${\rm CpSc~418}$

Due: February 7, 2023, 11:59pm Early-Bird: February 5, 2023, 11:59pm

105 points

Prelude

Please submit your solution using:

handin cs-418 hw2 Your solution should contain three files:

hw2.erl: Erlang source code for your solutions to the questions.

hw2_tests.erl: <u>EUnit</u> tests for the functions you were asked to write. In addition to the template that I will post, you can use hw1_tests.erl as an example.

hw2.pdf: Your solutions to written questions.

Templates for hw2_tests.erl.are available at http://www.serl.and.hw2_tests.erl.are available at http://www.serl.and.hw2_tests.erl.and.

The Questions WeChat: cstutorcs

- 1. π reduce (25 points): Recall the method of estimating π by choosing a positive integer, N, and finding the probability, P(N), that two integers, A and B are co-prime. We then note $\lim_{N\to\infty} P(N) = 6/\pi^2$ and use this to compute π . For this problem, you may use the functions for trees of workers provided in <u>wtree</u> or from <u>red.erl</u>. I'll describe the questions using the <u>wtree</u> functions, but either approach is acceptable.
 - (a) (15 points): Write a parallel implementation of the deterministic method for estimating π (see <u>HW1</u> Q1.a&b). Write a function p(W, N) where W is a worker-tree returned by <u>wtree:create</u>, i.e. <u>wtree:create(23)</u> returns a binary tree of 23 worker processes. p(W, N) should return the number of pairs of integers $1 \le A, B \le N$ such that A and B are co-prime.
 - (b) (10 points): Measure the speed-up for your parallel implementation. Run your timing measurements on thetis.students.cs.ubc.ca and use $\underline{\text{time_it:t/1}}$. Thetis has 64 cores (more technically, it has 32 hardware cores, each of which is $\overline{2}$ -way multithreaded). Speed-up is T_{seq}/T_{par} where T_{seq} is the sequential running time (e.g. your solution from HW1), and T_{par} is the parallel run-time. Try experiments using 4, 16, 32, 64, 128, and 256 processes and values of N from 1000 increasing by multiples of 10 until you reach a value (for the number of processes) where the execution takes between 1 and 10 seconds. What number of processes and value for N gives you the highest speed-up?
 - (c) **Just for fun:** Implement a parallel version of the randomized version from <u>HW1</u> Q1.c and measure the speed-up.

2. Reduce – by the book (25 points): As noted in class, the course-library implementations of reduce and scan start with a master process broadcasting a request from the root of the process tree down to the leaves, the leaves do the work, and the results are combined back to the root and the grand total is sent to the master. When performing a scan, the course library adds a final top-down pass to generate the cumulative sums (or whatever operator was used) at the leaves. In the book, reduce and scan are both start with a bottom-up pass that is initiated by the leaf processes, followed by a top-down pass the distributes the results. Scan uses the same bottom-up pass as reduce, but the final top-down pass is different for scan and reduce, both by the books method and the course library.

For this question, implement

```
reduce_bu(ProcState, LeafVal, Combine) -> % Total
  % ProcState: the process state for this worker.
 % LeafVal: the value at the leaf of the reduce tree computed by this worker.
  % Combine: the associative function for combining values.
```

to work with worker trees as constructed by <u>red.erl</u>:create/1. The function reducc_bu/3 is called by each leaf of the worker tree to compute the parallel reduce. Note: ProcState is needed by reduce bu

because it includes entries for:

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parent: The pid of the parent node for this process, or the atom none if this is the root node.

children_bu: A list of pids of the children of this tree, in bottom-up order. To describe this list, I'll assume that that P, the number of worker processes in the tree is a power of 2. If the index of a worker node is in the country to $f + 2^K O$ where either O in ode, or J = 0 and $K = log_2 P$. Node I has K children in the first associate with children out these are the workers with indices $I + 2^M$ for each $M \in \{0, 1, \dots, K-1\}$. The list is in order of increasing worker index. For example, if P = 16, then $worker_0$ has the list of children:

```
[worker1, www.ere worken1awerkerestutores] and worker12 has the list of children
```

```
[worker<sub>13</sub>, worker<sub>14</sub>]
```

If P is not a power of two, we construct a binary tree where the left subtree has ceil(P / 2) leaves, and the right subtree has floor (P / 2) leaves, and likewise for the subtrees. If a (sub)tree spans workers W_I through W_J, then worker W_I is the root of the (sub)tree and its left subtree. There are M = J + 1 - I leaves to this tree, and worker $W_{I} = \{I + (M \text{ div } 2)\}$ is the root of the right subtree.

Hint: Here's a sketch of reduce_bu:

- Fetch the list of child pids and the parent pid from ProcState.
- Call a recursive helper function that walks down the list of child pids, receiving value from each, and combining them. Make sure that you keep the left-right order of arguments correct. I'll test your reduce bu with a Combine function that is associative but not commutative.
- When you reach the end of the list, send your result to your parent (if you have one).
 - If your parent is **none**, then propagate the result back down the tree.

Each worker process calls reduce bu when its LeafVal is ready. The values are Combine's up the tree, and the final total propagated down the tree to each worker process.

3. Scan – by the book (20 points): For this question, implement

```
scan_bu(ProcState, AccIn, LeafVal, Combine) -> % AccLeft

% Parameters:
    % ProcState: the process state for this worker.
    % AccIn: the initial value for the accumulator (used at the root of the tree).
    % LeafVal: the value at the leaf of the reduce tree computed by this worker.
    % Combine(Left, Right): the associative function for combining values.

% Result:
    % AccLeft: % the result of combining everything to the left of this node using Combine.
    % If this is the leftmost node, then AccLeft =:= AccIn.
```

Each worker process calls scan_bu when its LeafVal is ready. The values are Combine'd up the tree. When the Combine operation reaches the root of the tree, you need to propagate values back down the tree. This is where the code for scan differs from that for reduce. Many of the ideas from your solution to reduce should carry over to scan.

- - (a) (20 points): Write a parallel implementation: brownie_par(W, N, Alpha) -> GreatestDistance. Use the functions from the wtree module in the class library. Hint: my solution uses:

```
wtree:nworkers(W): - find out how many leaf processes there are to know how much work to give to each worker.
```

wtree:update(...): - each worker computes its sequence of steps.

wtree:scan(...): - Each worker computes a list of the locations reached after performing each
 of its steps. Note: the "walk" by worker I (for I > 0) starts from the end point of the walk
 by worker I-1.

wtree:reduce(...): - find the maximum distance from the origin.

- (b) **Optional/extra-credit**: This problem has been rendered unreasonable for students (but just fine for the instructor) because new release of Erlang is a memory hog and student accounts have small per-process memory limits. There will be 5 (or maybe a bit more) points of extra-credit for reporting any reasonable results.
 - Compute the speed-up for various numbers of worker processes and various choices of \mathbb{N} . You can fix $\mathtt{Alpha} = 1.0$. Follow the guidelines for measuring speed-up that were given in Q1.
- (c) Just for fun: the estimate of max-distance has a *large* variance. I'm observing a variance of about 1/3 the mean. Don't let this stress you out. If you want more consistent results, try computing the average from 100 to 1000 runs. Note that this provides another opportunity for parallelism.
- 5. **Speed-up** (15 points): Consider using reduce on a problem of size N using P processors. For simplicity, assume that P is a power of two thus, the reduce tree is a complete binary tree. Each leaf worker takes

time $(N/P)*T_{leaf}$ time to compute it's local result. The time to send a message between processes is λ , and the time to combine the results of two sub-trees (not including the communication time) is $T_{combine}$.

- (a) (easy, 3 points) What is the total time to compute the reduce?
- (b) (easy, 2 points) What is the total time to compute the same result sequentially? Remember: no communication costs.
- (c) (5 points) If $T_{combine} = T_{leaf}$, how big does N need to be to get a speed-up of P/2? Assume that $\lambda \gg T_{leaf}$ (had been $\lambda \gg 1$ but T_{leaf} is what matters) and simplify accordingly. Your solution should make it clear where you use this assumption.
 - Note: several students have noted that you can derive an exact formula for N without making a the simplifying approximation that comes by assuming that λ is large. Indeed, you can. The exact formula has a sum in it. If you assume λ is large, then you can eliminate one term from the sum to get a formula where it's obvious how N depends on P and λ . In other words, if you're working on a project in real-life and asked "If we increase the number of processors by $10 \times$, can we make this go at least 1.8 times faster?" you can quickly estimate it. Often, system design needs an ability to quickly eliminate unworkable solutions without having to do detailed calculations first. That's why simplifying to the asymptotic form is really good for getting intuition about the

tra A-offs ignment Project Exam Help (d) (5 points) If $\mathcal{H}_{eaf} = \lambda$, how big does N need to be to get a speed-up of P/2?

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