

Assignment Project Exam Help

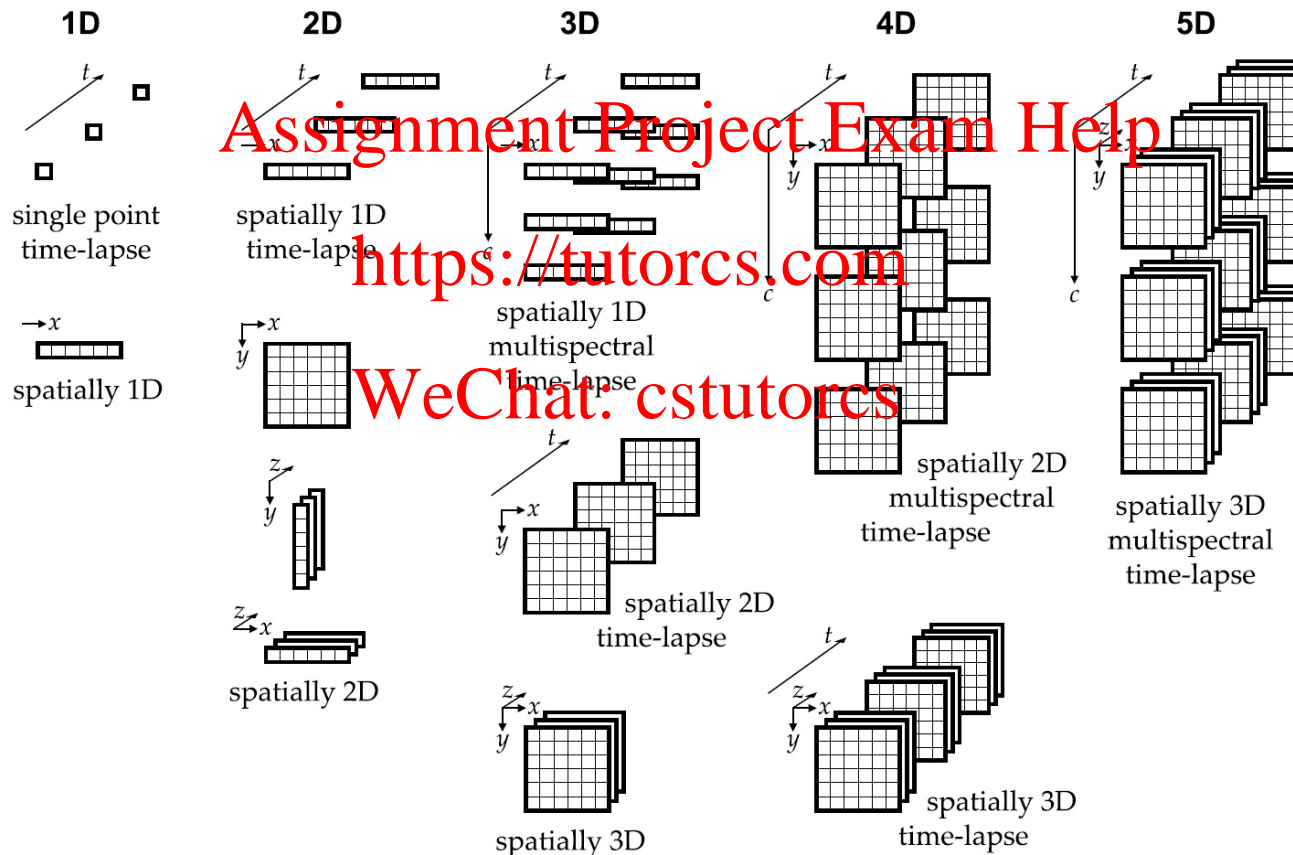
COMP9517: Computer Vision

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Motion

Introduction

- Adding the time dimension to the image formation



Introduction

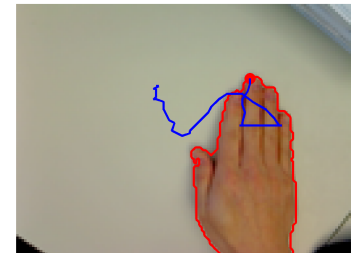
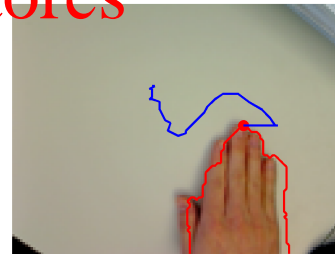
- A changing scene may be observed and analysed via a sequence of images

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Introduction

- Changes in an image sequence provide features for
 - Detecting objects that are moving
 - Computing trajectories of moving objects
 - Performing motion analysis of moving objects
 - Recognising objects based on their behaviours
 - Computing the motion of the viewer in the world
 - Detecting and recognising activities in a scene

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Applications

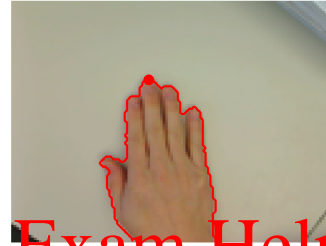
- **Motion-based recognition**
 - Human identification based on gait, automatic object detection
- **Automated surveillance**
 - Monitoring a scene to detect suspicious activities or unlikely events
- **Video indexing**
 - Automatic annotation and retrieval of videos in multimedia databases
- **Human-computer interaction**
 - Gesture recognition, eye gaze tracking for data input to computers
- **Traffic monitoring**
 - Real-time gathering of traffic statistics to direct traffic flow
- **Vehicle navigation**
 - Video-based path planning and obstacle avoidance capabilities

Scenarios

- Still camera

Constant background with

- Single moving object
- Multiple moving objects



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- Moving camera

Relatively constant scene with

- Coherent scene motion
- Single moving object
- Multiple moving objects



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Topics

- **Change detection**

Using *image subtraction* to detect changes in scenes

- **Sparse motion estimation**

Using *template matching* to estimate local displacements

- **Dense motion estimation**

Using *optical flow* to compute a dense motion vector field

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Change Detection

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Change Detection

- Detecting an object moving across a constant background
- The forward and rear edges of the object advance only a few pixels per frame



- By subtracting the image I_t from the previous image I_{t-1} the edges should be evident as the only pixels significantly different from zero

Image Subtraction

Step: Derive a background image from a set of video frames at the beginning of the video sequence



**Performance
Evaluation of
Tracking and
Surveillance
(PETS) 2009
Benchmark**

Image Subtraction

Step: Subtract the background image from each subsequent frame to create a difference image

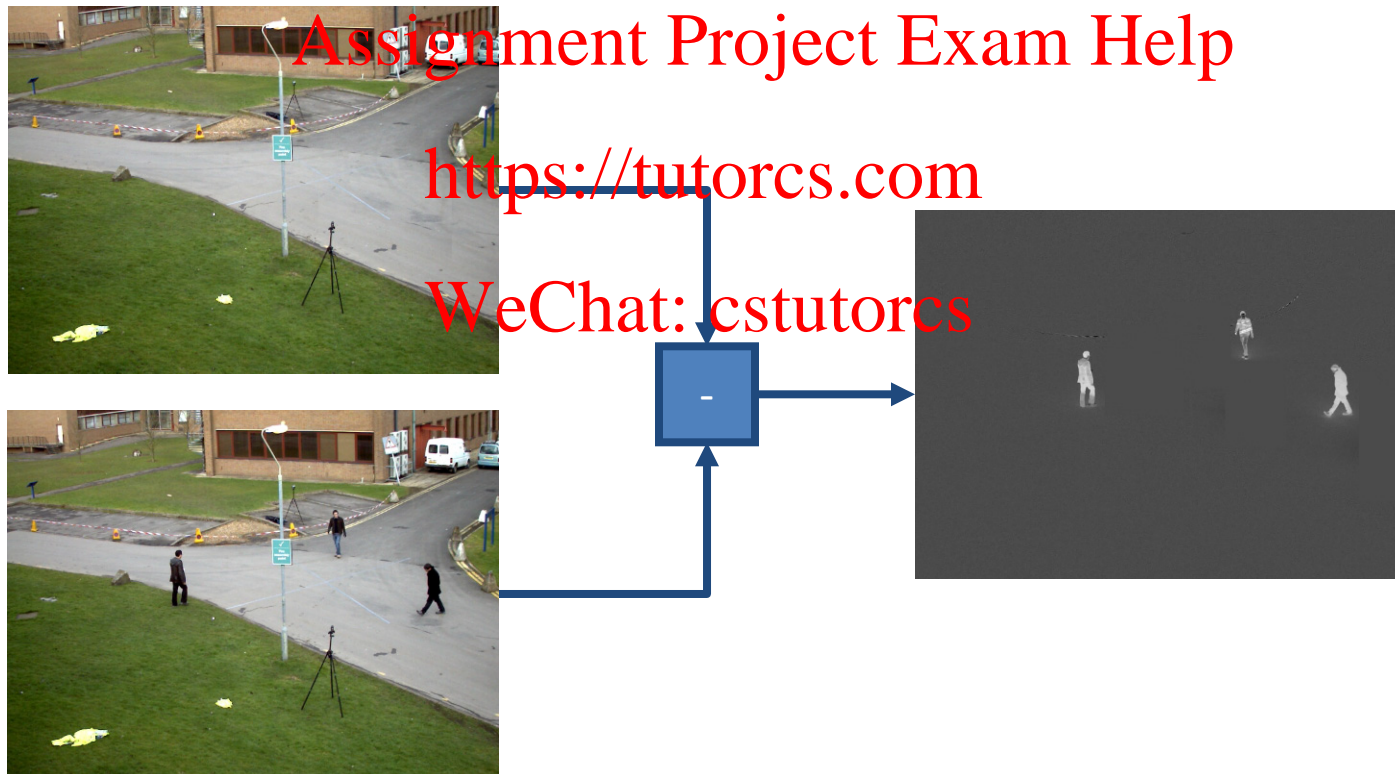


Image Subtraction

Step: Threshold and enhance the difference image to fuse neighbouring regions and remove noise

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Image Subtraction

Detected bounding boxes overlaid on input frame



Change Detection

- Image subtraction algorithm

- Input: images I_t and $I_{t-\Delta t}$ (or a model image)
- Input: an intensity threshold τ
- Output: a binary image I_{out}
- Output: a set of bounding boxes B

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1. For all pixels $[r, c]$ in the input images,
set $I_{out}[r, c] = 1$ if $(|I_t[r, c] - I_{t-\Delta t}[r, c]| > \tau)$
set $I_{out}[r, c] = 0$ otherwise
2. Perform connected components extraction on I_{out}
3. Remove small regions in I_{out} assuming they are noise
4. Perform a closing of I_{out} using a small disk to fuse neighbouring regions
5. Compute the bounding boxes of all remaining regions of changed pixels
6. Return $I_{out}[r, c]$ and the bounding boxes B of regions of changed pixels

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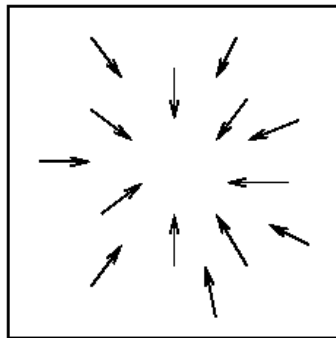
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Sparse Motion Estimation

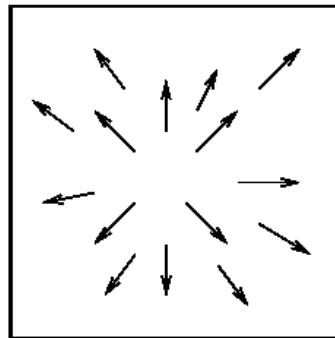
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Motion Vector

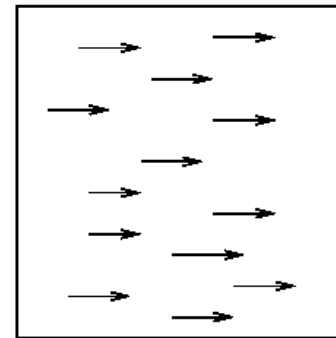
- A motion field is a 2D array of 2D vectors representing the motion of 3D scene points
- A motion vector in the image represents the displacement of the image of a moving 3D point
 - Tail at time t and head at time $t + \Delta t$
 - Instantaneous velocity estimate at time t



Zoom out



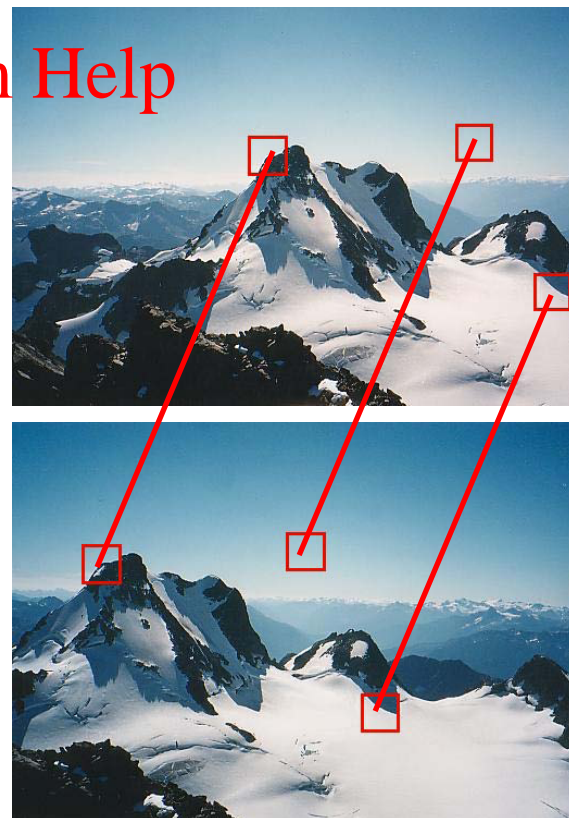
Zoom in



Pan Left

Sparse Motion Estimation

- A sparse motion field can be computed by identifying pairs of points that correspond in two images taken at times t and $t+\Delta t$
- Assumption: intensities of interesting points and their neighbours remain nearly constant over time
- Two steps:
 - Detect interesting points at t
 - Search corresponding points at $t+\Delta t$



Sparse Motion Estimation

- Detect interesting points
 - Image filters
 - Canny edge detector
 - Hessian ridge detector
 - Harris corner detector
 - SIFT features
 - ...
 - Interest operator
 - Computes intensity variance in the vertical, horizontal and diagonal directions
 - Interest point if the minimum of these four variances exceeds a threshold

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Detect Interesting Points

```
Procedure detect_interesting_points(I,V,w,t) {
```

```
    for (r = 0 to MaxRow - 1)
```

```
        for (c = 0 to MaxCol - 1)
```

```
            if (I[r,c] is a border pixel) break;
```

```
            else if (interest_operator(I,r,c,w) >= t)
```

```
                add (r,c) to set V;
```

```
}
```

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```
Procedure interest_operator (I,r,c,w) {
```

```
    v1 = variance of intensity of horizontal pixels I[r,c-w]...I[r,c+w];
```

```
    v2 = variance of intensity of vertical pixels I[r-w,c]...I[r+w,c];
```

```
    v3 = variance of intensity of diagonal pixels I[r-w,c-w]...I[r+w,c+w];
```

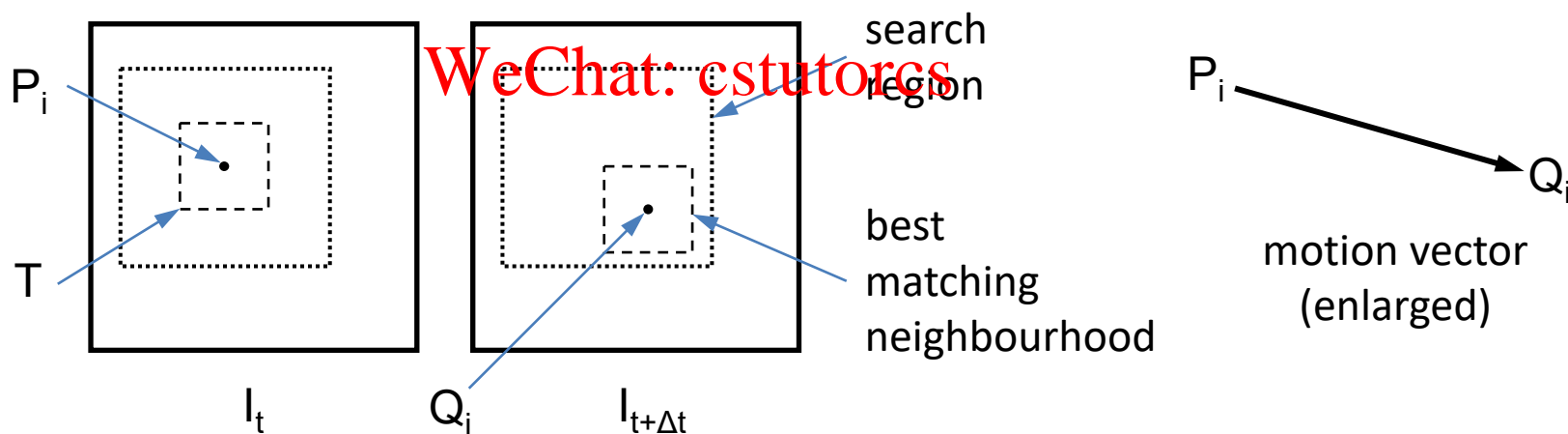
```
    v4 = variance of intensity of diagonal pixels I[r-w,c+w]...I[r+w,c-w];
```

```
    return min(v1, v2, v3, v4);
```

```
}
```

Sparse Motion Estimation

- Search corresponding points
 - Given an interesting point P_i from I_t , take its neighbourhood in I_t and find the best matching neighbourhood in $I_{t+\Delta t}$ under the assumption that the amount of movement is limited



This approach is also known as template matching

Similarity Measures

- Cross-correlation (to be maximised)

$$CC(\Delta x, \Delta y) = \sum_{(x,y) \in T} I_t(x, y) \cdot I_{t+\Delta t}(x + \Delta x, y + \Delta y)$$

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- Sum of absolute differences (to be minimised)

$$SAD(\Delta x, \Delta y) = \sum_{(x,y) \in T} |I_t(x, y) - I_{t+\Delta t}(x + \Delta x, y + \Delta y)|$$

- Sum of squared differences (to be minimised)

$$SSD(\Delta x, \Delta y) = \sum_{(x,y) \in T} [I_t(x, y) - I_{t+\Delta t}(x + \Delta x, y + \Delta y)]^2$$

Similarity Measures

- Mutual information (to be maximised)

$$MI(A, B) = \sum_a \sum_b P_{AB}(a, b) \log_2 \left(\frac{P_{AB}(a, b)}{P_A(a) P_B(b)} \right)$$

Subimages to compare:

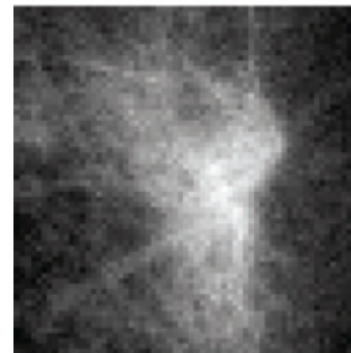
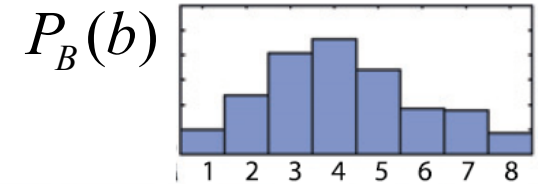
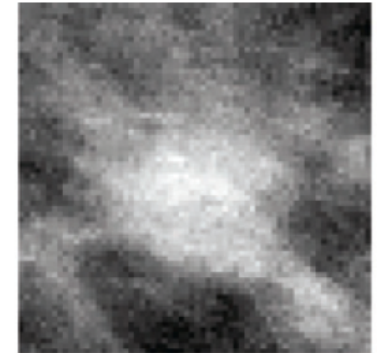
$$A \subset I_t \quad B \subset I_{t+\Delta t}$$

Intensity probabilities:

$$P_A(a) \quad P_B(b)$$

Joint intensity probability:

$$P_{AB}(a, b)$$



A

$P_A(a)$

$P_{AB}(a, b)$

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Dense Motion Estimation

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Dense Motion Estimation

- Assumptions:
 - The object reflectivity and illumination do not change during the considered time interval
 - The distance of the object to the camera and the light sources does not vary significantly over this interval
 - Each small neighbourhood $N_t(x,y)$ at time t is observed in some shifted position $N_{t+\Delta t}(x+\Delta x, y+\Delta y)$ at time $t+\Delta t$
- These assumptions may not hold tight in reality, but provide useful computation and approximation

Spatiotemporal Gradient

- Taylor series expansion of a function

$$f(x + \Delta x) = f(x) + \frac{\partial f}{\partial x} \Delta x + \text{h.o.t} \Rightarrow$$

$$f(x + \Delta x) \approx f(x) + \frac{\partial f}{\partial x} \Delta x$$

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- Multivariable Taylor series approximation

$$f(x + \Delta x, y + \Delta y, t + \Delta t) \approx f(x, y, t) + \frac{\partial f}{\partial x} \Delta x + \frac{\partial f}{\partial y} \Delta y + \frac{\partial f}{\partial t} \Delta t \quad (1)$$

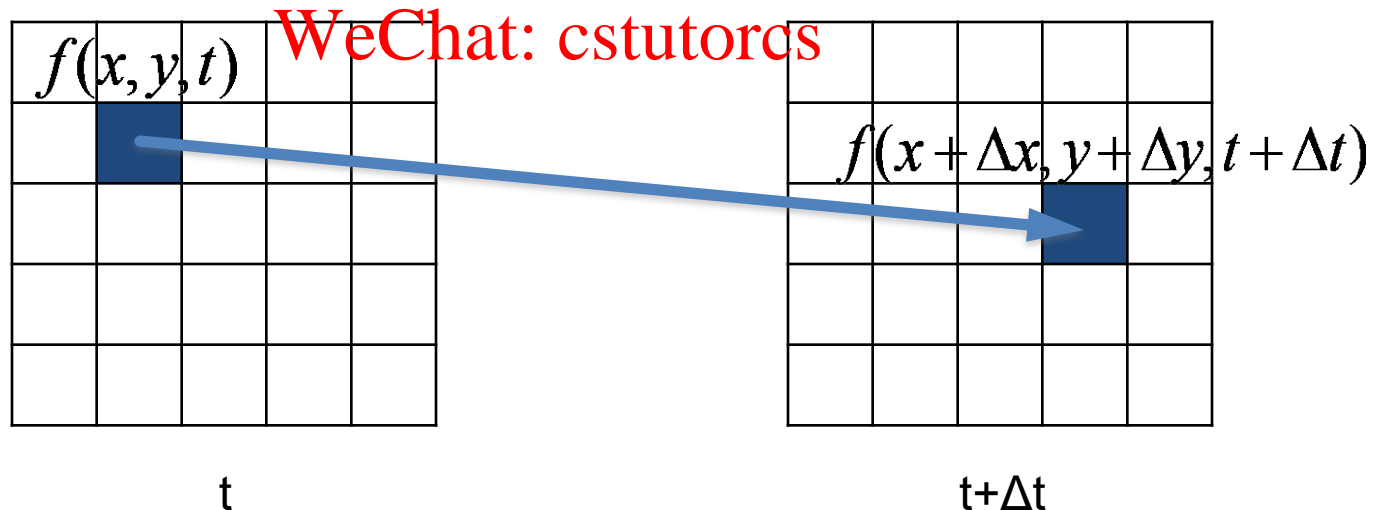
Optical Flow Equation

Assuming neighbourhood $N_t(x, y)$ at time t moves over vector $V=(\Delta x, \Delta y)$ to an identical neighbourhood $N_{t+\Delta t}(x+\Delta x, y+\Delta y)$ at time $t+\Delta t$ leads to the optical flow equation:

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$$f(x + \Delta x, y + \Delta y, t + \Delta t) = f(x, y, t) \quad (2)$$

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Optical Flow Computation

Combining (1) and (2) yields the following constraint:

$$\frac{\partial f}{\partial x} \Delta x + \frac{\partial f}{\partial y} \Delta y + \frac{\partial f}{\partial t} \Delta t = 0 \Rightarrow$$

$$\frac{\partial f}{\partial x} \frac{\Delta x}{\Delta t} + \frac{\partial f}{\partial y} \frac{\Delta y}{\Delta t} + \frac{\partial f}{\partial t} \frac{\Delta t}{\Delta t} = 0 \Rightarrow$$

$$\frac{\partial f}{\partial x} v_x + \frac{\partial f}{\partial y} v_y + \frac{\partial f}{\partial t} = 0 \Rightarrow$$

$$\nabla f \cdot v = -f_t$$

where $v = (v_x, v_y)$ is the velocity or *optical flow* of $f(x, y, t)$
and $\nabla f = (f_x, f_y) = (\partial f / \partial x, \partial f / \partial y)$ is the gradient

Optical Flow Computation

- The optical flow equation provides a constraint that can be applied at every pixel position
- However, the equation does not have a unique solution and thus further constraints are required

For example, by using the optical flow equation for a group of adjacent pixels and assuming that all of them have the same velocity, the optical flow computation task amounts to solving a linear system of equations using the least-squares method

Many other solutions have been proposed (see references)

Optical Flow Computation

- Example: Lucas-Kanade approach to optical flow

Assume the optical flow equation holds for all pixels p_i in a certain neighbourhood and use the following notation:

$$\mathbf{v} = (v_x, v_y) \quad f_x = \frac{\partial f}{\partial x} \quad f_y = \frac{\partial f}{\partial y} \quad f_t = \frac{\partial f}{\partial t}$$

Then we have the following set of equations:

$$\begin{array}{rcl} f_x(p_1)v_x + f_y(p_1)v_y & = & -f_t(p_1) \\ f_x(p_2)v_x + f_y(p_2)v_y & = & -f_t(p_2) \\ \vdots & & \vdots \\ f_x(p_N)v_x + f_y(p_N)v_y & = & -f_t(p_N) \end{array}$$

Optical Flow Computation

- Example: Lucas-Kanade approach to optical flow

The set of equations can be rewritten as $Av = b$ where

$$A = \begin{bmatrix} f_x(p_1) & f_y(p_1) \\ f_x(p_2) & f_y(p_2) \\ \vdots & \vdots \\ f_x(p_N) & f_y(p_N) \end{bmatrix} \quad v = \begin{bmatrix} v_x \\ v_y \end{bmatrix} \quad b = \begin{bmatrix} -f_t(p_1) \\ -f_t(p_2) \\ \vdots \\ -f_t(p_N) \end{bmatrix}$$

This can be solved using the least-squares approach:

$$A^T A v = A^T b \quad \Rightarrow \quad v = (A^T A)^{-1} A^T b$$

Optical Flow Example



<https://www.youtube.com/watch?v=GIUDAZLfYhY>

References and Acknowledgements

- Chapter 8 of Szeliski 2010
- Chapter 9 of Shapiro and Stockman 2001
- Images drawn from the above references

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