## Assignment Project Exam Help Foundations of Computer Science UNSWITTER: 4: Letter CS. COM

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### Assignment Project Exam Help

Laws of Set Operations
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Two Useful Results

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Laws of Set Operations

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### Assignment Project Exam Help

- Explicitly list elements
- 2 Take top Set of the source Sy emina the elements
- 3 Build up from existing sets using Set Operations

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### Set Operations

#### **Definition**

Assignment Project Exam Help  $A \subseteq \{x : x \in A \text{ or } x \in B\}.$ 

```
 \begin{array}{c} A \cap B \text{ --intersection, (a and b):} \\ \mathbf{ntps:} / \mathbf{tutorcs.com} \\ A \cap B = \{x : x \in A \text{ and } x \in B\}. \end{array}
```

```
A^c - complement (with respect to a universal set \mathcal{U}): A^c = \{x : x \in \mathcal{U} \text{ and } x \notin A\}.
```

We say that A, B are **disjoint** if  $A \cap B = \emptyset$ 

### Set Operations

Other set operations

### Assignment Project Exam Help A B set difference, relative complement (a but not b):

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 $A \oplus B$  – symmetric difference (a and not b or b and not a; also

known as a or beaclusively; a xor,b): 
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$$A \oplus B = (A \setminus B) \cup (B \setminus A)$$

A Venn Diagram is a simple graphical approach to visualize the ssignment Project Exam Help https://tutorcs.com WeChat: cstutorcs

A Venn Diagram is a simple graphical approach to visualize the ssignment Project Exam Help https://tutorcs.com WeChat: estutores  $A \cup B$ 

A Venn Diagram is a simple graphical approach to visualize the ssignment Project Exam Help https://tutorcs.com WeChat: estutores  $A \cap B$ 

A Venn Diagram is a simple graphical approach to visualize the Assignment Project Exam Help https://tutorcs.com WeChat: cstutorcs  $A^{c}$ 

A **Venn Diagram** is a simple graphical approach to visualize the ssignment Project Exam Help https://tutorcs.com WeChat: cstutorcs  $A \setminus B$ 

A Venn Diagram is a simple graphical approach to visualize the ssignment Project Exam Help https://tutorcs.com WeChat: cstutorcs  $A \oplus B$ 

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#### Set Equality

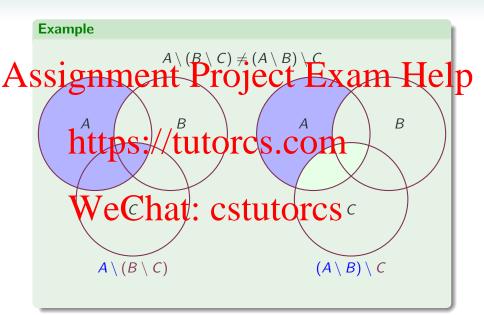
### As significant Projection The same elemental p

To show equality:

- Examine all the elements
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- Use the Laws of Set Operations

### Venn diagrams can help visualize, but are not rigorous.

### Example



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#### Example

Show https: %/tutorcs.com

 $(0,4) = \{1,2,3\} = \{3,2,1\}.$ 

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#### Examples

### Assignment Project Exam Help Show $\{n : n \in \mathbb{Z} \text{ and } n^2 < 5\} = \{n : n \in \mathbb{Z} \text{ and } |n| \le 2\}$

### https://tutorcs.com ${n: n \in \mathbb{Z} \text{ and } n^2 < 5} = {-2, -1, 0, 1, 2}$

### WeChat: cstutorcs and $|n| \le 2$

#### Examples

### Ssignment Project Exam Help

#### Show:

- Interest in the second of t

#### That is, show:

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### Laws of Set Operations

### Associativity Associativity $Project \cup Exam Help$ Associativity $Project \cup Exam Help$ $A \cap B = B \cap A$

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 $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$ 

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 $A \cap (A^c) = \emptyset$ 

#### Substitution

Assignment Project Exam Help expressions for each set symbol.

```
Example to S. //tutores.com
```

Therefore:  $(C \cap D) \cup (D \oplus E) = (D \oplus E) \cup (C \cap D)$ We Chat: CSUITORCS

#### Example

### Assignment Project Exam Help

$$A \cap (B \cap C) = (A \cap B) \cap C$$
 [Associativity]  
 $https://tuto(A \cap B) \cap C$  [Commutativity]

### (Aim to) limit each step to a non-overlapping applications of a

(Aim to) limit each step to a non-overlapping applications of a single rule

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Laws of Set Operations

Derivation Derivation

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#### Other useful set laws

# Assigning calleriable where Exam Help Idempotence $A \cap A = A$ $A \cup A = A$ Double complementation $C_{A}^{c}C_{$

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```
http = A \cup \emptyset  (Identity)
= A \cup (A \cap A^c)  (Complementation)
http = (A \cup A)  (Complementation)
= (A \cup A)  (Identity)
= (A \cup A)  (Identity)
```

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#### Two useful results

#### **Definition**

If A is a set defined using A, A and A, then A is the Selection A is the Selection A and A (and A are lading) with A (and vice-versa).

### The prove $A_1 = A_2$ using the Laws of Set Operations then

If you can prove  $A_1 = A_2$  using the Laws of Set Operations then you can prove  $dual(A_1) = dual(A_2)$ 

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Absorption law:  $A \cup (A \cap B) = A$ 

Dual:  $A \cap (A \cup B) = A$ 

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```
\begin{array}{ll} A &= A \cup \emptyset & \text{(Identity)} \\ \textbf{https:}(A) & \text{(Complementation)} \\ &= (A \cup A) \cap \mathcal{U} & \text{(Complementation)} \\ &= (A \cup A) & \text{(Identity)} \\ \textbf{WeChat: cstutorcs} \end{array}
```

### Assignment Project Exam Help

```
\begin{array}{ll} A &= A \cap \mathcal{U} & \text{(Identity)} \\ \textbf{https:} (A \cap A) \cup (A \cap A) \cup (Complementation) \\ &= (A \cap A) \cup \emptyset & \text{(Complementation)} \\ &= (A \cap A) & \text{(Identity)} \\ \textbf{WeChat: cstutorcs} \end{array}
```

#### Two useful results

#### Theorem (Uniqueness of complement)

 $A \cap B = \emptyset$  and  $A \cup B = \mathcal{U}$  if, and only if,  $B = A^c$ .

### Assignment Project Exam Help

$$\begin{array}{ll} B &= B \cap \mathcal{U} & \text{(Identity)} \\ \textbf{https://AutoAcs.complement)} \\ &= B \cap (A \cup A^c) & \text{(Complement)} \\ &= (A \cap B) \cup (A^c \cap B) & \text{(Commutativity)} \\ &= \emptyset \cup (A^c \cap B) & \text{(Given)} \\ \textbf{Wetalack} \cup (A^c \cap B) & \text{(Distributivity)} \\ &= A^c \cap (A \cup B) & \text{(Distributivity)} \\ &= A^c \cap \mathcal{U} & \text{(Given)} \\ &= A^c & \text{(Identity)} \end{array}$$

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```
 \begin{array}{ll} X^c \cap X &= X \cap X^c & \text{(Commutativity)} \\ \textbf{https://tutorcs.com}^{\text{(Identity)}} \\ X^c \cup X &= \mathcal{U} & \text{(Principle of duality)} \end{array}
```

By the uniqueness of complement,  $(X^c)^c = X$ . CSTUTOTCS

#### Exercises

#### **Exercises**

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- $\bullet \ (C \cup A) \cap (B \cup A) = A \cup (B \cap C)$
- (A \cap B) \cup (A \cup B^c)^c = B https://tutorcs.com

#### **Exercises**

Give counterexamples to show the following do not hold for all

 $\overset{\text{sets:}}{\underset{\bullet}{\mathsf{N}}} \underbrace{WeChat:}_{\mathcal{B} \setminus \mathcal{C}} \underbrace{cstutorcs}$ 

- $(A \cup B) \setminus C = A \cup (B \setminus C)$
- $(A \setminus B) \cup B = A$

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