Q1. Searching with Heuristics

Consider the A* searching process on the connected undirected graph, with starting node S and the goal node G. Suppose the cost for each connection edge is **always positive**. We define $h^*(X)$ as the shortest (optimal) distance to G from a node X.

Answer Questions (a), (b) and (c). You may want to solve Questions (a) and (b) at the same time.

(a) Suppose h is an admissible heuristic, and we conduct A* tre C be the cost of the found path (directed by h', defined in part	· · · · · · · · · · · · · · · · · · ·
(i) Choose one best answer for each condition below.	(,,
1. If $h'(X) = \frac{1}{2}h(X)$ for all Node X , then	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
2. If $h'(X) = \frac{h(X) + h^*(X)}{2}$ for all Node X, then	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
3. If $h'(X) = h(X) + h^*(X)$ for all Node X, then	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
	hbor nodes Y satisfying $h^*(X) > h^*(Y)$, and the following
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then,	$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$
5. If K is the same as above, we have $h'(X) = \begin{cases} \min_{Y \in K(X)} h(X) \\ h(X) \end{cases}$	S.COM $Y + cost(X, Y)$ if $K(X) \neq \emptyset$ if $K(X) = \emptyset$
	X and X and
6. If $h'(X) = \min_{Y \in K(X) + \{X\}} h(Y)$ (K is the same as a	above), \bigcirc $C = h^*(S)$ \bigcirc $C > h^*(S)$ \bigcirc $C \ge h^*(S)$
(ii) In which of the conditions above, h' is still admissible are we say h , dominates h_2 when $h_1(X) > h_2(X)$ holds for	nd for sure to dominate h? Check all that apply. Remember

- (b) Suppose h is a **consistent** heuristic, and we conduct A^* graph search using heuristic h' and finally find a solution.
 - (i) Answer exactly the same questions for each conditions in Question (a)(i).

1.
$$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$$

2.
$$\bigcirc$$
 $C = h^*(S)$ \bigcirc $C > h^*(S)$ \bigcirc $C \ge h^*(S)$

3.
$$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$$

4.
$$\bigcirc$$
 $C = h^*(S)$ \bigcirc $C > h^*(S)$ \bigcirc $C \ge h^*(S)$

5.
$$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$$

6.
$$\bigcirc C = h^*(S) \bigcirc C > h^*(S) \bigcirc C \ge h^*(S)$$

(ii) In which of the conditions above, h' is still **consistent** and for sure to dominate h? Check all that apply.

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(c) Suppose h is an **admissible** heuristic, and we conduct A* **tree search** using heuristic h' and finally find a solution. If $\epsilon > 0$, and X_0 is a node in the graph, and h' is a heuristic such that

$$h'(X) = \begin{cases} h(X) & \text{if } X = X_0 \\ h(X) + \epsilon & \text{otherwise} \end{cases}$$

- Alice claims h' can be inadmissible, and hence $C = h^*(S)$ does not always hold.
- Bob instead thinks the node expansion order directed by h' is the same as the heuristic h'', where

$$h''(X) = \begin{cases} h(X) - \epsilon & \text{if } X = X_0 \\ h(X) & \text{if otherwise} \end{cases}$$

Since h'' is admissible and will lead to $C = h^*(S)$, and so does h'. Hence, $C = h^*(S)$ always holds.

The two conclusions (<u>underlined</u>) apparently contradict with each other, and **only exactly one of them are correct and the other is wrong**. Choose the **best** explanation from below - which student's conclusion is wrong, and why are they wrong?

- Alice's conclusion is wrong, because the heuristic h' is always admissible.
 Alice's conclusion is wrong, because an inadmissible heuristics does not necessarily always lead to the failure of the optimality when conducting A* tree search.
 Alice's conclusion is wrong, because of another reason that is not listed above.
 Bob's conclusion is wrong, because the node visiting expansion ordering of h" during searching might not be the same as h'.
- Bob's conjusted it gon, present the list of inchested than recompte searches argess of its optimally property.
- O Bob's conclusion is wrong, because of another reason that is not listed above.

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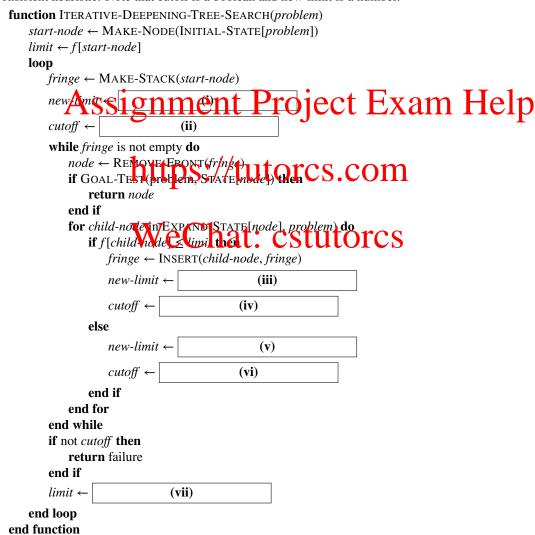
Q2. Iterative Deepening Search

Pacman is performing search in a maze again! The search graph has a branching factor of b, a solution of depth d, a maximum depth of m, and edge costs that may not be integers. Although he knows breadth first search returns the solution with the smallest depth, it takes up too much space, so he decides to try using iterative deepening. As a reminder, in standard depth-first iterative deepening we start by performing a depth first search terminated at a maximum depth of one. If no solution is found, we start over and perform a depth first search to depth two and so on. This way we obtain the shallowest solution, but use only O(bd) space.

But Pacman decides to use a variant of iterative deepening called **iterative deepening A***, where instead of limiting the depth-first search by depth as in standard iterative deepening search, we can limit the depth-first search by the f value as defined in A* search. As a reminder f[node] = g[node] + h[node] where g[node] is the cost of the path from the start state and h[node] is a heuristic value estimating the cost to the closest goal state.

In this question, all searches are tree searches and **not** graph searches.

(a) Complete the pseudocode outlining how to perform iterative deepening A* by choosing the option from the next page that fills in each of these blanks. Iterative deepening A* should return the solution with the lowest cost when given a consistent heuristic. Note that cutoff is a boolean and new-limit is a number.



A_1	-∞	$\mathbf{A_2} \boxed{0}$		A ₃ ∞	A ₄	limit	
$\mathbf{B_1}$	True	B ₂ False		B ₃ cutoff	B ₄	not cutoff	
C_1	new-limit	C ₂ new-l	imit + 1	C_3 new-limit + $f[node]$	C ₄	new-limit + f[child-node]	
$\mathbf{C_5} igg[$	MIN(new-limit, f[node])	•	new-limit, d-node])	$\mathbf{C_7}$ MAX(new-line $f[node]$)	mit, C ₈	MAX(new-limit, f[child-node])	
(i)	$\bigcirc A_1$	$\bigcirc A_2$	$\bigcirc A_3$	\bigcirc $\mathbf{A_4}$			
(ii)	$\bigcirc B_1$	$\bigcirc B_2$	$\bigcirc B_3$	$\bigcirc B_4$			
(iii)			\bigcirc C_3 \bigcirc C_7	$\bigcirc {\operatorname{C}_4} \\ \bigcirc {\operatorname{C}_8}$			
(iv)	$\bigcirc B_1$	$\bigcirc B_2$	$\bigcirc B_3$	\bigcirc B ₄			
(v)			$\bigcirc C_3 \\ \bigcirc C_7$	\bigcirc C_4 \bigcirc C_8			
(vi)	$\bigcirc B_1$	$\bigcirc B_2$	$\bigcirc B_3$	\bigcirc B ₄			
(vii)	Asstg	gnifie	nt Pi	oject Ex	kam I	Help	
iterati	ve deepening A* exp	ard+is True?	If the same		tiple times, o	bout the number of node count all of the times that	
	A* will expand a node	X / (1)	4	4 4		or equal to the number of	

○ We don't know if the number of times iterative deepening A* expands a node is more or less than the number

A* will expand a node.

O None of the above

of times A* will expand a node.