



Assignment Project Exam Help

Functional Dependencies – Part 2

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Definition and Identification

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Codd and Functional Dependencies

- **Functional dependencies** (FDs) were introduced by Codd in 1971¹
- Edgar F. Codd of IBM Research (1923–2003) invented the **relational data model** for data management in 1970.
- He received the ACM Turing Award in 1981 for his contributions on the theoretical foundations of relational databases:

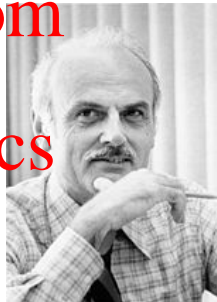
- **Functional dependencies**

- **Normalization**

- Boyce–Codd Normal Form (BCNF)

- **Query languages**

- Relational Calculus
 - Relational Algebra



¹ Further Normalization of the Data Base Relational Model. E. F. Codd, IBM Research Report, San Jose, California, 1971.

Why Functional Dependencies?

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- We need some **formal way** of analysing whether a database schema is well-designed, or why one is better than another.
- FDs are developed to define the **goodness** and **badness** of (relational) database design in a formal way.
 - **Top down**: start with a relation schema and FDs, and produce smaller relation schemas in certain normal form (called *normalisation*).
 - **Bottom up**: start with attributes and FDs, and produce relation schemas (*not popular in practice*).

FDs tell us “relationship between and among attributes”!



Functional Dependencies – Informal Description

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- We have two FDs on ENROLMENT.

ENROLMENT					
Name	<u>StudentID</u>	DoB	<u>CourseNo</u>	<u>Semester</u>	Unit
Tom	123456	25/01/1988	COMP2400	2010 S2	6
Tom	123456	25/01/1988	COMP8740	2011 S2	12
Michael	123458	21/04/1985	COMP2400	2009 S2	6
Michael	123458	21/04/1985	COMP8740	2011 S2	12
Fran	123457	11/09/1987	COMP2400	2009 S2	6

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- StudentID **functionally determines** Name and DoB, i.e.,
 $\{\text{StudentID}\} \rightarrow \{\text{Name}, \text{DoB}\}$
- CourseNo **functionally determines** Unit, i.e.,
 $\{\text{CourseNo}\} \rightarrow \{\text{Unit}\}$



Functional Dependencies – Informal Description

- A **FD** says that, within a relation, the values of some attributes determine the values of other attributes.

Animal	→	Legs
Ostrich		2
Wombat		4



- If attributes A, B, C determine attributes D, E , then we write

$$\{A, B, C\} \rightarrow \{D, E\}$$

- This means, if two tuples have the same values for A, B and C , then they must also have the same values for D and E .
- A, B and C are the **determinant**, while D and E are the **dependent**.



Formal Definition

- Let R be a relation schema.

- A **FD** on R is an expression $X \rightarrow Y$ with attribute sets $X, Y \subseteq R$.

- A relation $r(R)$ **satisfies** $X \rightarrow Y$ on R if, for any two tuples $t_1, t_2 \in r(R)$, whenever the tuples t_1 and t_2 coincide on values of X , they also coincide on values of Y .

$$t_1[X] = t_2[X]$$



$$t_1[Y] = t_2[Y]$$

- A FD is **trivial** if it can always be satisfied, e.g.

- $\{A, B, C\} \rightarrow \{C\}$
- $\{A, B, C\} \rightarrow \{A, B\}$

- Syntactical convention:** (1) Instead of $\{A, B, C\}$, we may use ABC . (2) A, B, \dots for individual attributes and X, Y, \dots for sets of attributes.



Exercise - Functional Dependencies on Relations

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- Consider the following relations with attributes $\{A, B, C, D, E\}$. Do they satisfy:
(1) $AB \rightarrow E$; (2) $C \rightarrow DE$;

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$r_1(R)$					$r_2(R)$				
A	B	C	D	E	A	B	C	D	E
1	4	1	9	4	1	3	1	3	8
1	4	2	8	9	1	3	2	4	8
1	4	3	8	9	1	2	2	4	9

- Check:

	$r_1(R)$	$r_2(R)$
(1) $AB \rightarrow E$	no	yes
(2) $C \rightarrow DE$	yes	no

How to Identify FDs in General?

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- A functional dependency specifies a constraint on the relation schema that must hold **at all times**.

- In real-life applications we often use the following approaches:

(1) **Analyse data requirements**

Can be provided in the form of discussion with application users and/or data requirement specifications.

(2) **Analyse sample data**

Useful when application users are unavailable for consultation and/or the document is incomplete.

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(1) Identifying FDs - Analyse Data Requirements

- Consider the following relation schema:

$RENTAL = \{CustID, CustName, PropertyNo, DateStart, Owner\}$.

- Data requirements:**

- Each customer can be uniquely identified by his or her customer ID.

$\{CustID\} \rightarrow \{CustName\}$

- A customer cannot rent two or more properties from the same date.

$\{CustID, DateStart\} \rightarrow \{PropertyNo\}$

- A customer cannot rent the same property more than once.

$\{PropertyNo, CustID\} \rightarrow \{DateStart\}$

- Each property can be uniquely identified by its owner.

$\{Owner\} \rightarrow \{PropertyNo\}$



(2) Identifying FDs - Analyse Sample Data

- Can you find some FDs of ENROLMENT based on the sample data?

ENROLMENT					
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Michael	123458	21/04/1985	COMP8740	2011 S2	12
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- We may have:

- $\{ \text{StudentID} \} \rightarrow \{ \text{Name}, \text{DoB} \}$
- $\{ \text{CourseNo} \} \rightarrow \{ \text{Unit} \};$
- $\{ \text{StudentID}, \text{CourseNo}, \text{Semester} \} \rightarrow \{ \text{Name}, \text{DoB}, \text{Unit} \};$
- $\{ \text{Name} \} \rightarrow \{ \text{StudentID} \} \times;$
- $\{ \text{DoB} \} \rightarrow \{ \text{StudentID} \} \times;$
-

Limitations: Sample data needs to be a true representation of **all possible values** that the database may hold.