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Term 2, 2022

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4. Puzzle

String matching algorithms

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Suppose you have an alphabet consisting of d symbols. Strings are just sequences of these symbols.

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Problem

Determine whether a string $B = b_0 b_1 \dots b_{m-1}$ (the pattern) appears a continuous substring of a much longer string $A = a_0 a_1 \dots a_{n-1}$ (the text).

String matching problem

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The "naïve" algorithm for string matching is as follows: for every position in A, check as the character tutores. Com

Even with early exit, this runs in O(mn) time in the worst case.

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Question

Can we do better?

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String matching with hashing

Assignment han recombine various produce an efficient string matching algorithm.

- We compute a hash value for the string $B = b_0 b_1 b_2 \dots b_{m-1}$ in the following way UOICS. COM
- Hereafter, when we refer to an integer a_i or b_i , we really mean the ID of the symbol a_i or b_i .

We can therefore identify B with a sequence of IDs

ASSI by the property of th

- Next we choose a large prime number p and define the hash value of B as $H(B) = h(B) \mod p$.

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- We want to find efficiently plus such that the string of length m of the form $a_s a_{s+1} \dots a_{s+m-1}$ and string $b_0 b_1 \dots b_{m-1}$ are equal.
- Five a Configurate subcrist A we also compute its hash value as

$$H(A_s) = d^{m-1}a_s + d^{m-2}a_{s+1} + \ldots + d^1a_{s+m-2} + a_{s+m-1} \mod p.$$

Assignment Project Exam Help If they disagree, we know that there is no match.

they agree there might be a match To confirm this, we'll check it character by character.

- There are O(n) substrings A_s to check. If we compute each has value $H(A_s)$ in O(n) substrings A_s to check. If we compute each naïve algorithm.
- This is where recursion comes into play: we do not have compute the hash value $H(A_{s+1})$ "from scratch". Instead, we can compute it efficiently from the previous hash value $H(A_s)$.

$$H(A_s) = d^{m-1}a_s + d^{m-2}a_{s+1} + \ldots + a_{s+m-1} \mod p.$$

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Multiplying both sides by d gives

since $A_{s+1} = a_{s+1} \dots a_{s+m-1} a_{s+m}$.

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 $H(A_{s+1}) = d \cdot H(A_s) - d^m a_s + a_{s+m} \bmod p.$

https://tutorcs.com Thus we can compute $H(A_{s+1})$ from $H(A_s)$ in constant time.

When implementing this, we need to make sure that the

intermediate values are not too large. In particular, we need to choose p such that (d+1)p fits in a single register. This is in conflict with the desired to choose large primes for better hashing.

Rabin-Karp Algorithm

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- 1. First compute H(B) and $H(A_0)$ in O(m) time using Horner's https://tutorcs.com
- 2. Then compute the O(n) subsequent values of $H(A_s)$ for s>0each in constant time using the recurrence above.

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3. Compare $H(A_s)$ with H(B), and if they are equal then confirm the potential match by checking the strings A_s and B characterby-character.

Rabin-Karp Algorithm

Assignment Project Exam Help Since p was chosen large, the false positives (where

- Since p was chosen large, the false positives (where $H(A_s) = H(B)$ but $A_s \neq B$) are very unlikely, which makes the algorithm run fast in the average case.
- However, as always when we use hashing, we cannot achieve useful bounds for the worst case performance.
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- So we now look for algorithms whose worst case performance is guaranteed to be linear.

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m+1 many states $0,1,\ldots,m$, which correspond to the number of characters matched thus far, and

https://tutorcs.com a transition function $\delta(k,a)$, where $0 \le k \le m$ and $a \in S$.

• Support hat that k Characters of the pattern B, and that a is the next character in the text. Then $\delta(k,a)$ is the new state after character a is read, i.e. the largest k' so that the last k' characters of A (ending at the new character c) match the first k' characters of B.

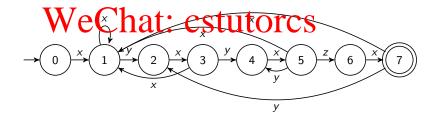
A stain example consider the string a syxy extra the Help

-	ķ	matched	X	у	Z	
https://	/ (]	utoro	S	C	0	m
	1	Х	1	2	0	
	2	xy	3	0	0	
Wach	3	xyx d	14	4	0	
WeCh	al	x xyxyx	U, I	6	10	CS
	5	xyxyx	1	4	6	
	6	xyxyxz	7	0	0	
	7	xyxyxzx	1	2	0	
	7		1	2	<u> </u>	

This table can be visualised as a state transition diagram. From Sex 1 5519 1 Median arrived Cot for each a 170 ter a let personal could be encountered next. Arrows pointing to state 0 have been omitted for clarity.

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B = xyxyxzx



Assignment te Phroject to Enx, annow Help fill the table?

- lettps://tuteorosfixcom k of the string
- Reing at craft k means that so far we have matched the prefix BY. CSTUTOTCS
- If we now see an input character a, then $\delta(k,a)$ is the largest ℓ such that the prefix B_{ℓ} of string B is a suffix of the string $B_k a$.

Question Sugnment the research that x amplies of the part of the

- https://methodics.e.g.k. then $\ell = k + 1$ and so $\delta(k, a) = k + 1$.
- But what if and the Then set can't extend our match from length k to k + 1.
- We'd like to extend some shorter match instead.
- Any other candidates to be extended must be both a proper suffix of B_k and a prefix of B.

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Definition

Let $\pi(k)$ be the largest integer ℓ such that the prefix B_ℓ of B is a property $B_k / LUIOTCS.COM$

 \mathcal{B}_ℓ is therefore the longest substring which appears at both the start with the end of $\mathcal{B}_{k,\ell}$ (allowing partial but not total overlap).

We will refer to π as the failure function.

The transition function $\delta(k,a)$ is closely related to this failure related to the related to the related to the related related

- If $a = b_k$, then $\delta(k, a) = k + 1$.
 - https://tutorcs.com Otherwise, we look to extend a shorter match. The next
- candidate has length $\pi(k)$, so we check whether $a = b_{\pi(k)}$ and if so we have $\delta(k, a) = \pi(k) + 1$.

• Otherwise, the next candidate has length $\pi(\pi(k))$ (why?) and so on.

We will describe the algorithm and complete the analysis entirely in terms of the failure function.

Assignment Project Exam Help each index of the pattern B.

- https://etulitediscs.ychip.pgramming.
- Naturally, the subproblems are the $\pi(k)$ values for each n, and the base case is $\pi(k)$ n
- Suppose we have solved $\pi(1), \ldots, \pi(k)$. How do we find $\pi(k+1)$?

- Recall that $B_{\pi(k)} = b_0 \dots b_{\pi(k)-1}$ is the longest prefix of B Assignment sufficient. $E_1 \times Help$
 - To compute $\pi(k+1)$, we first try to extend this match, by ehecking whether $b_k = b_{\pi(k)}$.

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 - If true, then $\pi(k+1) = \pi(k) + 1$.
 - In the proper cannot extend B_1 what's the next longest prefix of B which is a proper suffix of B_k ?
 - It's $B_{\pi(\pi(k))}$! So we check whether $b_k = b_{\pi(\pi(k))}$.
 - If true, then $\pi(k+1) = \pi(\pi(k)) + 1$.
 - If false, check whether $b_k = b_{\pi(\pi(\pi(k)))} \dots$

```
1: function Compute-Failure-Function(B)
  ignment.Project Exam Help
     for k = 1 to m - 1 do
        while \ell > 0 do
6:
          js:##tutorcs.com
9:
10:
           end if
11:
           if \ell > 0 then
              hat: cstutores
12:
13:
14:
              break
15:
           end if
16:
        end while
17:
        \pi[k+1] \leftarrow \ell
18:
     end for
     return \pi
19:
20: end function
```

• What is the complexity of this algorithm? There are O(m)Assignment Project Exam !Help

- No! It is actually linear, i.e. O(m).
- https://tutorcs.com
 Maintain two pointers: the left pointer at $k-1-\ell$ (the start point of the match we are trying to extend) and the right

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- After each 'step' of the algorithm (i.e. each comparison between b_k and b_ℓ), exactly one of these two pointers is moved forwards.
- Each can take up to m values, so the total number of steps is O(m). This is an example of amortisation.

• We can now do our search for the pattern B in the text A.

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- - If true, then the answer for A_{i+1} is s+1

We check whether $a_i = b_{\pi(s)} \dots$

- If the answer for any A_i is m, we have a match!
 - Reset to state $\pi(m)$ to detect any overlapping full matches.
- By the same two pointer argument, the time complexity is O(n).

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```
2: n \leftarrow |A|

3: m \leftarrow |B|

4: h_s \leftarrow |B|

6: for i = 0 to n - 1 do

7: while s \ge 0 do

8: w \leftarrow |A|

6: w \leftarrow |B|

7: w \leftarrow |B|

8: w \leftarrow |B|

9: w \leftarrow |B|

9: w \leftarrow |B|

10: w \leftarrow |B|

10: w \leftarrow |B|

11: w \leftarrow |B|

12. w \leftarrow |B|

13. w \leftarrow |B|

14. w \leftarrow |B|

15. w \leftarrow |B|

16. w \leftarrow |B|

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18. w \leftarrow |B|

19. w \leftarrow |B|

19. w \leftarrow |B|

10. w \leftarrow |B|

10. w \leftarrow |B|

11. w \leftarrow |B|
```

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```
14:
            else
    https:///tutorcs.com
15:
         end while
17:
         if s=m then
18:
           print match found from index i—m
19:
20:
         end if
21:
      end for
22:
23: end function
```

Looking for imperfect matches

Sometimes we are not interested in finding just the perfect Help matteres, but also in matches that might have a few errors, such as particular and replacements.

Problemttps://tutorcs.com

Instance: a text

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a pattern $B = b_0 b_1 b_2 \dots b_{m-1}$ where $m \ll n$, and an integer $k \ll m$.

Task: find all matches for B in A which have up to k errors.

Looking for imperfect matches

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Split B into k+1 substrings of (approximately) equal length. Within any match in A with at most k errors, at least one of these k+1 part of S must be nationally S

For each of the k + 1 parts of B, we use the Knuth-Morris-Pratt algorithm to find all perfect matches in A.

Then for each of these matches, we test by brute force whether the remaining parts of B match sufficiently with the appropriate parts of A.

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4. Puzzle

On a rectangular table there are 25 round coins of equal size, and no two of these coins overlap. You observe that in current arrangement, it is not possible to add another coin without overlapping any of the existing coins and without the coin falling off the table (for a coin to stay on the table its centre must be within the table).

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Show that it is possible to completely cover the table with 100 coins (allowing overlaps).



That's All, Folks!!