# Assignment Project Exam Help

## https://textofforrammig

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# Assignment Project Exam Help

1. Example Problems https://tutorcs.com

2. Linear Programming

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3. Puzzle

# Problem Pro

- its price per gram p<sub>i</sub>;
- the number of calories c; per gram, and
- for each of 13 vitamins  $V_1, \dots, V_{13}$ , the content  $v_{i,j}$  in milligrams of vitamin  $V_i$  in one gram of food source  $f_i$ .

**Task:** find a combination of quantities of food sources such that:

- the to a number of calcies the total to a recommended daily value of 2000 calories;
- for each  $1 \le j \le 13$ , the total intake of vitamin  $V_j$  is at least the recommended daily intake of  $w_j$  milligrams, and
- the price of all food per day is as low as possible.

# Suppose we take $x_i$ grams of each food source $F_i$ for $1 \le i \le n$ . A step the total number of calories must satisfy

# https://tutores?com

For each  $1 \le j \le 13$ , the total amount of vitamin  $V_j$  in all foot rules satisfalt. CSTULOTCS

$$\sum_{i=1}^n x_i v_{i,j} \ge w_j.$$

■ Implicitly, all the quantities must be non-negative numbers, i.e.  $x_i \ge 0$  for all  $1 \le i \le n$ .

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• Our goal is to minimise the objective function, which is the that  $y = \sum x_i p_i$ .

• Mt techatint CS tutbjetic Senction are linear.

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#### Problem

Instance: you are a politician and you want to ensure an election victor by tracking certain plante Ctoth Cectone. You can promise to build:

- bridges, each costing 3 billion;
- rWanfits hat tost as touth orcs
- Olympic swimming pools, each costing 1 billion.

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You were told by your, wise advisers that

- attbos you truttofice Sociol Mity votes, 7% of suburban votes and 9% of rural votes;
- each rural airport you promise brings you no city votes, 2% of structure votes and 15% of rural total CS
- each Olympic swimming pool promised brings you 12% of city votes, 3% of suburban votes and no rural votes.

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#### Problem (continued)

In order to Syon have the Company of the city, suburban and rural votes.

Task: decide now many bridges, airports and pools to promise in order to guarantee an election win at minimum cost to the budget.

# Assignment blogs jecit bexamof Help airports $x_a$ and the number of swimming pools $x_p$ .

We now see that the problem amounts to minimising the dictive see that the following constraints are satisfied:

$$\begin{array}{c} \begin{array}{c} 0.05x_b \\ 0.05x_b \\ 0.09x_b \\ \end{array} + \begin{array}{c} 0.12x_p \geq 0.51 \\ 0.09x_b \\ \end{array} \begin{array}{c} (\text{city votes}) \\ 0.09x_b \\ \end{array} \begin{array}{c} 0.05x_b \\ 0.05x_b \\ \end{array} \begin{array}{c} (\text{city votes}) \\ 0.09x_b \\ \end{array} \begin{array}{c} (\text{city votes}) \\ 0.09x_b \\ \end{array} \begin{array}{c} (\text{city votes}) \\ (\text{city vot$$

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- you can eat 1.56 grams of chocolate, but proposite type 1.56 by 1.50 b
- The second example is an example of an Integer Linear Regeranting problem, which requires all the solutions to be integer. CSTUTOTCS
- Such problems are MUCH harder to solve than the "plain" Linear Programming problems whose solutions can be real numbers.

## Solving Linear Programming problems

# Assign won't see algorithms which solve Literoblems in the lens of these problems to the further.

- There is solynortial time in Solynortial tim
- It ractice we typically use the SIMPLEX algorithm instead; its worst case time complexity is exponential, but it is very efficient in the 'average' case.
- There is no known polynomial time algorithm for Integer Linear Programming!

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and the constraints are of the form

$$x_j \geq 0$$
  $(1 \leq j \leq n)$ .

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- get a more compact representation of linear programs, we use vectors and matrices.
- het x represent/2 (column) vector, com  $\mathbf{x} = \langle x_1 \dots x_n \rangle^T.$
- Define a partial ordering on the vectors in  $\mathbb{R}^n$  by  $\mathbf{x} \leq \mathbf{y}$  if and only if the corresponding inequalities hold coordinate-wise, i.e., if and only if  $x_j \leq y_j$  for all  $1 \leq j \leq n$ .

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$$\mathbf{c} = \langle c_1 \dots c_n \rangle^T \in \mathbb{R}^n,$$
 the coefficients in the constraints of an exponential constraints of the constraints of the

$$A = (a_{ij})$$
and the light Charles State of the Charles State of the

$$\mathbf{b} = \langle b_1 \dots b_m \rangle^T \in \mathbb{R}^m.$$

## Assignment Project Exam Help Then the standard form can be formulated simply as:

- $\blacksquare$  maximize  $\mathbf{c}^T \mathbf{x}$
- Subject to the following two (matrix vector) constraints:

 $Ax \leq b$ 

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Thus, a Linear Programming optimisation problem can be specified

Thus, a Linear Programming optimisation problem can be specified as a triplet  $(A, \mathbf{b}, \mathbf{c})$ , which is the form accepted by most standard LP solvers.

#### Translating other constraints to Standard Form

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- The Standard Form doesn't immediately appear to handle the full generality of LP problems. https://tutorcs.com
- LP problems could have:
  - equality constraints
    - Wung onstrained trariables (i.e. totentially negative values
      - absolute value constraints

#### Equality constraints

# Assignment Project Exam Help $\sum_{a_{ij}x_i=b_j.}^{\text{An LP problem may include equality constraints of the form} \sum_{a_{ij}x_i=b_j.}^{\text{Note of the problem may include equality constraints of the form}$

# https://tutorcs.com Each of can be replaced by two inequalities:

$$\sum_{i=1}^n a_{ij}x_i \leq b_j.$$

Thus, we can assume that all constraints are inequalities.

#### Unconstrained variables

# Assimonative. In general, a "natura formulation" of a problem as a Linear of the control of the

- Hyreton the Standard Form does imposer this constraint.
- This poses no problem, because each occurrence of an unconstrained variable  $x_i$  can be replaced by the expression  $X_i X_i^*$

where  $x'_j, x^*_j$  are new variables satisfying the inequality constraints

$$x_j'\geq 0,\ x_j^*\geq 0.$$

#### Absolute value constraints

For a vector

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$$|\mathbf{x}| = \langle |x_1|, \ldots, |x_n| \rangle^T.$$

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Some problems are naturally translated into constraints of the

 Some problems are naturally translated into constraints of the form

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This also poses no problem because we can replace such constraints with two linear constraints:

$$A\mathbf{x} \leq \mathbf{b}$$
 and  $-A\mathbf{x} \leq \mathbf{b}$ ,

because  $|x| \le y$  if and only if  $x \le y$  and  $-x \le y$ .

## Summary of Standard Form

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and

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Any vector  $\mathbf{x}$  which satisfies the two constraints is called a *feasible solution*, regardless of what the corresponding objective value  $\mathbf{c}^T \mathbf{x}$  might be.

# A saing remple tent to be following better interesting problem

```
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subject to

WeChat+x_2+3x_3 \le 30 (2)

4x_1+x_2+2x_3 \le 36 (4)
```

 $x_1, x_2, x_3 > 0$ 

(5)

# Assignment Project Exam Help $z(x_1, x_2, x_3) = 3x_1 + x_2 + 2x_3$

be, without violating the constraints?
We can achieve a crude bound by Cdoing inequalities (2) and (3), to obtain

$$3x_1 + 3x_2 + 8x_3 \le 54.$$

Since Wardles and instrument to the legative, we are assured that

$$3x_1 + x_2 + 2x_3 \le 3x_1 + 3x_2 + 8x_3 \le 54$$
,

i.e. the objective does not exceed 54. Can we do better?

# Assi ginarountion of the describes $x_1, y_2, y_2 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to be used to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_3, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_3, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_3, y_3 \ge 0$ to $x_1, y_2, y_3 \ge 0$ to $x_2, y_3 \ge 0$ to $x_3, y_3 \ge$

$$y_1(x_1 + x_2 + 3x_3) \le 30y_1 \tag{6}$$

Then, summing up all these inequalities and factoring, we get

$$+ x_2(y_1 + 2y_2 + y_3)$$
  
 $+ x_3(3y_1 + 5y_2 + 2y_3)$   
 $< 30y_1 + 24y_2 + 36y_3$ .

If we compare this with our objective (1) we see that if we choose

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then

Combining this with (6) - (8) we get

$$30y_1 + 24y_2 + 36y_3 \ge 3x_1 + x_2 + 2x_3 = z(x_1, x_2, x_3).$$

# Assissint montro in the projective $z(x_1, x_2, x_3)$ in the original problem P, we have to find

 $y_1, y_2, y_3$  which solve problem  $P^*$ :

subject to:

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$$_{2y}^{y_1+2y_2+4y_3} \ge 3$$
 (10)

$$3y_1 + 5y_2 + 2y_3 \ge 2 \tag{12}$$

$$y_1, y_2, y_3 \ge 0 \tag{13}$$

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https:
$$\frac{z^{*}(y_{1})}{tut} = \frac{30}{5}x_{1} + x_{2} + 2x_{3} + 36x_{3}$$
  
=  $z(x_{1}, x_{2}, x_{3})$ 

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The new problem  $P^*$  is called the *dual problem* of P.

Let us now repeat the whole procedure in order to find the dual of A special which will be denoted by the constant of the content of the cont

## Summy the up no tactom structors

$$y_1(z_1 + z_2 + 3z_3) + y_2(2z_1 + 2z_2 + 5z_3) + y_3(4z_1 + z_2 + 2z_3) \ge 3z_1 + z_2 + 2z_3$$

(14)

If we choose multipliers  $z_1, z_2, z_3$  so that

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 $\underset{\text{we will have}}{\text{https:}}//\underset{tutorcs.com}{\overset{4z_1+z_2+2z_3\leq 36}{\text{com}}}$ 

WeChat. 
$$(z_1 + z_2 + 3z_3)$$
  
 $+ y_3(4z_1 + z_2 + 2z_3)$   
 $\leq 30y_1 + 24y_2 + 36y_3$ 

Combining this with (14) we get

$$3z_1 + z_2 + 2z_3 \le 30y_1 + 24y_2 + 36y_3.$$

# Assignment he double just crogram ( $x_1$ ) and $x_2$ the maximising the objective $3z_1 + z_2 + 2z_3$ subject to the constraints

https://turtorc3 $\frac{1}{2} \frac{1}{2} \frac{1$ 

 $4z_1 + z_2 + 2z_3 \le 36$ 

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This is exactly our starting program P, with only the variable names changed! Thus, the double dual program  $(P^*)^*$  is just P itself.

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- It appeared at first that looking for the multipliers  $y_1, y_2, y_3$  did not help much, because it only reduced a maximisation problem.
- It is useful at this point to remember how we proved that the Ford-Fullersch algorithm produces a maximal flow, by showing that it terminates only when we reach the capacity of a minimal cut.

### Primal and dual linear programs

In general, the *primal* Linear Program P and its *dual*  $P^*$  are:

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https://tutifics.bcom 
$$i \leq m$$

and  $x_1,\ldots,x_n\geq 0$ ;

subject to 
$$\sum_{i=1}^m a_{ij}y_i \ge c_j \qquad (1 \le j \le n)$$

and  $y_1, \ldots, y_m \ge 0$ .

#### Primal and dual linear programs

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$$\begin{array}{c} \textbf{https:} & \textbf{maximize} & z(\mathbf{x}) = \mathbf{c}^T \mathbf{x}, \\ \textbf{https:} & \textbf{subjection COAR} \leq \mathbf{b} \\ & \textbf{and} & \mathbf{x} \geq 0; \\ \textbf{WeChier to CSTUTORS} \geq \mathbf{c} \\ & \textbf{and} & \mathbf{y} \geq 0. \end{array}$$

# Assignment Phihotsecte Exams Help and x > 0 is called a feasible solution, regardless of what the

and  $\mathbf{x} \geq 0$  is called a *feasible solution*, regardless of what the corresponding objective value  $\mathbf{c}^T \mathbf{x}$  might be.

## Theorem UDS://tutorcs.com

If  $\mathbf{x} = \langle x_1 \dots x_n \rangle$  is any feasible solution for P and  $\mathbf{y} = \langle y_1 \dots y_m \rangle$  is any feasible solution for  $P^*$ , then:

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$$z(\mathbf{x}) = \sum_{j=1}^{n} c_j x_j \leq \sum_{i=1}^{n} b_i y_i = z^*(\mathbf{y})$$

# A Sport Project Exam Help Since and y are feasible solutions for P and P\* respectively, we

can use the constraint inequalities, first from  $P^*$  and then from P to obtain

to obtain tps://tutorcs.com
$$z(\mathbf{x}) = \sum_{j=1}^{n} c_j x_j \le \sum_{j=1}^{n} \left(\sum_{i=1}^{n} a_{ij} y_i\right) x_j$$

WeChat: 
$$(\underbrace{\sum_{j=1}^{c} a_{ij} x_j}_{j}) y_i \leq \sum_{i=1}^{c} b_i y_i$$

$$=z^*(\mathbf{y}).$$

# A Significant of the objective of $P^*$ is an upper bound for the set of all values of (the objective of P for) all feasible solutions of P, and every feasible solution of P is a lower bound for the set of feasible solutions for $P^*$ .

Solutions for P
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Solutions for P\*

# Solution to $P^*$ , this common value must be the maximal feasible value of the objective of P and the minimal feasible value of the objective of $P^*$ . Solutions for P

Solutions for P\*

# Assignment Project Exam Help If we use a search procedure to find an optimal solution for P

- If we use a search procedure to find an optimal solution for P we know when to stop: when such a value is also a feasible solution for P\*/./tutorcs.com
   This is why the most commonly used LP solving method, the
- This is why the most commonly used LP solving method, the SIMPLEX method, produces an optimal solution for P: because it stops at a value of the primal objective which is a value of the livel objective.
- See the supplemental notes for the details and an example of how the SIMPLEX algorithm runs.

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There are five sisters in a house.

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- Jennifer is playing chess.
- Catherine is cooking.
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What is Helen, the fifth sister, doing?



That's All, Folks!!