook, the lecture notes, the discussion forum, and you can ask us in office hours or class sessions. We do not provide individual email support.

Handing in the Assignment. Please use the submission system on courses.cs.sfu.ca.

You should post

- a pdf document that contains your written answers, as well as the screenshots and diagrams required.
- A Bayesian network in executable file format (.xml or .bif), for the power station problem.

Probabilistic Reasoning With Bayesian Networks 75 points total.

Go to www.aispace.org and start the "belief and decision network" tool. Load the sample file "File/Load Sample Problem/Simple Diagnostic Example". We will use this to test some of the basic probability laws. The Alspace tool can do many of these calculations for you, but the purpose of the exercise is to learn the principles behind the calculations. You can use the tool to check your answers, but you should compute them yourself using the probability calculus together with the conditional probabilities from the Bayesian network. If you have difficult running the tool in the browser, try downloading the jar file.

```
Joint probabilities
```

```
1. P(all nodes false)
= P(Influenza = F) * P(Smokes = F) * P(Sore Throat = F | Influenza =
F) * P(Fever = F | Influenza = F) * P(Bronchitis = F | Influenza = F and Smoke = F) *
P(Coughing = F \mid Bronchitis = F) * P(Wheezing = F \mid Bronchitis = F)
= 0.95 * 0.8 * 0.999 * 0.95 * 0.9999 * 0.93 * 0.999
= 0.670051 Assignment Project Exam Help
2. P(Sore Throat = T, all other nodes false)
= P(Influenza = F) * P(Sninglet p F) * P(Strate p F) * P(Fever = F | Influenza = F) * P(Bronchitis = F
F and Smoke = F) * P(Coughing = F | Bronchitis = F) * P(Wheezing = F | Bronchitis = F) =
0.95 * 0.8 * 0.001 * 0.95 * 0.999 * 0.93 * 0.999
- 0.000671 WeChat: Cstutorcs
3. P(all nodes others than Sore throat false) = P(Sore\ Throat = T, all\ other\ nodes\ false) or P(Sore\ Throat = T, all\ other\ nodes\ false)
       Throat = F, all other nodes false) = P(Sore Throat = T, all other nodes false) + P(all nodes false)
= 0.670051 + 0.000671
= 0.670722
4. P(Sore Throat = F \mid all other node are false) * P(all other nodes are false)
= 0.999 * 0.670722
= 0.670051
= P(all nodes false)
5. P(Sore Throat = T, Fever = T)
= P(Sore Throat = T | Influenza = T) * P(Fever = T | Influenza = T) P(Influenza = T) + P(Sore Throat =
T \mid Influenza = F) * P(Fever = T \mid influenza = F) * P(Influenza = F)
= 0.3 * 0.9 * 0.05 + 0.001 * 0.05 * 0.95
= 1.35475 * 10^{(-2)}
```

Independence

20 points

Influenze

"If no evidence is observed, Influenza and Smoking are probabilistically independent."

1. (10) Prove this statement from the numerical semantics, i.e. show that the values of Influenza and Smokes are independent for all possibilities. You may use queries in the tool to do this.

joint

i. Must check all possible values of joint.

Smoking

TRUE TRUE 0.01 0.01 TRUE FALSE 0.04 0.04

product

FALSE SSIGNMENT Project Exam Help

Checking the equivalent of P(A)=P(A|B) is also acceptable.

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$$P(A \cap B) = P(A)P(B) \Leftrightarrow P(A) = \frac{P(A)P(B)}{P(B)} = \frac{P(A \cap B)}{P(B)} = P(A \mid B)$$

WeChat: cstutorcs 0) Prove this from the topological semantics, i.e. using the

2. (10) Prove this from the topological semantics, i.e. using the Markov condition that given values for its parents, a variable is probabilistically independent of all its nondescendants.

Neither has a parent, so the condition holds vacuously. Neither is a descendant of the other, so they are independent.

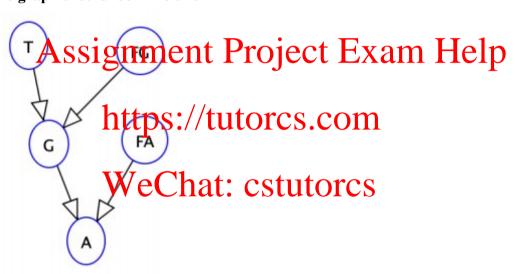
Bayesian Networks and Constraints (30 points total)

In a power station, an alarm senses when a temperature gauge exceeds a given threshold. The gauge measures the temperature of the core. Using the AIspace tool, draw a Bayesian network that represents the following information about the plant. You may consider editing your Bayes net in a text editor to facilitate copying of similar entries.

1. (5 points) Create a Bayes net with the following variables (=nodes) and domains. Each domain represents a range of possible locations.

Variable	Domain	Meaning
A	{T,F}	alarm sounds
FA	{T,F}	alarm is faulty
FG	{T,F}	gauge is faulty
G	{Normal, High}	gauge reading
T	{Normal, High}	core temperature

The graph should look like this



- 2. Draw edges between the nodes and specify conditional probability tables to represent the following information.
 - a. (6) The alarm works correctly unless it is faulty. If it is faulty, it never sounds.

FA	G	P(A=T)	P(A=F)		
Т	Normal	0.0	1.0		
Т	High	0.0	1.0		
F	Normal	0	1.0		
F	High	1	0.0		

b. (6) If the gauge is not faulty, there is a 90% chance that it gives the correct temperature. If the gauge is faulty, there is a 10% chance that it gives the correct temperature.

FG	Т	P(G=Normal)	P(G=High)
Т	Normal	0.1	0.9
Т	High	0.9	0.1
F	Normal	0.9	0.1
F	High	0.1	0.9

c. (10) Suppose the alarm and gauge are working correctly and the alarm sounds. Using the probability calculus probability, and the various conditional probabilities in the network, calculate the probability that under these circumstances, the temperature of the core is high. You can make the following assumptions. (i) The temperature is normal 70% of the time, high authority 10% of the time.

Since the gauge is not faulty, and the alarm is true, we know that the gauge must be high the light tutores.com

Moreover, given gauge=high, from the Bayes net, we can conlude that alarm and faulty plant is conditional independent to the temperature and faulty gauge. CSTUTOTCS

d. (3) Use the AIspace query tool to confirm your answer from c. According to our solution for c), you can use any estimate you like for the

prior P(FA=T), e.g. 50% or 80%. We suggest experimenting with the tool to verify that you get the same result as c) no matter what prior value you use. e.

```
Query Results for Variable T [A=T] [FA=F] [FG=F]
P (T = Normal) = 0.20588
P (T = High) = 0.79412
```

Difference to textbook 14.11: no edge from T to FG. Extra parameters are specified in the problem.

What to Submit for this question. Everything specified in the problem, including answers and brief explanations. In addition: A loadable .xml or .bif file for your Bayesian network in part 1. A screenshot of your Bayesian network, screenshots of your CP-tables, and a screenshot of your query and the answer from Alspace.

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