Study Guide

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Module 05 terminology

- **Auxiliary parameter:** In a recursive function, a parameter that "goes along for the ride", passed unchanged along a chain of recursive calls
- **Base case:** In a recursive function, a path through the function that terminates without requiring any more recursion
- **Box-and-pointer visualization:** A list visualization in which list items are arranged in a linked chain
- **Condensed trace:** Highlights from the trace of a function application, showing only the recursive calls and any final non-recursive steps
- **Data analysis:** A preliminary step in the Design Recipe where new types are defined based on the problem domain, and data definitions and templates are created for them
- **Data definition:** A comment that defines a new type name and describes the complete structure of values of that type
- **Data-directed design:** The principle that the form of a function should mirror the form of the data it processes
- **Filtering a list:** A list processing idiom where a sub-list is extracted from a list, consisting of all items that have a certain property
- **Folding a list:** A list processing idiom where a list is reduced down to a single value by repeatedly combining elements with a base value
- **Homogeneous list:** A list whose elements are all of a given type
- **Idiom:** In programming, a pattern or style of code that is useful in a wide range of contexts
- **Mapping a list:** A list processing idiom where every item of a list is transformed in a consistent way to produce a new list
- **Nested visualization:** A list visualization in which successive list items are shown nested within the items that refer to them
- **Recursion:** The property of a function that's defined in terms of itself. See also ***Recursion***
- **Self-reference:** A case in a data definition where a value is built from another value of the type currently being defined
- **Structural recursion:** A style of recursion in which recursive calls exactly follow the self-references in a data definition
- **Wrapper function:** A simple, non-recursive function that initiates a large computation, often preparing data for recursive processing and polishing up the result

Module 05 types

- `(anyof` t_1 `...` t_n v_1 `...` v_m`)`
- `Char`
- `cons cell`
- `empty list`
- `(listof` τ`)`

Module 05 functions, constants, and syntax

- `cons`
- `cons?`
- `empty`
- `empty?`
- `first`
- `list->string`
- `list?`
- `member?`
- `rest`
- `string->list`

Extra Practice Problems

Here are a few additional programming problems that you can use for practice with lists. They are not worth any marks, but they might help you hone your skills if you need it. No automated tests are provided for these problems. You are welcome to get help with them during office hours.

1. Write a function `before-tea` that consumes a list of symbols and produces the list of symbols that occur before the first occurrence of the symbol `'tea`.
2. Write a function `after-tea` that consumes a list of symbols and produces the list of symbols that occur after the first occurrence of the symbol `'tea`.
3. Write a function `after-tea` that consumes a list of symbols and produces the list of symbols that occur after the *last* occurrence of the symbol `'tea`.
4. Write a function `sixy` that consumes a list of integers and produces a sub-list consisting of those integers that are divisible by 6.
5. Write a function `total-string-length` that consumes a list of strings and produces the total number of characters in all the strings in the list.
6. Write a function `initials` that consumes a list of strings and produces a single string formed from the first character of each string in the list. For example, `(initials (cons "Computer" (cons "Science" empty)))` produces `"CS"`.
7. Write a function `how-true` that consumes a list of Booleans and produces the difference between the number of `true` values and the number of `false` values in the list.
8. Write a function `how-true` that consumes a list of *any* values and produces the difference between the number of `true` values and the number of `false` values in the list, ignoring any values that are not Booleans.
9. Write a function `collatz-list` that consumes a list of integers and produces the next Collatz number for each integer. That is, if the integer is even, divide by 2; if the integer is odd and larger than one, multiply the number by three and add 1; if the integer is one, it remains as one. For example, `(collatz-list (cons 5 (cons 10 (cons 2 (cons 1 (cons 9 empty))))))` produces `(cons 16 (cons 5 (cons 1 (cons 1 (cons 28 empty)))))`.
10. Write a function `pair-sum` that consumes a list of numbers of length at least two, and computes the list which is the sum of each pair of consecutive numbers. For example, `(pair-sum (cons 1 (cons 2 (cons 3 (cons -4 (cons 5 empty))))))` should produce `(cons 3 (cons 5 (cons -1 (cons 1 empty))))`.
11. Write a function `replace-all` that consumes a list `lst` and two values a and b. The function produces a new list that's identical to `lst`, except that every occurrence of a has been replaced by b. For example, `(replace-all (cons 'fish (cons 'dog (cons 'apple (cons 'dog (cons true empty))))) 'dog "pancakes")` would produce `(cons 'fish (cons "pancakes" (cons 'apple (cons "pancakes" (cons true empty)))))`.
12. Write a function `eval-poly` to evaluate a polynomial. A polynomial can be represented as a list of coefficients, from smallest power to largest. The function should consume such a list together with a number x at which to evaluate. For example, `(eval-poly (cons 2 (cons 0 (cons 1 (cons 3 empty)))) 5)` should produce the number $2 + 0 \cdot 5 + 1 \cdot 5^2 + 3 \cdot 5^3$.
13. Write a function `get-divisible` that consumes a list of natural numbers `lon` together with a natural number n. The function produces a new list containing all those elements of `lon` that are divisible by n.
14. Using the function defined in the previous question, write a function `divisible23` that consumes a list of natural numbers `lon` and produces a new list containing all those elements of `lon` that are divisible by both 2 and 3.
15. Write a function `swap-pairs` that consumes a list of even length. The function produces a new list in which consecutive pairs of values been swapped (positions 0 and 1, 2 and 3, 4 and 5, and so on). For example, `(swap-pairs (cons 1 (cons "hello" (cons 'apple (cons true empty)))))` produces `(cons "hello" (cons 1 (cons true (cons 'apple empty))))`.
16. Write a function `count-char` that consumes a string `str` and a character `ch` and computes how many times `ch` occurs in `str`.
17. Write a function `remove-char` that consumes a string `str` and a character `ch` and produces a new string in which every copy of `ch` has been removed. For example, `(remove-char "Now is the winter of our discontent" #\o)` produces `"Nw is the winter f ur discntent"`.
18. Write a function `remove-chars` that consumes a string `str` and a second string `rm`, and produces a new string in which *all* of the characters in `rm` are removed from `str`. For example, `(remove-chars "Now is the winter of our discontent" "aeiou")` produces `"Nw s th wntr f r dscntnt"`. Use the function from the previous question as a helper.
19. Write a function `replace-char` that consumes a string `str` together with two characters a and b. It produces a new string in which every occurrence of a has been replaced by b. For example, `(replace-char "computer science" #\c #\q)` produces `"qomputer sqienqe"`. An earlier function in this list may be useful as a helper.
20. Write a predicate `has-char?` that consumes a string `str` and a character `ch` and determines whether `str` contains any occurrences of `ch`. Do not always perform recursion all the way to the end of `str`: if you discover an occurrence of `ch`, stop immediately and produce `true`.
21. Write a function `tser` that consumes a non-empty list and produces a new list that has all the same elements as the original, except for the last one. For example, `(tser (cons 2 (cons 8 (cons -3 empty))))` produces `(cons 2 (cons 8 empty))`.
22. Write a predicate `non-decreasing?` that consumes a list of numbers and determines whether the numbers in the list are in non-decreasing order (i.e., each number in the list is greater than or equal to the one before it). Experiment with modifying your function to produce the related predicates `strictly-increasing?`, `non-increasing?`, and `strictly-decreasing?`.
23. In a certain sports league, a team gets two season points for a win, one point for a tie, and zero points for a loss. Write a function `standing` that consumes a list of symbols, each one of `'win`, `'tie`, or `'loss`, and calculates the total number of points the team has earned for the season. For example, `(standing (cons 'win (cons 'loss (cons 'loss (cons 'tie)))))` produces 3.
24. Using recursion on lists of characters, write `string->nat`, which behaves like `string->number` but only works on natural numbers. For example, `(string->nat "5238")` produces 5238. This one is a bit challenging!