



# Assignment Project Exam Help

## Normalisation – Part 2

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## From BCNF to 3NF

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### Facts

(1) There exists an algorithm that can generate a **lossless decomposition** into BCNF.

(2) However, a BCNF-decomposition that is **both lossless and dependency-preserving** does not always exist.

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- 3NF is a **less restrictive normal form** such that a lossless and dependency preserving decomposition can always be found.

## 3NF - Definition

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- A relation schema  $R$  is in **3NF** if whenever a non-trivial FD  $X \rightarrow A$  holds in  $R$ , then  $X$  is a **superkey** or  $A$  is a **prime attribute**.
- 3NF allows data redundancy but excludes relation schemas with certain kinds of FDs (i.e., partial FDs and transitive FDs).

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## Normalisation to 3NF

- Consider the following FDs of ENROL:

- $\{\text{StudentID}, \text{CourseNo}, \text{Semester}\} \rightarrow \{\text{ConfirmedBy\_ID}, \text{StaffName}\},$
- $\{\text{ConfirmedBy\_ID}\} \rightarrow \{\text{StaffName}\}.$

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ENROL				
<u>StudentID</u>	<u>CourseNo</u>	<u>Semester</u>	ConfirmedBy_ID	StaffName
123456	COMP2400	2010 S2	u12	Jane
123458	COMP2400	2008 S2	u13	Linda
123458	COMP2600	2008 S2	u13	Linda

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- Is ENROL in 3NF?

- $\{\text{StudentID}, \text{CourseNo}, \text{Semester}\}$  is the only key.
- ENROL is not in 3NF because  $\{\text{ConfirmedBy\_ID}\} \rightarrow \{\text{StaffName}\},$   
 $\{\text{ConfirmedBy\_ID}\}$  is not a superkey and  $\{\text{StaffName}\}$  is not prime attribute.

## Normalisation to 3NF

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- Algorithm for a dependency-preserving and lossless 3NF-decomposition

**Input:** a relation schema  $R$  and a set  $\Sigma$  of FDs on  $R$ .

**Output:** a set  $S$  of relation schemas in 3NF, each having a set of FDs

- Compute a **minimal cover**  $\Sigma'$  for  $\Sigma$  and start with  $S = \phi$
- Group FDs in  $\Sigma'$  by their left-hand-side attribute sets
- For each distinct left-hand-side  $X_i$  of FDs in  $\Sigma'$  that includes  $X_i \rightarrow A_1, X_i \rightarrow A_2, \dots, X_i \rightarrow A_k$ :
  - Add  $R_i = X_i \cup \{A_1\} \cup \{A_2\} \dots \cup \{A_k\}$  to  $S$
- Remove all redundant ones from  $S$  (i.e., remove  $R_i$  if  $R_i \subseteq R_j$ )
- if  $S$  does not contain a superkey of  $R$ , add a key of  $R$  as  $R_0$  into  $S$ .
- Project the FDs in  $\Sigma'$  onto each relation schema in  $S$



## Normalisation to 3NF

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$R_1 = X_1 A_1 \dots A_K$ 
...
 $R_n = X_n A$

$X_1 \rightarrow A_1$ 
...
 $X_n \rightarrow A$

$\dots$

$X_1 \rightarrow A_K$ 
...

**A minimal cover**

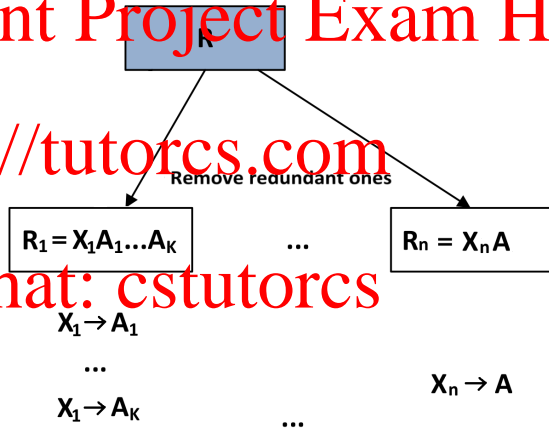


## Normalisation to 3NF

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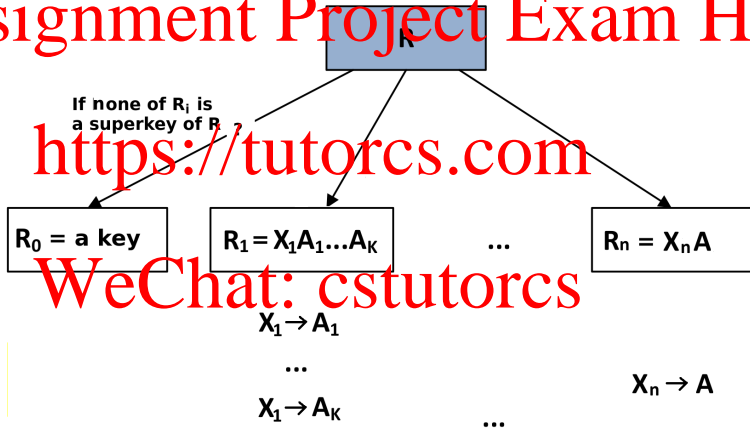
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## Normalisation to 3NF

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## Minimal Cover – The Hard Part!

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Let  $\Sigma$  be a set of FDs. A **minimal cover**  $\Sigma_m$  of  $\Sigma$  is a set of FDs such that

- 1  $\Sigma_m$  is equivalent to  $\Sigma$ , i.e., start with  $\Sigma_m = \Sigma$ ;
- 2 **Dependent:** each FD in  $\Sigma_m$  has only a single attribute on its right hand side, i.e., replace each FD  $X \rightarrow \{A_1, \dots, A_k\}$  in  $\Sigma_m$  with  $X \rightarrow A_1, \dots, X \rightarrow A_k$ ;
- 3 **Determinant:** each FD has as few attributes on the left hand side as possible, i.e., for each FD  $X \rightarrow A$  in  $\Sigma_m$ , check each attribute  $B$  of  $X$  to see if we can replace  $X \rightarrow A$  with  $(X - B) \rightarrow A$  in  $\Sigma_m$ ;
- 4 Remove a FD from  $\Sigma_m$  if it is redundant.



## Minimal Cover

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### Theorem:

The minimal cover of a set of functional dependencies  $\Sigma$  always exists but is not necessarily unique.

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- **Examples:** Consider the following set of functional dependencies:

$$\Sigma = \{A \rightarrow BC, B \rightarrow C, B \rightarrow A, C \rightarrow AB\}$$

$\Sigma$  has two different minimal covers:

- $\Sigma_1 = \{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$
- $\Sigma_2 = \{A \rightarrow C, C \rightarrow B, B \rightarrow A\}$



## Minimal Cover - Examples

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- The set  $\{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$  can be reduced to  $\{A \rightarrow B, B \rightarrow C\}$ , because  $\{A \rightarrow C\}$  is implied by the other two.
- Given the set of FDs  $\Sigma = \{B \rightarrow A, D \rightarrow A, AB \rightarrow D\}$ , we can compute the minimal cover of  $\Sigma$  as follows:

- 1 start from  $\Sigma$ ;
- 2 check whether all the FDs in  $\Sigma$  have only one attribute on the right hand side (look good);
- 3 determine if  $AB \rightarrow D$  has any redundant attribute on the left hand side ( $AB \rightarrow D$  can be replaced by  $B \rightarrow D$ );
- 4 look for a redundant FD in  $\{B \rightarrow A, D \rightarrow A, B \rightarrow D\}$  ( $B \rightarrow A$  is redundant);

Therefore, the minimal cover of  $\Sigma$  is  $\{D \rightarrow A, B \rightarrow D\}$ .



## Normalisation to 3NF – Example

- Consider ENROL again:

- $\{ \text{StudentID}, \text{CourseNo}, \text{Semester} \} \rightarrow \{ \text{ConfirmedBy\_ID}, \text{StaffName} \}$
- $\{ \text{ConfirmedBy\_ID} \} \rightarrow \{ \text{StaffName} \}$

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StudentID	CourseNo	Semester	ConfirmedBy_ID	StaffName
...	...	...	...	...

- Can we normalise ENROL into 3NF by a lossless and dependency preserving decomposition?

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## Normalisation to 3NF – Example

- Consider ENROL again:

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- $\{ \text{ConfirmedBy\_ID} \} \rightarrow \{ \text{StaffName} \}$

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StudentID	CourseNo	Semester	ConfirmedBy_ID	StaffName
...	...	...	...	...

- A **minimal cover** is  $\{ \{ \text{StudentID}, \text{CourseNo}, \text{Semester} \} \rightarrow \{ \text{ConfirmedBy\_ID} \}, \{ \text{ConfirmedBy\_ID} \} \rightarrow \{ \text{StaffName} \} \}$ .

- Hence, we have:

- $R_1 = \{ \text{StudentID}, \text{CourseNo}, \text{Semester}, \text{ConfirmedBy\_ID} \}$  with  $\{ \text{StudentID}, \text{CourseNo}, \text{Semester} \} \rightarrow \{ \text{ConfirmedBy\_ID} \}$
- $R_2 = \{ \text{ConfirmedBy\_ID}, \text{StaffName} \}$  with  $\{ \text{ConfirmedBy\_ID} \} \rightarrow \{ \text{StaffName} \}$
- Omit  $R_0$  because  $R_1$  is a superkey of ENROL.

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## 3NF - Exercises

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- Let us do some exercises for the 3NF-decomposition algorithm

• **Exercise 1:**  $R = \{A, B, C, D\}$  and  $\Sigma = \{A \rightarrow B, B \rightarrow C, AC \rightarrow D\}$ :

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• **Exercise 2:**  $R = \{A, B, C, D\}$  and  $\Sigma = \{AD \rightarrow B, AB \rightarrow C, C \rightarrow B\}$ :

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## 3NF - Exercises

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- Let us do some exercises for the 3NF-decomposition algorithm.

• **Exercise 1:**  $R = \{A, B, C, D\}$  and  $\Sigma = \{A \rightarrow B, B \rightarrow C, AC \rightarrow D\}$ :

- $\{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$  is a minimal cover.
- $R_1 = ABD, R_2 = BC$  (omit  $R_0$  because  $R_1$  is a superkey of  $R$ )
- The 3NF-decomposition is  $\{ABD, BC\}$ .

• **Exercise 2:**  $R = \{A, B, C, D\}$  and  $\Sigma = \{AD \rightarrow B, AB \rightarrow C, C \rightarrow B\}$ :

- $\Sigma$  is its own minimal cover.
- $R_1 = ABD, R_2 = ABC, R_3 = CB$  (omit  $R_3$  because  $R_3 \subseteq R_2$  and omit  $R_0$  because  $R_1$  is a superkey of  $R$ )
- The 3NF-decomposition is  $\{ABD, ABC\}$ .

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