

# CMT107 Visual Computing Assignment Project Exam Help

https://tutorcs.com Image Filtering

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Jing Wu

School of Computer Science and Informatics Cardiff University

#### Overview

- Linear filtering
- Convolution
- Box filtering
- Gaussian filtering
- Separable kernel
- Median filter
- Sharpening

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Acknowledgement

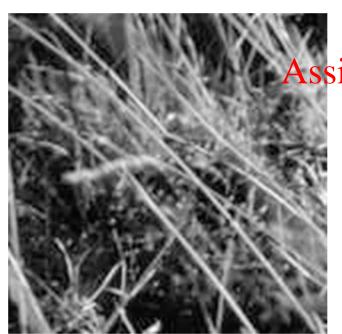
The majority of the slides in this section are from Svetlana Lazebnik at University of Illinois at Urbana-Champaign

## Image Filtering

- Filtering is a technique for modifying or enhancing an image
  - Emphasise certain features or remove other feature
- Filtering is a neighbourhood operation
  - The output value of any given pixel is determined by the values of the pixels in the neighbourhood of the corresponding input times. Help
- Linear filtering is filtering in which the values of the pixel is a linear combination (weighted average) of the values of the pixels in the input pixel's neighbourhood

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  - Linear filtering can be represented by convolution

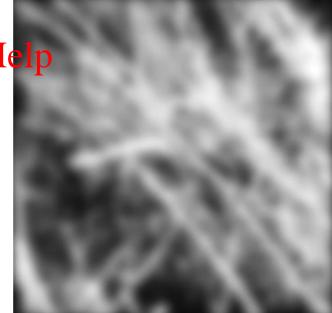
# Linear Filtering



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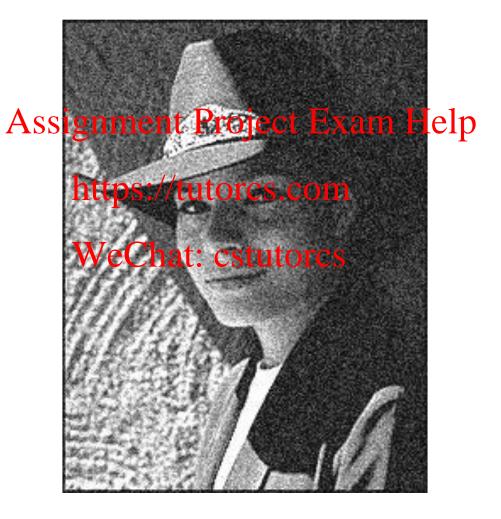
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### Motivation: Image Denoising

How can we reduce noise in a photograph?



- Let's replace each pixel with a weighted average of its neighbourhood
- The weights are called the filter kernel

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- Let's replace each pixel with a weighted average of its neighbourhood
- The weights are called the filter kernel
- What are the weights for the average of a 3x3 neighbourhood?

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Source: D. Lowe

- Let's replace each pixel with a weighted average of its neighbourhood
- The weights are called the filter kernel
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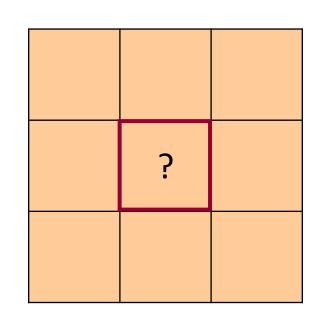
"box filter"

- Let's replace each pixel with a weighted average of its neighbourhood
- The weights are called the filter kernel
- What are the weights for the average of a 3x3 neighbourhood?

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1	1	1
1	10	1
1	1	1

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* \frac{1W}{9}	eChat:	cstute 1	orcs 1
	1	1	1



"box filter"

- Let's replace each pixel with a weighted average of its neighbourhood
- The weights are called the filter kernel

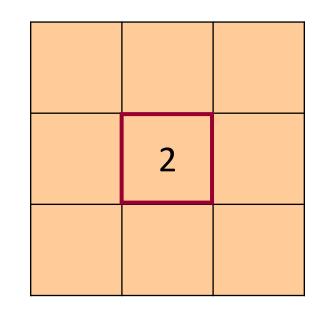
\*

What are the weights for the average of a 3x3 neighbourhood?

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1	1	1
1	10	1
1	1	1

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$\frac{1W}{9}$	eChat:	cstute 1	orcs 1
	1	1	1



"box filter"

• Let f be the image and g be the kernel. The output of convolving f with g is denoted  $f \ast g$ 

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Source: F. Durand

• Let f be the image and g be the kernel. The output of convolving f with g is denoted  $f \ast g$ 

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g

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f

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• Let f be the image and g be the kernel. The output of convolving f with g is denoted  $f \ast g$ 

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g

Convention: kernel is flipped for convolution



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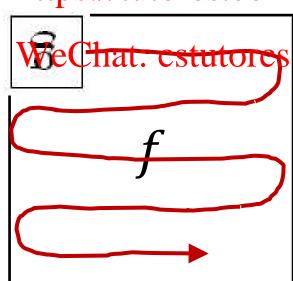
Source: F. Durand

• Let f be the image and g be the kernel. The output of convolving f with g is denoted  $f \ast g$ 

#### Assignment Project Exam Help

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Convention: kernel is flipped for convolution



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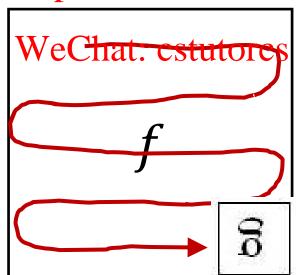
Source: F. Durand

• Let f be the image and g be the kernel. The output of convolving f with g is denoted  $f \ast g$ 

$$(f * g)[x,y] = \sum_{i=-k}^{k} \sum_{j=-l}^{l} f[x-i,y-j]g[i,j]$$
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Convention: kernel is flipped for convolution



# Linear Filter: Key Properties

- Linearity: filter( $f_1 + f_2$ ) = filter( $f_1$ ) + filter( $f_2$ )
- Shift invariance: same behaviour regardless of pixel location filter(shift(f)) = shift(filter(f))
- Theoretical result: any Aineign shift i Projeion Experator per le represented as a convolution

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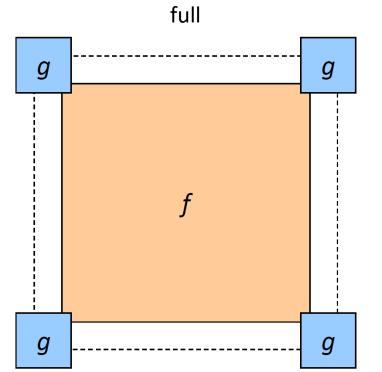
### Linear Filter: More Properties

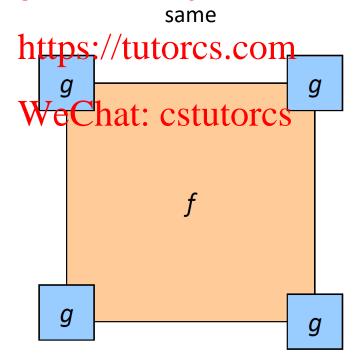
- Commutative: a \* b = b \* a
  - Conceptually no difference between filter and signal
- Associative: a \* (b \* c) = (a \* b) \* c
  - Often apply several filters one after another:  $((a*b_1)*b_2)*b_3)$  This is equivalent to applying one filter:  $a*(b_1*b_2*b_3)$
- Distributive over addition: bttp(b/tuto)cs.(am b) + (a \* c)
- Scalars factor out:  $ka * b = q_{\bullet}(kb) = k(a * b)$
- Identity: unit pulse e = [..., 0, 0, 1, 0, 0, ...], a \* e = a

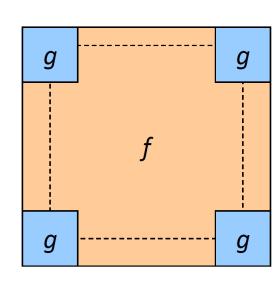
# Size of the Output

- "full": output size is the sum of sizes of f and g minus 1
- "same": output size is the same as the size of f
- "valid": output size is the difference of the sizes of f and g

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valid

- What about near the edge?
  - The filter window falls off the edge of the image
  - Need to extrapolate
  - Method
    - Clip filter (black)
    - Wrap around
    - Copy edge
    - Reflect across edge

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• Clip filter (black)



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Source: S. Marschner

#### Wrap around

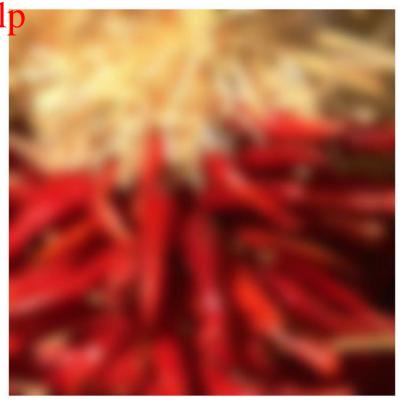


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Source: S. Marschner

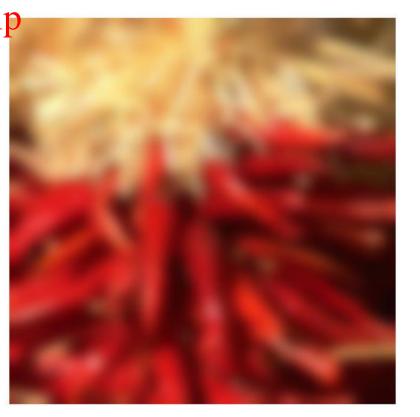
• Copy edge





Reflect across edge

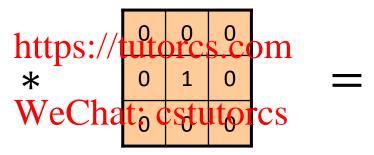




Source: S. Marschner



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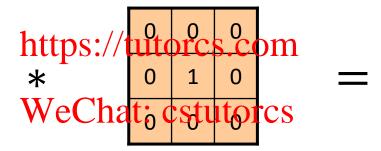




Original

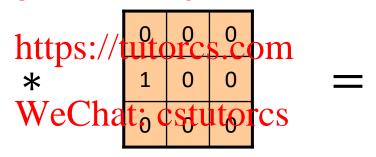


Original



Filtered (no change)



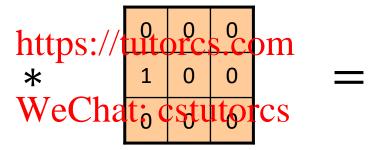




Original



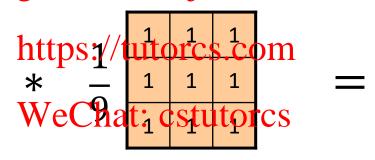
Original





Shifted left by 1 pixel



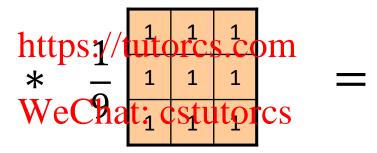




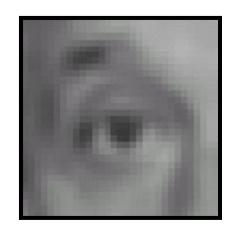
Original



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Original



Blur (with a box filter)



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Original

(Note that filter weights sum to 1)



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Original

(Note that filter weights sum to 1)

Sharpening filter:
Accentuates differences
with local average

# Smoothing with Box Filter revisited

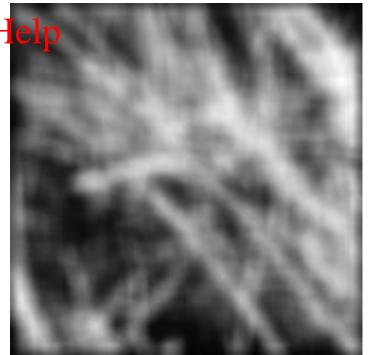
- What's wrong with this picture?
- What's the solution?



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# Smoothing with Box Filter revisited

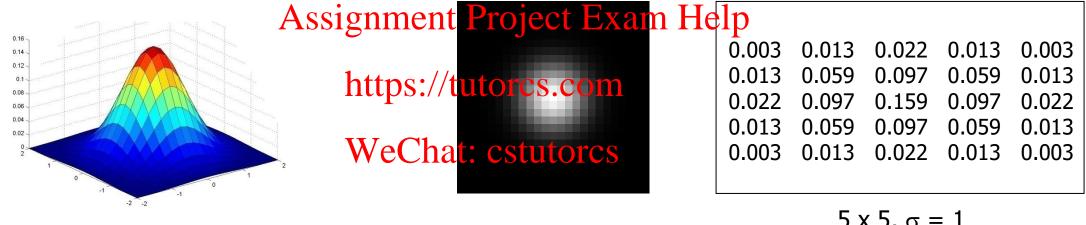
- What's wrong with this picture?
- What's the solution?
  - To eliminate edge effect, weight contribution of neighbourhood pixels according to their closeness to the centre.



"fuzzy blob"

### Gaussian Kernel

$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$



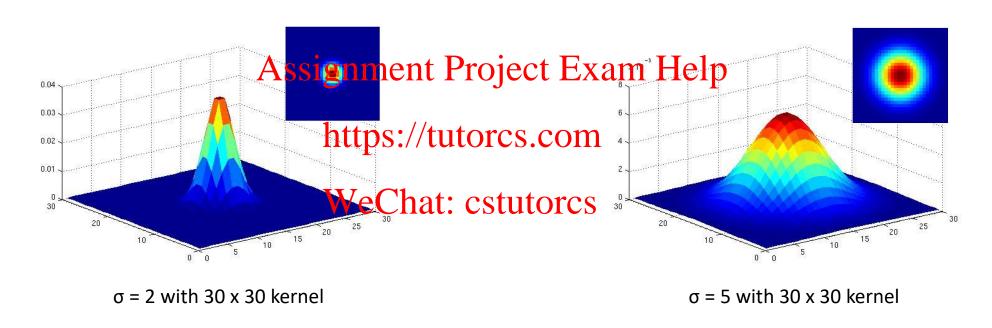
 $5 \times 5$ ,  $\sigma = 1$ 

 Constant factor at front makes volume sum to 1 (can be ignored when computing the filter values, as we should renormalize weights to sum to 1 in any case

Source: C. Rasmussen

### Gaussian Kernel

$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2 + y^2)}{2\sigma^2}}$$

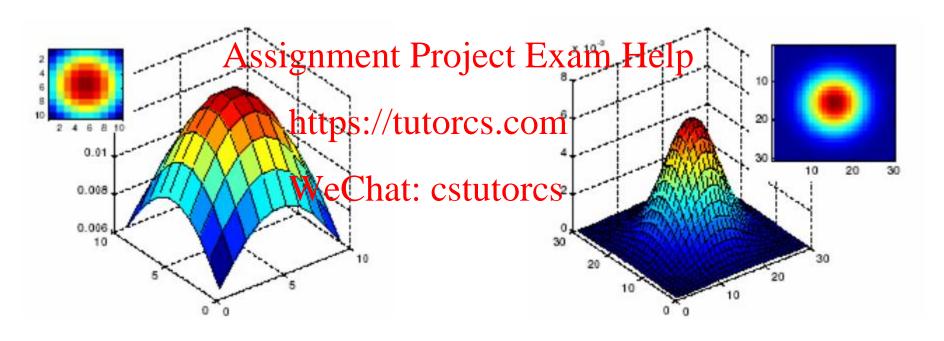


• Standard deviation  $\sigma$  determines the extent of smoothing

Source: K. Grauman

# Choosing Kernel Width

• The Gaussian function has infinite support, but discrete filters use finite kernels



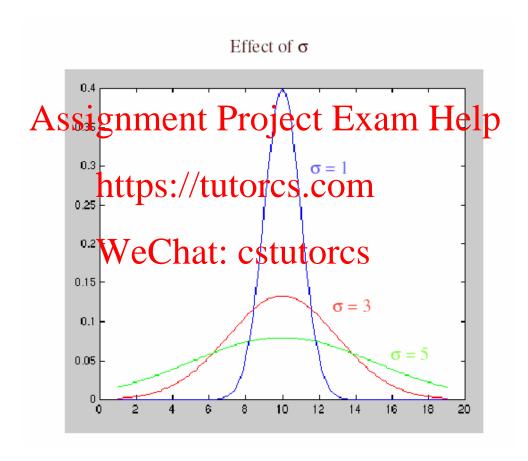
 $\sigma$  = 5 with 10 x 10 kernel

 $\sigma$  = 5 with 30 x 30 kernel

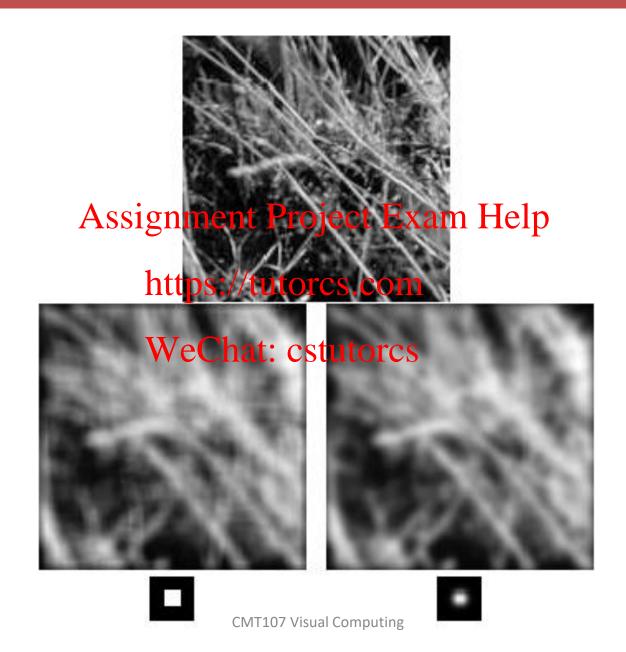
Source: K. Grauman

## Choosing Kernel Width

• Rule of thumb: set filter half width to about  $3\sigma$ 



## Gaussian vs. Box Filtering



#### Gaussian Filters

- Remove "high frequency" component from the image (low-pass filter)
- Convolution with self is another Gaussian
  - So can smooth with small- $\sigma$  kernel, repeat, and get same result as large- $\sigma$  kernel would have
  - Convolving two times with same as convolving one with Gaussian kernel with standard deviation  $\sigma\sqrt{2}$
- Separable kernel
  - Factors into product of two Weshianstutores

## Separability of the Gaussian Filter

$$G_{\sigma}(x,y) = \frac{1}{2\pi\sigma^{2}}e^{-\frac{(x^{2}+y^{2})}{2\sigma^{2}}} = \left(\frac{1}{\sqrt{2\pi}\sigma}e^{-\frac{x^{2}}{2\sigma^{2}}}\right)\left(\frac{1}{\sqrt{2\pi}\sigma}e^{-\frac{y^{2}}{2\sigma^{2}}}\right)$$

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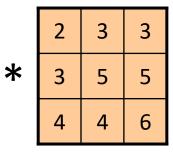
- The 2D Gaussian can be expressed as the product of two 1D functions: one is a function of x, and the other is a function of y.
- In this case, the two functions are the the the file of the file

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Source: D. Lowe

2D convolution (centre location only)

1	2	1
2	4	2
1	2	1



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2D convolution (centre location only)

1	2	1
2	4	2
1	2	1

$$= 1 \times 2 + 2 \times 3 + 1 \times 3 = 11$$

$$= 2 \times 3 + 4 \times 5 + 2 \times 5 = 36$$

$$= 1 \times 4 + 2 \times 4 + 1 \times 6 = 18$$

$$= 65$$

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2D convolution (centre location only)

1	2	1
2	4	2
1	2	1

$$= 1 \times 2 + 2 \times 3 + 1 \times 3 = 11$$

$$= 2 \times 3 + 4 \times 5 + 2 \times 5 = 36$$

$$= 1 \times 4 + 2 \times 4 + 1 \times 6 = 18$$
65

The filter factors into a Assignment Proje product of 1D filters

2D convolution (centre location only)

1	2	1
2	4	2
1	2	1

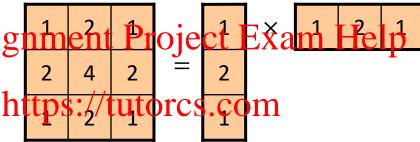
$$= 1 \times 2 + 2 \times 3 + 1 \times 3 = 11$$

$$= 2 \times 3 + 4 \times 5 + 2 \times 5 = 36$$

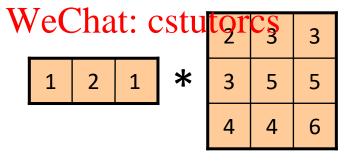
$$= 1 \times 4 + 2 \times 4 + 1 \times 6 = 18$$

$$= 65$$

The filter factors into a Assignment Proje product of 1D filters



Perform convolution along rows



2D convolution (centre location only)

1	2	1
2	4	2
1	2	1

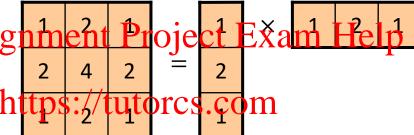
$$= 1 \times 2 + 2 \times 3 + 1 \times 3 = 11$$

$$= 2 \times 3 + 4 \times 5 + 2 \times 5 = 36$$

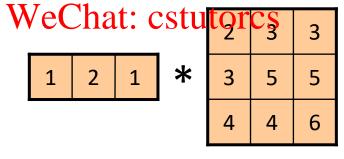
$$= 1 \times 4 + 2 \times 4 + 1 \times 6 = 18$$

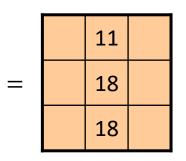
$$= 65$$

The filter factors into a Assignment Proje product of 1D filters



Perform convolution along rows





2D convolution (centre location only)

1	2	1
2	4	2
1	2	1

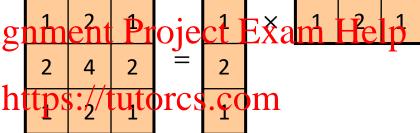
$$= 1 \times 2 + 2 \times 3 + 1 \times 3 = 11$$

$$= 2 \times 3 + 4 \times 5 + 2 \times 5 = 36$$

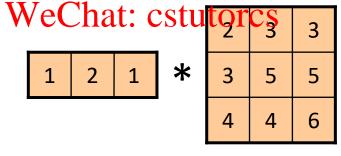
$$= 1 \times 4 + 2 \times 4 + 1 \times 6 = 18$$

$$= 65$$

The filter factors into a Assignment Proje product of 1D filters



Perform convolution along rows



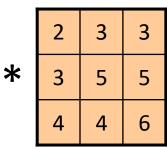
	11	
=	18	
	18	

Followed by convolution along the remaining column

1			11	
2	*		18	
1	CMT107 Visual Co	mputi	ng 18	

2D convolution (centre location only)

1	2	1
2	4	2
1	2	1



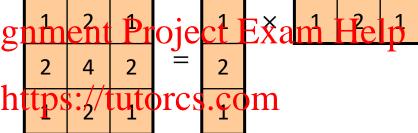
$$= 1 \times 2 + 2 \times 3 + 1 \times 3 = 11$$

$$= 2 \times 3 + 4 \times 5 + 2 \times 5 = 36$$

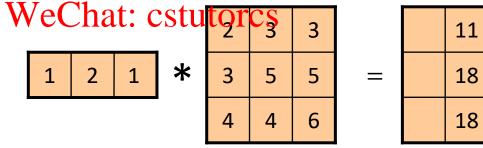
$$= 1 \times 4 + 2 \times 4 + 1 \times 6 = 18$$

$$= 65$$

The filter factors into a Assignment Proje product of 1D filters

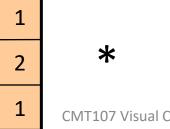


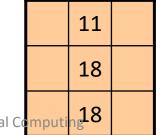
Perform convolution along rows



	11	
=	18	
	18	

Followed by convolution along the remaining column





$$= 1 \times 11 + 2 \times 18 + 1 \times 18 = 65$$

## Why is Separability Useful

- What is the complexity of filtering an  $n \times n$  image with an  $m \times m$  kernel?
  - $O(n^2 \times m^2)$
- What if the kernel separable?
  - $O(n^2 \times m)$

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#### Noise

• Salt and pepper noise: contains random occurrences of black and white pixels

• Impulse noise: contains random occurrences of white pixels

• Gaussian noise: variations in intensity drawn from a gaussian normal

distribution

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Original



Salt and pepper noise



OISE Impulse noise CMT107 Visual Computing



Gaussian noise

Source: S. Seitz

#### Gaussian Noise

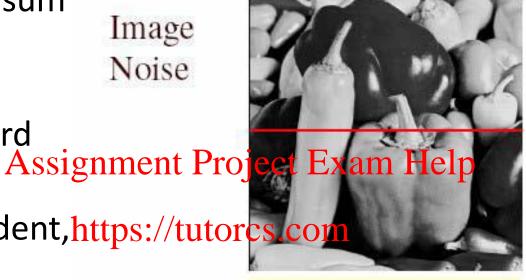
 Mathematical model: sum of many independent factors

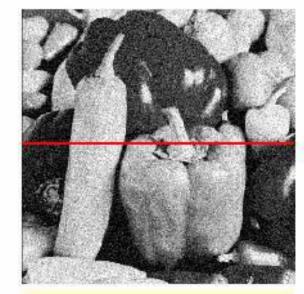
**Image** Noise

 Good for small standard deviations

Assumption: independent, <a href="https://tutorcs.com">https://tutorcs.com</a>

zero-mean noise



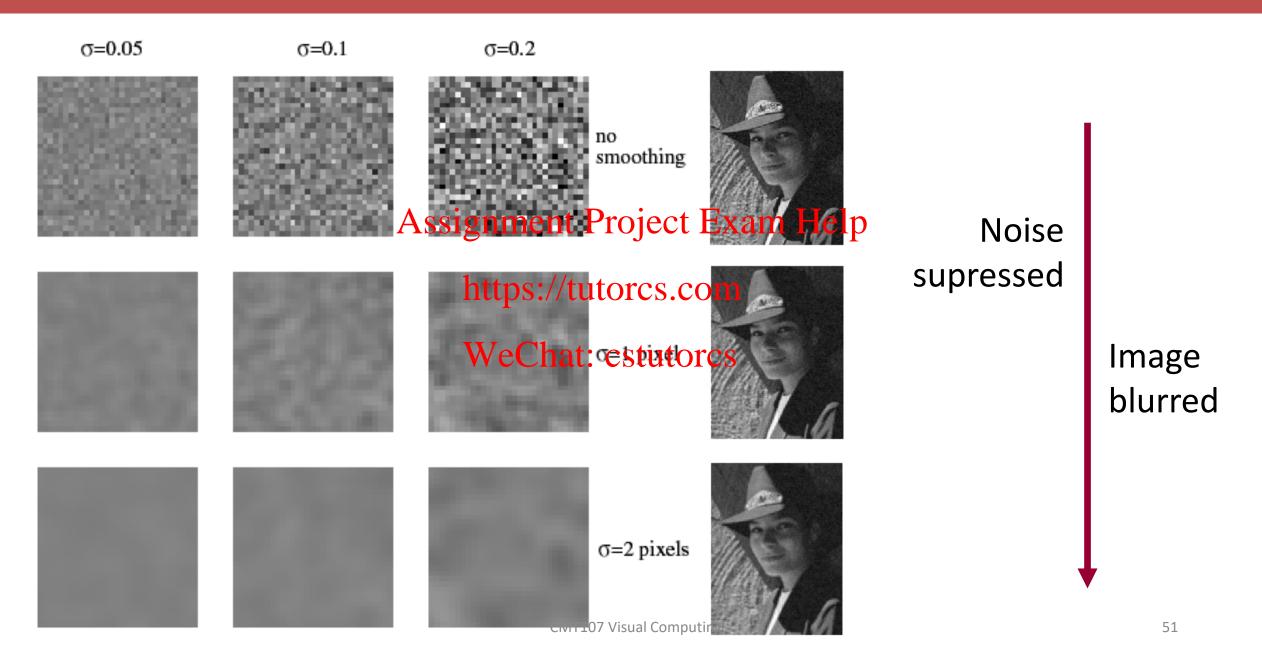




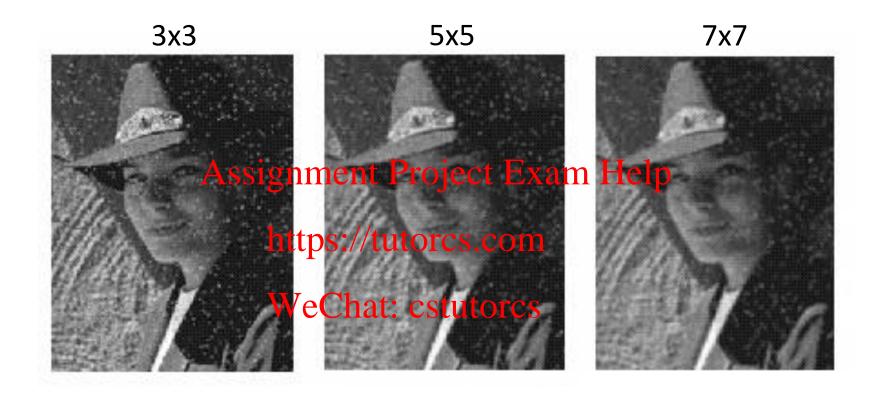
$$f(x,y) = \overbrace{\widehat{f}(x,y)}^{\text{Ideal Image}} + \overbrace{\eta(x,y)}^{\text{Noise process}}$$

Gaussian i.i.d. ("white") noise:  $\eta(x,y) \sim \mathcal{N}(\mu,\sigma)$ 

## Reducing Gaussian Noise



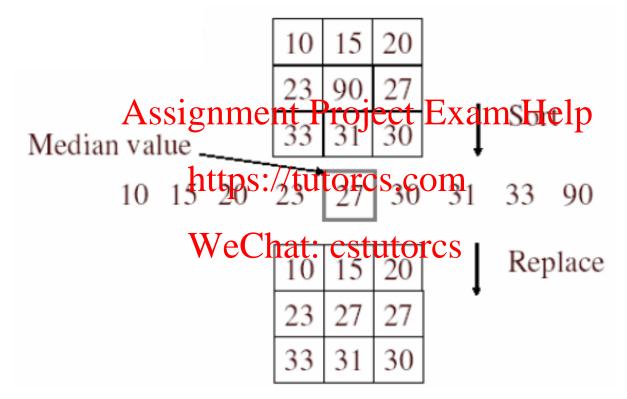
## Reducing Salt and Pepper Noise



What's wrong with the results?

## Alternative Idea: Median Filtering

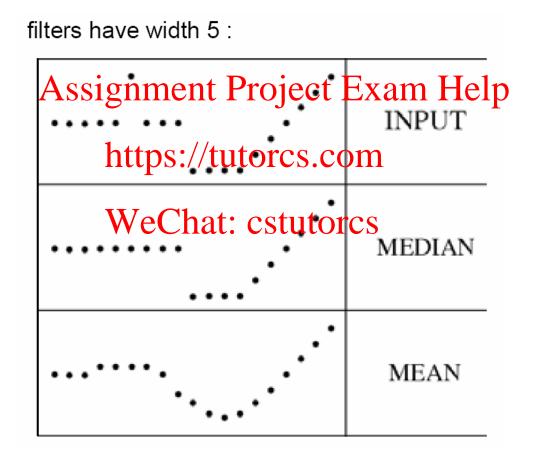
 A median filter operates over a window by selecting the median intensity in the window



• Is median filtering linear?

#### Median Filter

- What advantage does median filtering have over Gaussian filtering?
  - Robustness to outliers



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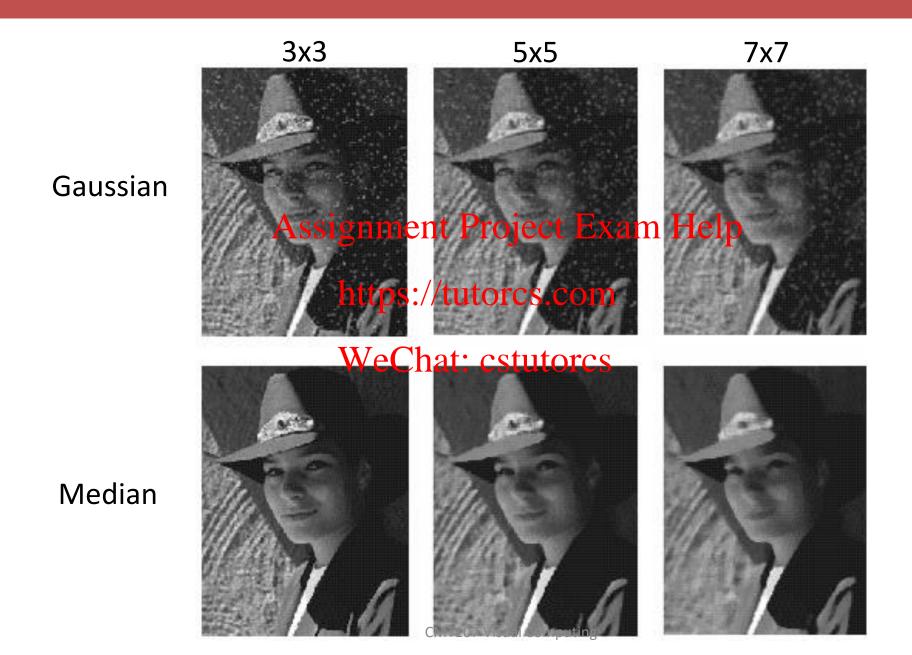
## Median Filter

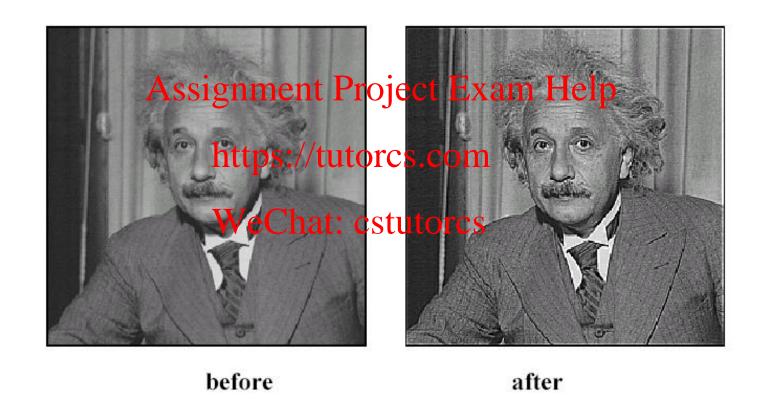
Median filtered Salt-and-pepper noise

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Source: M. Hebert

#### Gaussian vs. Median Filter





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What does blurring take away?



What does blurring take away?



What does blurring take away?



• Let's add it back



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What does blurring take away?



• Let's add it back

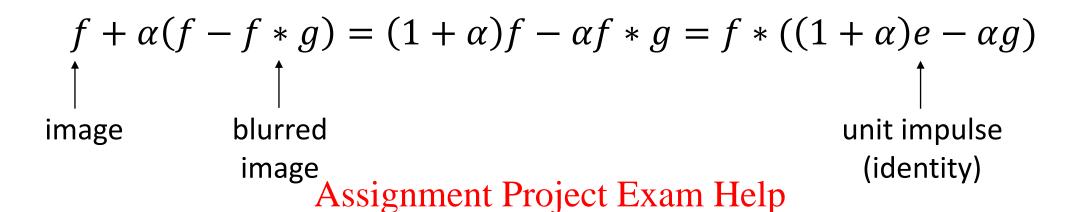


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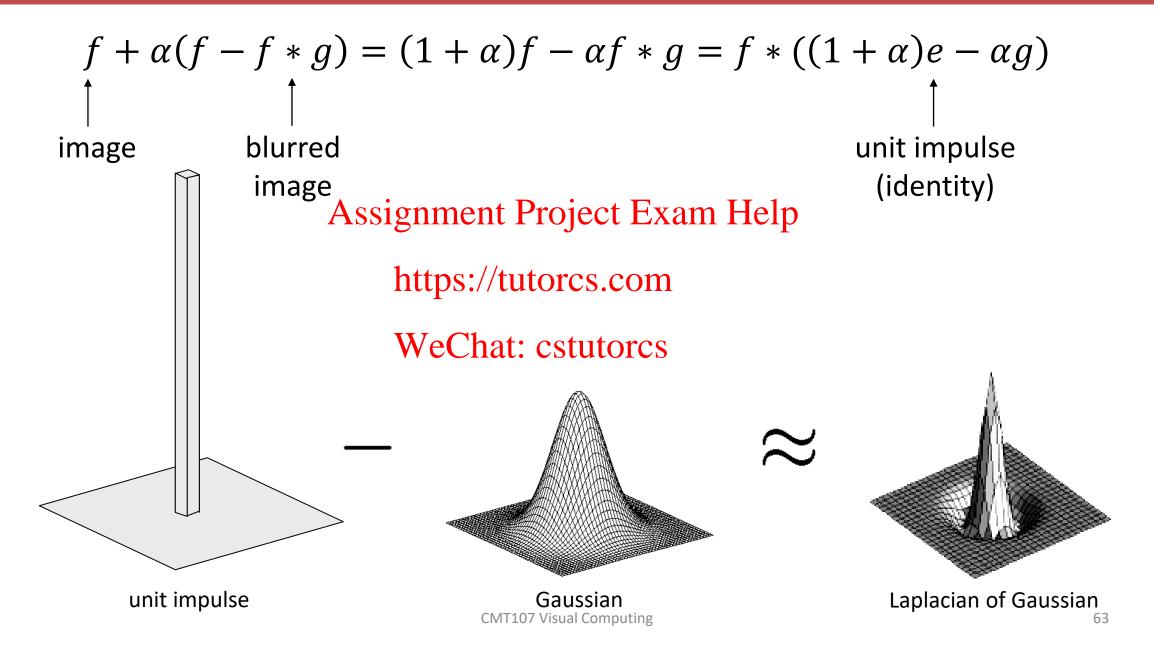


## Unsharp Mask Filter



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## Unsharp Mask Filter



## Image Filtering with Java

- Use filter() in BufferedImageOp
- Implement filtering without using filter() function

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#### Use filter() Function

Define a filter kernel

```
float[] km = { // low-pass filter kernel
       0.1f, 0.1f, 0.1f, // Suppose the matrix has been flipped
       0.1f, 0.2f, 0.1f,
                           Assignment Project Exam Help
       0.1f, 0.1f, 0.1f
   };
   Kernel kernel = new Kernel(3, 3, km); | ConvolveOp(Kernel kernel, int edgeCondition,
                                                                           RenderingHints hints)
                                WeChat: cstutorcs edgeCondition: ConvolveOp.EDGE_NO_OP or

    Define an operator

   BufferedImageOp op = null;
                                                                 ConvolveOp.EDGE ZERO FILL
   op = new ConvolveOp(kernel, ConvolveOp.EDGE NO OP, null);
```

Call the filter() function

```
out = new BufferedImage(width, height, BufferedImage.TYPE_INT_RGB);
op.filter(in, out);
```

#### Not Use filter() Function

Define a filter kernel matrix

```
float[] km = { // low-pass filter kernel
       0.1f, 0.1f, 0.1f, // Suppose the matrix has been flipped
       0.1f, 0.2f, 0.1f,
                           Assignment Project Exam Help
       0.1f, 0.1f, 0.1f
   };
                                https://tutorcs.com

    Calculate convolution on each pixel

   int[] rArray = new int[width*here that: cstutorcs
   for each pixel {
       get the neighbourhood colours of the pixel
       calculate the colour according to the convolution formula
       set the pixel colour in the output image
```

More details in Lab session 6

#### Summary

- What is filtering? What is linear filtering?
- What is convolution?
- How to do sharpening of image?
- What is box filtering, Gausisjam bitte Pinge and Exmad Holfiltering?
- What is separable kernel? Why use separable kernel?