This time: informed search

Informed search:

Use heuristics to guide the search

- Best first
- A* Assignment Project Exam Help
- Heuristics
- Hill-climbing
- Simulated annealing

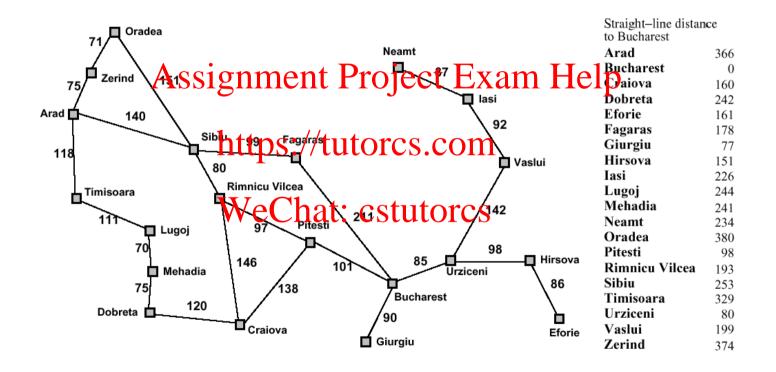
https://tutorcs.com

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Best-first search

- Idea:
 use an evaluation function for each node; estimate of "desirability"
 ⇒ expand most desirable unexpanded jedet Exam Help
- Implementation: https://tutorcs.com
 QueueingFn = insert successors in decreasing order of desirability
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- Special cases: greedy search
 A* search

Romania with step costs in km



Greedy search

Estimation function:

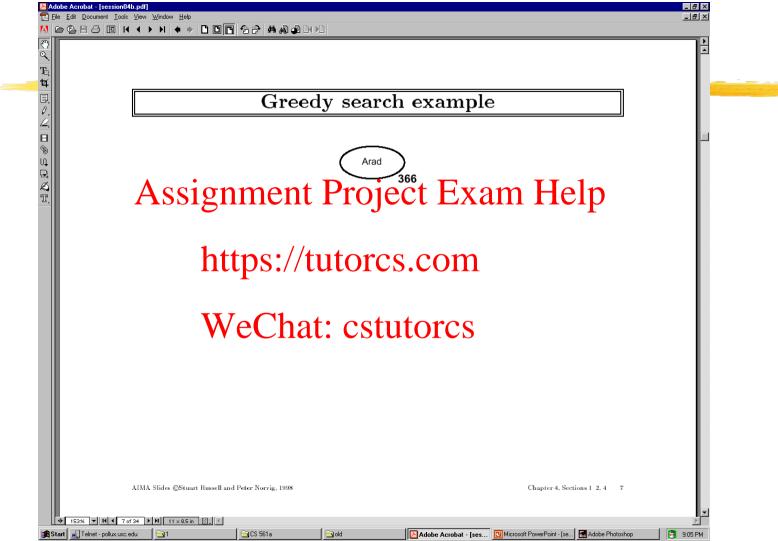
h(n) = estimate of cost from n to goal (heuristic) Assignment Project Exam Help

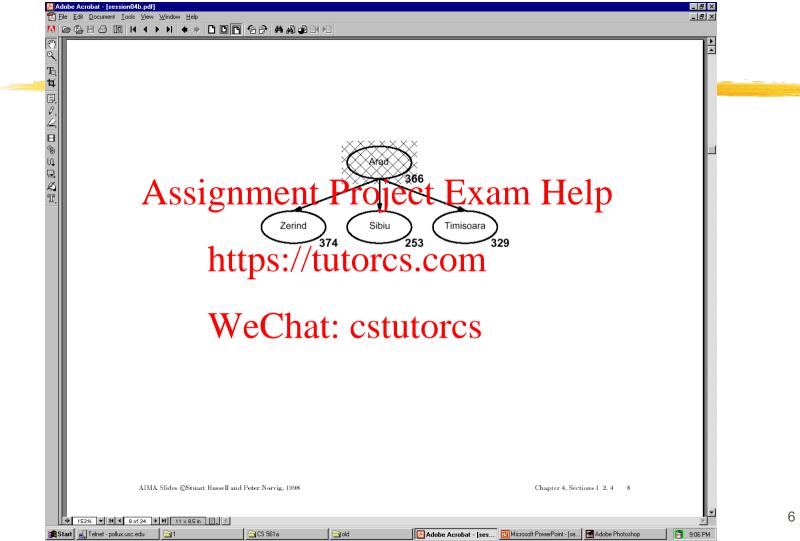
For example:

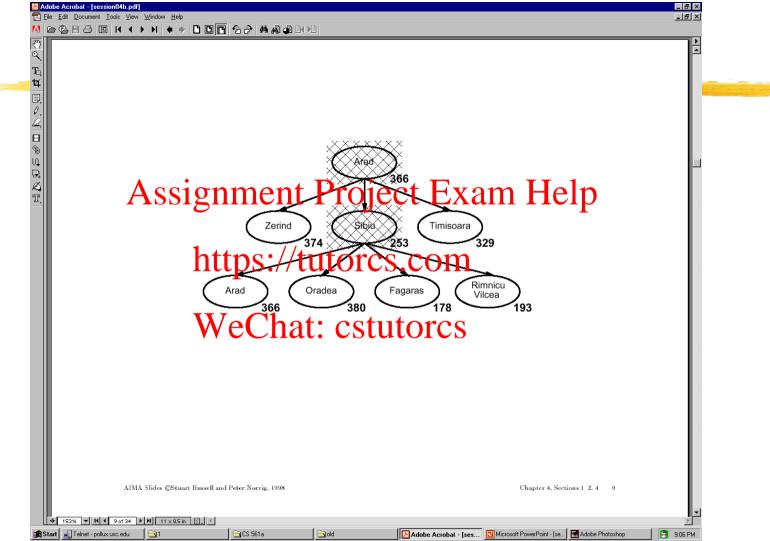
 $h_{SLD}(n) = \text{straight-diptences from n}$ to Bucharest

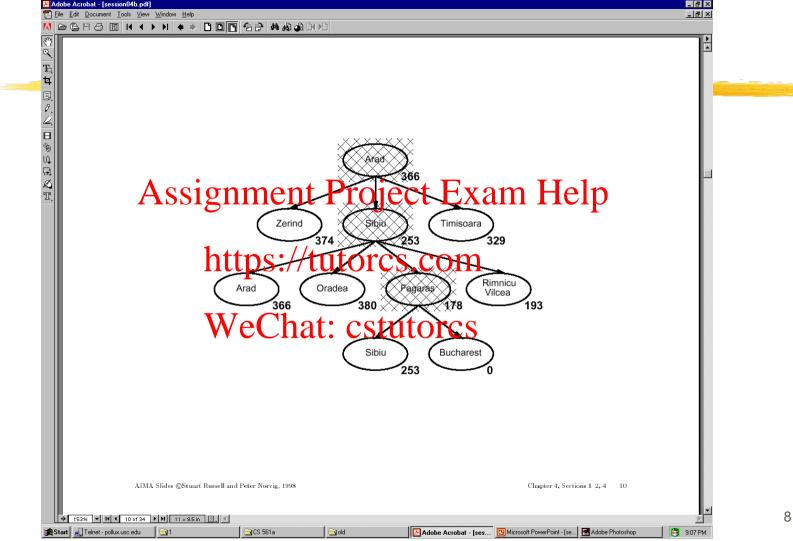
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• Greedy search expands first the node that appears to be closest to the goal, according to h(n).









Properties of Greedy Search

Complete?

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• Time?

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Space?

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Optimal?

Properties of Greedy Search

Complete? No – can get stuck in loops

e.g., Iasi > Neamt > Iasi > Neamt > ...

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Time?

O(b^m) but a good heuristic can give https://dicomosyment

Space?

O(bon) - keeps all nodes in memory

Optimal? No.

A* search

Idea: avoid expanding paths that are already expensive

- A* search uses an admissible heuristic, that is $h(n) \le h^*(n)$ where $h^*(n)$ is the true cost from n. For example: $h_{SLD}(n)$ never overestimates actual road distance.
- Theorem: A* search is optimal

A* search

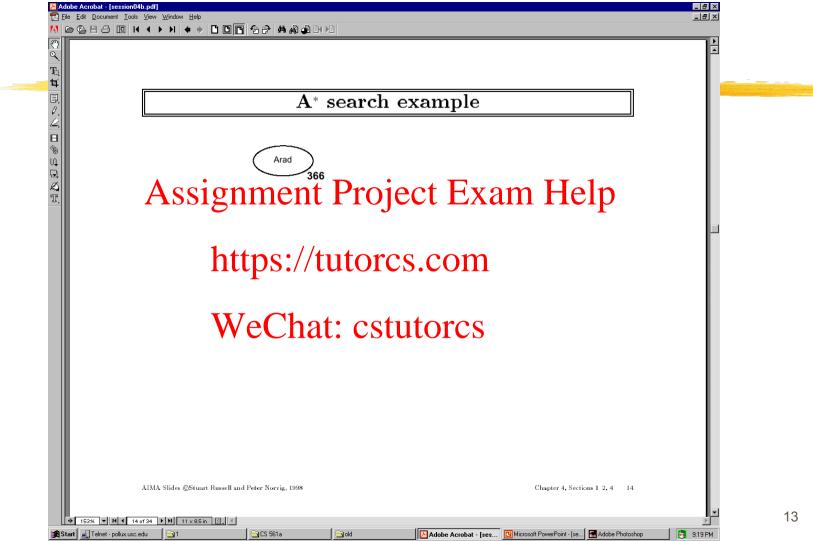
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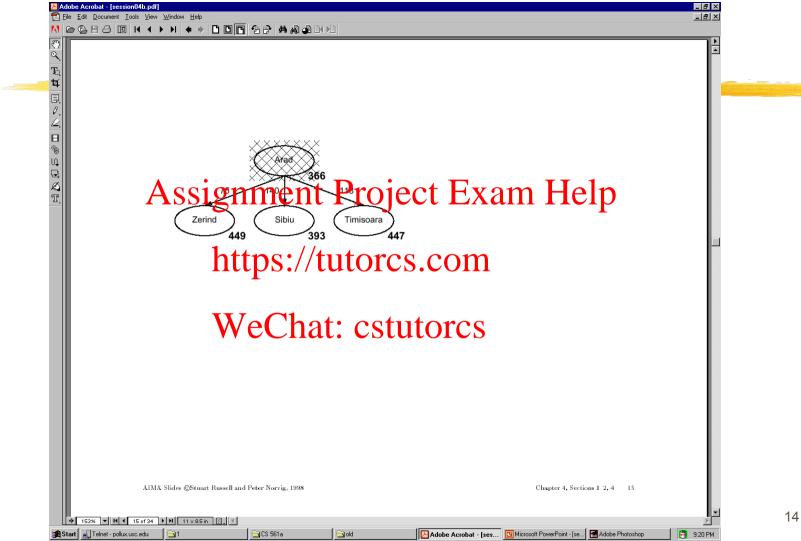
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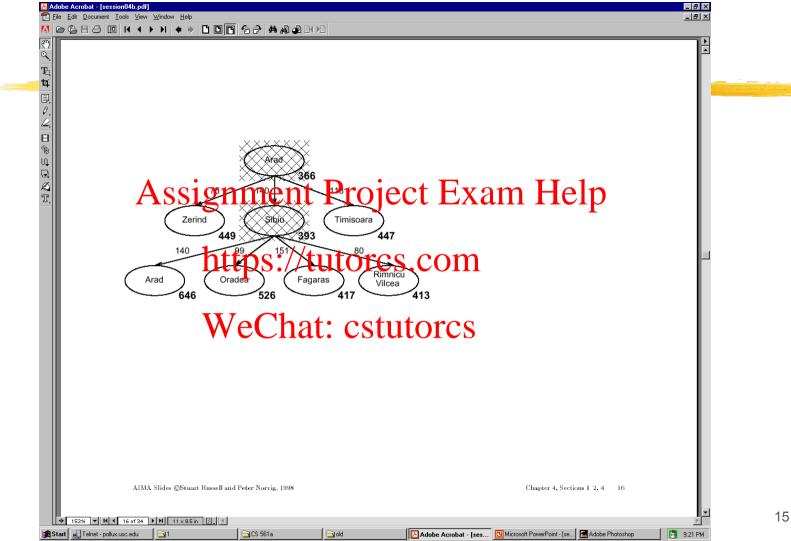
Note: A* is also optimal if the heuristic is consistent, i.e.,

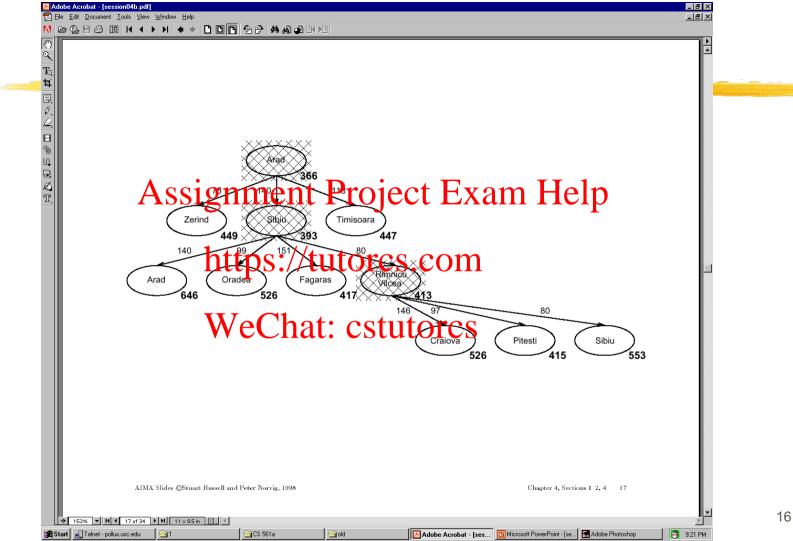
$$h(N) \leq N_{\mathcal{F}} G$$
 at $h_{\mathcal{F}}$ at $h_{\mathcal{F}}$ Actual cost From N to P

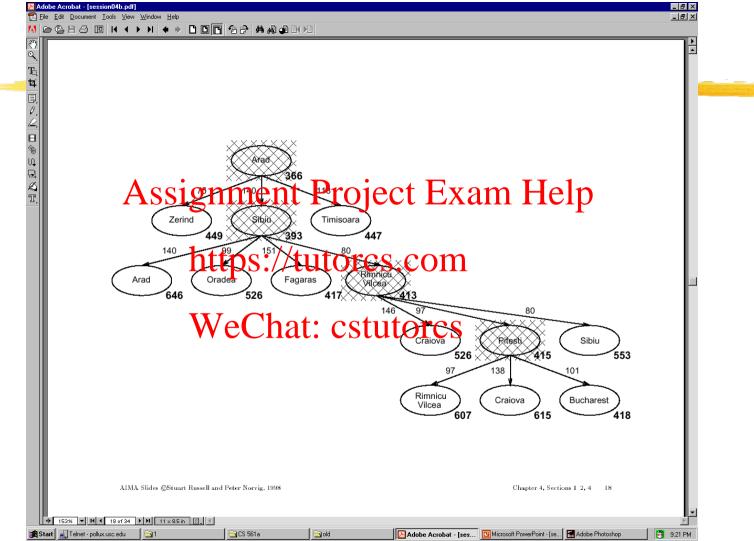
• (a consistent heuristic is admissible (by induction), but the converse is not always true)

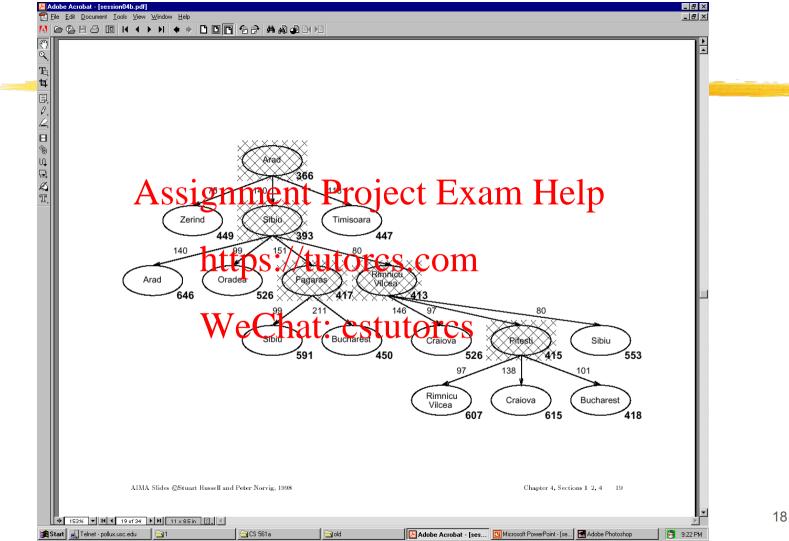












Optimality of A* (standard proof)

Suppose some suboptimal goal G_2 has been generated and is in the queue. Let n be an unexpanded node on a shortest path to an optimal goal G_1 .

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$$f(G_2) = g(G_2)$$
 since $h(G_2) = 0$
> $g(G_1)$ since G_2 is suboptimal
 $\geq f(n)$ since h is admissible

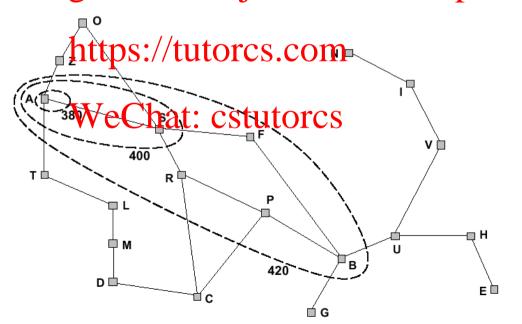
Since $f(G_2) > f(n)$, A* will never select G_2 for expansion

Optimality of A* (more useful proof)

<u>Lemma</u>: A^* expands nodes in order of increasing f value

Gradually adds "f-contours" of nodes (cf. breadth-first adds layers)

Contour Abs ig more with Projection for the Exame Help



f-contours

How do the contours look like when h(n) = 0? Assignment Project Exam Help tos://tutorcs.com ⊞ H □ М D

Properties of A*

Complete?

• Time? Assignment Project Exam Help

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Space?

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Optimal?

Properties of A*

Complete? Yes, unless infinitely many nodes with f ≤ f(G)

Time?

Space?

Assignment (Paroject Examele Polution)]

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Keeps all nodes in memory

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Optimal? Yes – cannot expand f_{i+1} until f_i is finished

Proof of lemma: pathmax

For some admissible heuristics, f may decrease along a path

E.g., suppose n' is a successor of n

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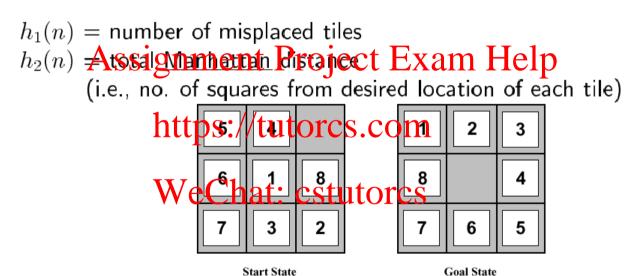
But this throws away information! $f(n) = 9 \Rightarrow$ true cost of a path through n is ≥ 9 Hence true cost of a path through n' is > 9 also

Pathmax modification to A*: Instead of f(n') = g(n') + h(n'), use f(n') = max(g(n') + h(n'), f(n))

With pathmax, f is always nondecreasing along any path

Admissible heuristics

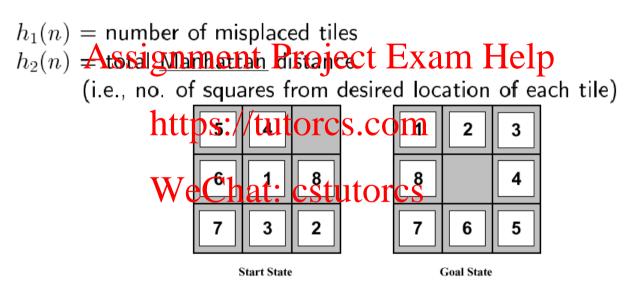
E.g., for the 8-puzzle:



$$\frac{h_1(S) = ??}{h_2(S) = ??}$$

Admissible heuristics

E.g., for the 8-puzzle:



$$\frac{h_1(S)}{h_2(S)} = ??$$
 7 $\frac{h_2(S)}{1} = ??$ 2+3+3+2+4+2+0+2 = **1**8

CS 561, Sessions 4-5

Relaxed Problem

- Admissible heuristics can be derived from the exact solution cost of a relaxed version of the problem that Project Exam Help
- If the rules of the 8-puzzle are relaxed so that a tile can move anywhere, then $h_1(n)$ gives the shortest solution.

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• If the rules are relaxed so that a tile can move to any adjacent square, then h₂(n) gives the shortest solution.

This time

- Iterative improvement
- Hill climbing
- Simulated annealing Assignment Project Exam Help

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Iterative improvement

 In many optimization problems, path is irrelevant; the goal state itself is the solution.

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• Then, state space = space of "complete" configurations.

Algorithm goal: https://tutorcs.com

- find optimal configuration (e.g., TSP), or,
- find configuration satisfying gongtraints (e.g., n-queens)
- In such cases, can use iterative improvement algorithms: keep a single "current" state, and try to improve it.

Iterative improvement example: vacuum world

Simplified world: 2 locations, each may or not contain dirt, each may or not contain vacuuming agent.

Goal of agent: clean up the dirt.

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If path does not matter, do not need to keep track of it.

Single-state, start in #5. Solution?? https://tutorcs.com Multiple-state, start in $\{1, 2, 3, 4, 5, 6, 7, 8\}$ e.g., Right goes (4) 621: Southon? CS Contingency, start in #5 Murphy's Law: Suck can dirty a clean car-23 pet Local sensing: dirt, location only. Solution??

Iterative improvement example: n-queens

 Goal: Put n chess-game queens on an n x n board, with no two queens on the same row, column, or diagonal.



 Here, goal state is initially unknown but is specified by constraints that it must satisfy.

Hill climbing (or gradient ascent/descent)

 Iteratively maximize "value" of current state, by replacing it by successor state that has highest value, as long as possible.

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"Like climbing Everest in thick fog with amnesia"

```
function Hill-Climbing( problem) returns a solution state
inputs: problem, a problem
local variables: curvetterno pat: cstutorcs
next, a node

current ← Make-Node(Initial-State[problem])
loop do

next ← a highest-valued successor of current
if Value[next] < Value[current] then return current
current ← next
end
```

Hill climbing

Note: minimizing a "value" function v(n) is equivalent to maximizing –v(n),

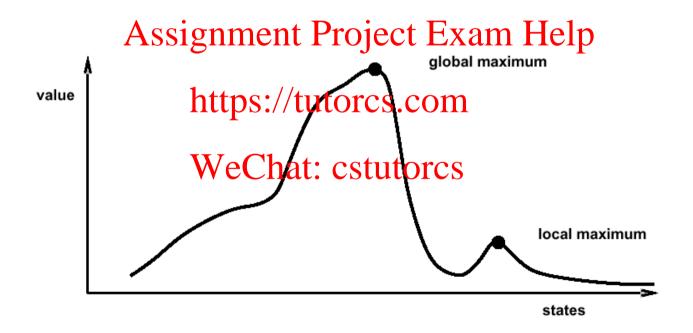
thus both notions are year interdiangle by Exam Help

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Notion of "extremizative" (fill detxtremtal (minima or maxima) of a value function.

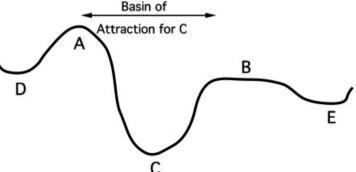
Hill climbing

Problem: depending on initial state, may get stuck in local extremum.



Minimizing energy

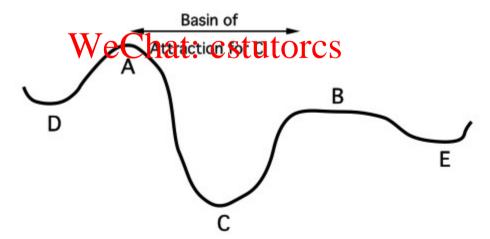
- Let's now change the formulation of the problem a bit, so that we can employ new formalism:
 - let's compare our state space to that of a physical Hsystem that is subject to natural interactions,
 - and let's compare our value function to the overall potential energy E of the systematics.//tutorcs.com
- On every updating, WeChat: cstutorcs we have ΔE ≤ 0



Minimizing energy

- Hence the dynamics of the system tend to move E toward a minimum.
- Assignment Project Exam Help

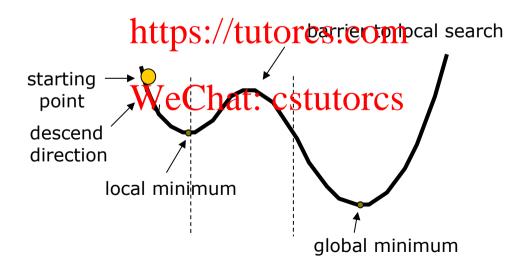
 We stress that there may be different such states they are *local* minima. Global minimization is not guaranteed. https://tutorcs.com



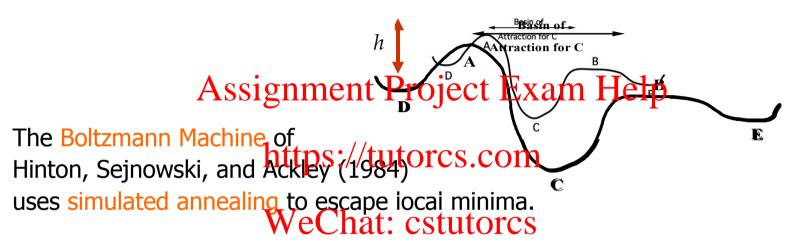
Local Minima Problem

Question: How do you avoid this local minimum?

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Boltzmann machines



To motivate their solution, consider how one might get a ball-bearing traveling along the curve to "probably end up" in the deepest minimum. The idea is to shake the box "about h hard" — then the ball is more likely to go from D to C than from C to D. So, on average, the ball should end up in C's valley.

Consequences of the Occasional Ascents

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Help escaping the local optima.

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adverse effect

(easy to avoid by keeping track of best-ever state)

Might pass global optima

after reaching it

Simulated annealing: basic idea

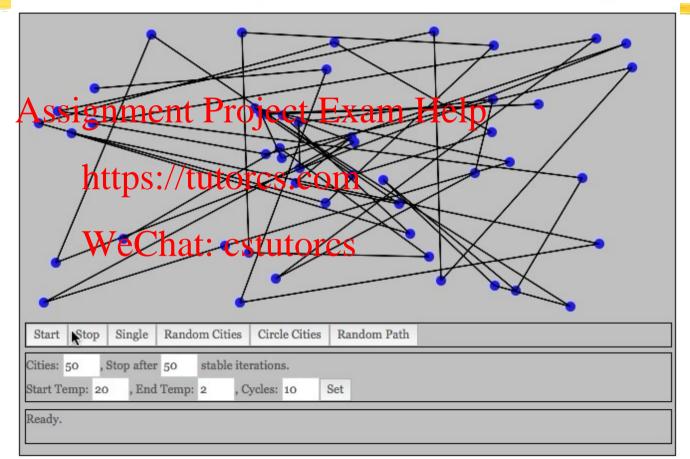
- From current state, pick a random successor state;
- If it has better Aque than current Pstate the xaccept the pansition," that is, use successor state as current state;

https://tutorcs.com

- Otherwise, do not give up, but instead flip a coin and accept the transition with a given probability (that is lower as the successor is worse).
- So we accept to sometimes "un-optimize" the value function a little with a non-zero probability.

Demo

AIFH Volume 1, Chapter 9: Traveling Salesman (TSP): Simulated Annealing



Boltzmann's statistical theory of gases

- In the statistical theory of gases, the gas is described not by a deterministic dynamics, but rather by the probability shall will be in different states. The probability shall will be in different states.
- The 19th century physicist type ig / type ig / type ig / per geveloped a theory that included a probability distribution of temperature (i.e., every small region of the gas had the same kinetic energy).
- Hinton, Sejnowski and Ackley's idea was that this distribution might also be used to describe neural interactions, where low temperature T is replaced by a small noise term T (the neural analog of random thermal motion of molecules). While their results primarily concern optimization using neural networks, the idea is more general.

Boltzmann distribution

• At thermal equilibrium at temperature T, the Boltzmann distribution gives the relative probability that the system will occupy state A vs. state B as:

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$$\frac{P(A)}{P(B)} = \exp\left[-\frac{httpsE(B)toE(B)om_{exp}(E(B)/T)}{WeChat: Cstutorcs}\right] = \exp(E(A)/T)$$

where E(A) and E(B) are the energies associated with states A and B.

Simulated annealing

Kirkpatrick et al. 1983:

Simulated annealing is a general method for making likely the escape from

local minima by allowing jumps to higher energy states.

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The analogy here is with the process of annealing used by a craftsman in forging a sword from an alloy.

He heats the metal, then slowly cools it as he hammers the plade into shape.

- If he cools the blade too quickly the metal will form patches of different composition;
- composition;

 If the metal is cooled slowly while it is snaped, the constituent metals will form a uniform alloy.





Simulated annealing in practice

- set T
- optimize for given T
- lower T Assignment Projecte Exam Help
- repeat

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- Geman & Geman (1984): if T is lowered sufficiently slowly (with respect to the number of iterations used to optimize (a) party, eighted progenting is guaranteed to find the global minimum.
- Caveat: this algorithm has no end (Geman & Geman's T decrease schedule is in the 1/log of the number of iterations, so, T will never reach zero), so it may take an infinite amount of time for it to find the global minimum.

Simulated annealing algorithm

 Idea: Escape local extrema by allowing "bad moves," but gradually decrease their size and frequency.

```
function SIMASSI ANTAI CONTROL OF CT PER A MILITAGE PO
   inputs: problem, a problem
            schedule, a mapping from time to "temperature"
   local variables: cuntil 35. / tutores.com
                      next. a node
                      T, a "temperature" controlling the probability of downward steps
   current ← MAKE-NOW ECIA PATTE STATIOTCS
   for t \leftarrow 1 to \infty do
        T \leftarrow schedule[t]
        if T=0 then return current
        next \leftarrow a randomly selected successor of current
        \Delta E \leftarrow \text{Value}[next] \quad \text{Value}[current]
        if \Delta E > 0 then current \leftarrow next
       else current \leftarrow next only with probability e^{\Delta E/T}
```

Simulated annealing algorithm

 Idea: Escape local extrema by allowing "bad moves," but gradually decrease their size and frequency.

```
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       else current \leftarrow next only with probability e^{\Delta E/T}
```

Note on simulated annealing: limit cases

• Boltzmann distribution: accept "bad move" with $\Delta E < 0$ (goal is to maximize E) with probability $P(\Delta E) = \exp(\Delta E/T)$

• If T is large: Assignment Project Exam Help

 $\Delta E/T < 0$ and very small

https://tores.teem
accept bad move with high probability

• If T is near 0: WeChat cstutorcs

 $\Delta E/T < 0$ and very large $\exp(\Delta E/T)$ close to 0 accept bad move with low probability

Note on simulated annealing: limit cases

• Boltzmann distribution: accept "bad move" with $\Delta E < 0$ (goal is to maximize E) with probability $P(\Delta E) = \exp(\Delta E/T)$

• If T is large: Assignment Project Exam Help

 $\Delta E/T < 0$ and very small

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accept bad move with high probability

• If T is near 0:

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Random walk

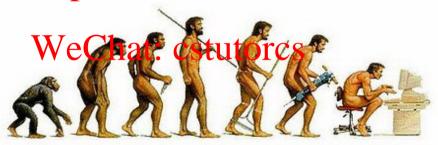
 $\Delta E/T < 0$ and very large $\exp(\Delta E/T)$ close to 0 accept bad move with low probability

Deterministic up-hill

Genetic Algorithms

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How do you find a solution in a large complex space?

Ask an expert?

Ask an expert?
Adapt existing designs signment Project Exam Help

Trial and error?

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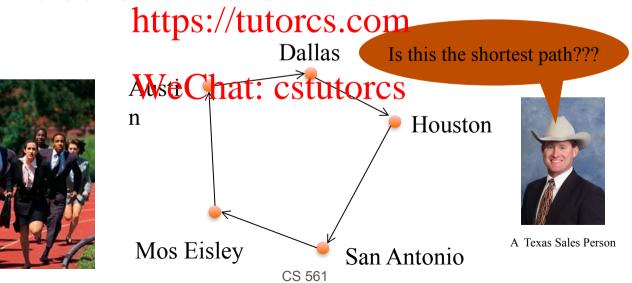
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Example: Traveling Sales Person (TSP)

- Classic Example: You have N cities, find the shortest route such that your salesperson will visit each city once and return.
- This problem is known to be NP-Hard Project Exam Help

 As a new city is added to the problem, computation time in the classic solution increases exponentially $O(2^n)$... (as far as we know)



What if.....

- Lets create a whole bunch of random sales people and see how well they do and pick the best one(s).
 - Salesperson A
 - Houston -> Dallas -> Austin -> San Antonio -> Mos Eisely
 Distance Traveled 780 27 Ment Project Exam Help
 - Salesperson B
 - Houston -> Mos Eisley -- Austin -> San Antonio -> Dallas
 Distance Traveled 820 Km
 - Salesperson A is better (more fit) than salesperson B
 - Perhaps we would like sales people to be more like A and less like B
- Ouestion:
 - do we want to just keep picking random sales people like this and keep testing them?

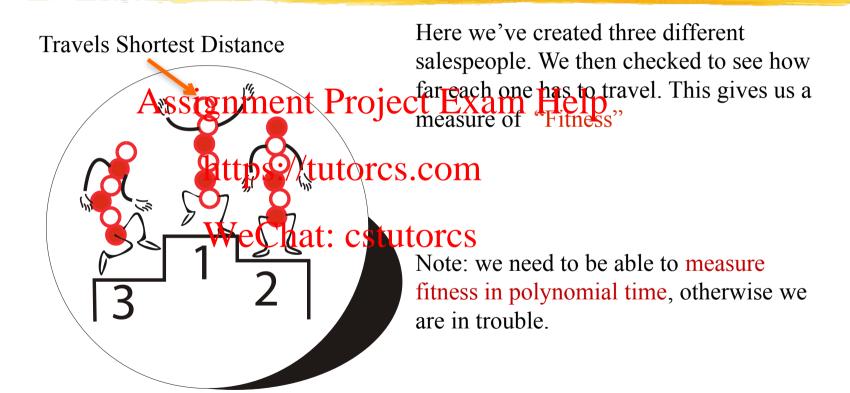
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Represent problem like a DNA sequence

Each DNA sequence is an encoding of a possible solution to the problem. Assignment Project Exam Help San Antonio Dallag //tutorescom Mos Eisely Mos Eisely hat: cstutores Austin Austin DNA - Salesperson B The order of the cities in the genes is the order of the cities the TSP will take. CS 561

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Ranking by Fitness:



Let's breed them!

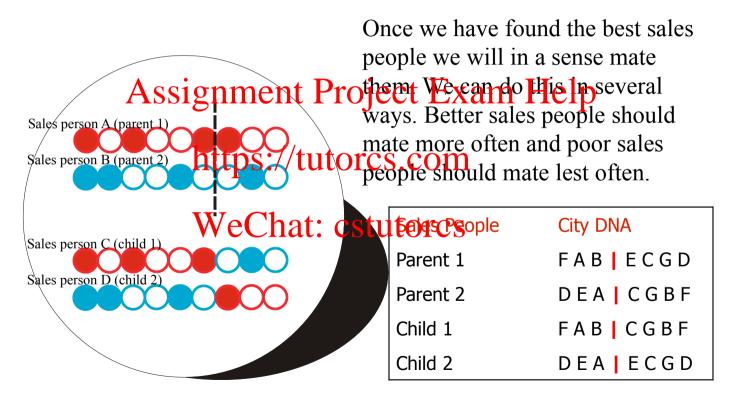
- We have a population of traveling sales people. We also know their fitness based on how long their trip is. We want to create more, but we don't want to create too many.
- We take the notion that the salespeople who perform better are closer to the optimal salesperson than the salesperson be a "combination" of the better sales people?
- We create a population of sales people as solutions to the problem.
- How do we actually mate a population of data????

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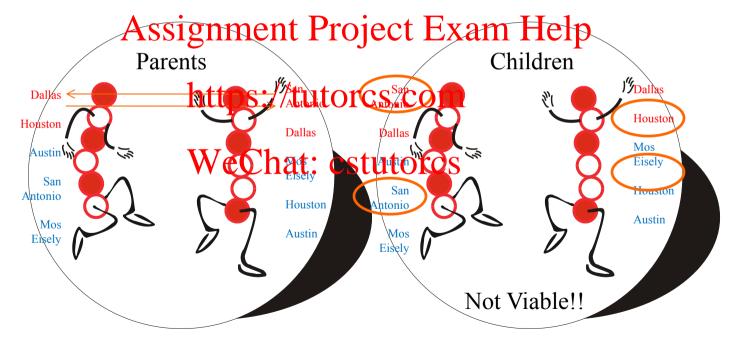
Crossover:

Exchanging information through some part of information (representation)



Crossover Bounds (Houston we have a problem)

- Not all crossed pairs are viable. We can only visit a city once.
- Different GA problems may have different bounds.



TSP needs some special rules for crossover

- Many GA problems also need special crossover rules.
- Since each genetic sequence contains all the cities in the travel, crossover is a swapping of travel order.

Remembers that crossover approjects to Dexefficien Help Children Parents https://tutorcs.com Dallas Antonio Antonio Mos Houston Eisely Austin Houston Eisely San Austin San Antonio Houston Antonio Mos Mos Austin Eisely Austin Eisely

CS 561

Viable ©

What about local extrema?

- With just crossover breading, we are constrained to gene sequences which are a cross product of our current population.
- Introduce random effects into our population,
 - Mutation Random Standard Enter Mitto pactro Exiting Help
 - Cataclysm Kill off n% of your population and create fresh new salespeople if it looks like you are reaching a local minimum.

 • Annealing of Mating Pairs Appent the mating of Supptimal pairs with some probability.

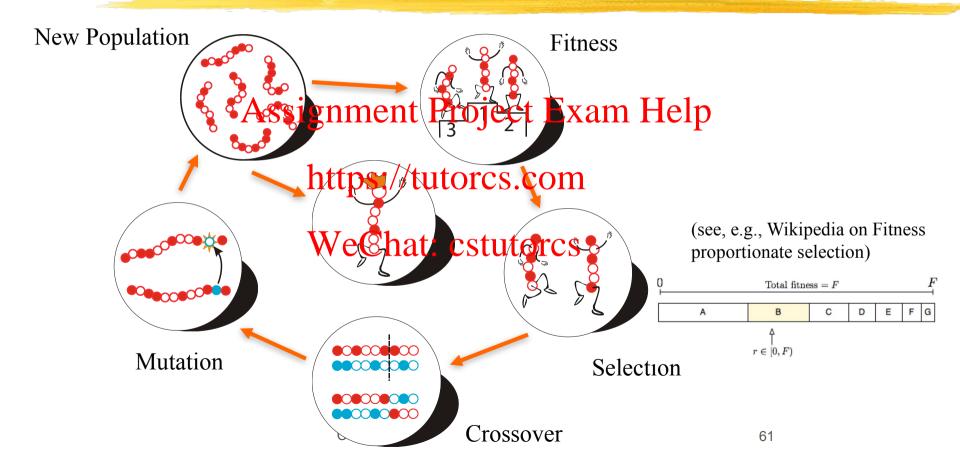
 - Etc...





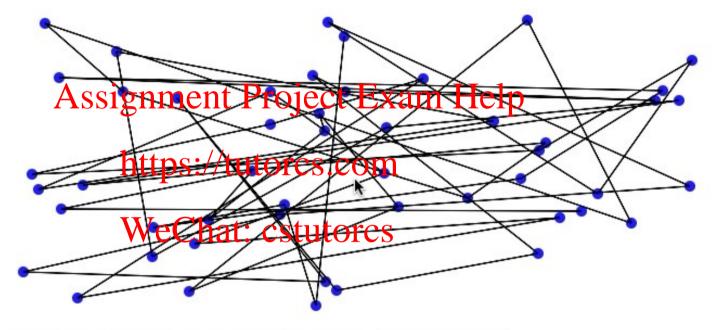
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In summation: The GA Cycle



Demo

AIFH Volume 2, Chapter 9: Traveling Salesman (TSP): Genetic Algorithm



Start	Stop		gle I	Random Cities		Circle Citie	s N	New Population		
Cities: 5	50 , Stop after 50			50	stable iterations.					
Populati	ion: 1	000	, Muta	tion %:	0.2	, % to Mate:	0.2	, Eligible Pop %:	0.5	Set

GA and TSP: the claims

- Can solve for over 3500 cities (still took over 1 CPU years).
 - Maybe holds the record.
- Will get within 2% of the optimal solution.
 - This means that its Solgaments Project proximate. Help



GA Discussion

- We can apply the GA solution to any problem where the we can represent the problems solution (even very abstractly) as a string.
- · We can create strings signment Project Exam Help
 - Digits
 - LabelsPointershttps://tutorcs.com
 - Code Blocks This creates new programs from strung together blocks of code. The key is to make sure the code can run.
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 - Whole Programs Modules or complete programs can be strung together in a series. We can also re-arrange the linkages between programs.
- The last two are examples of Genetic Programming

Things to consider

- How large is your population?
 - A large population will take more time to run (you have to test each member for fitness!).

A large population will cover more bases at once. Assignment Project Exam Help

- How do you select your initial population?
 - You might create a population applications applications might start you in the wrong position with too much bias.
- How will you cross bread your population?

 You want to cross bread and select for your best specimens.
 - Too strict: You will tend towards local minima
 - Too lax: Your problem will converge slower
- How will you mutate your population?
 - Too little: your problem will tend to get stuck in local minima
 - Too much: your population will fill with noise and not settle.

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GA is a good no clue approach to problem solving

- GA is superb if:
 - Your space is loaded with lots of weird bumps and local minima.
 - GA tends to spread out and test a larger subset of your space than many other types of learning/optimation regrithment Project Exam Help
 - You don't quite understand the underlying process of your problem space.
 - NO I DONT: What makes the stock market work??? Don't know? Me neither! Stock market prediction might thus be good for a GA.
 - YES I DO: Want to make a program to predict people's height from personality factors? This might be a Gaussian process and a good candidate for statistical methods which are more efficient.
 - You have lots of processors
 - GA's parallelize very easily!

Why not use GA?

- Creating generations of samples and cross breading them can be resource intensive.
 - Some problems may be better solved by a general gradient descent method which uses less resource.
 - However, resour sq. wisq. whitstill putte efficient of computation of derivatives, etc).
- In general if you know the transmitted to the space, there may be a better solution designed for your specific need.
 - Consider Kernel Based Learning and Support Vector Machines?
 - Consider Neural Networks? eChat: cstutorcs
 - Consider Traditional Polynomial Time Algorithms?
 - Etc.

More demos: motorcycle design

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Summary

- Best-first search = general search, where the minimum-cost nodes (according to some measure) are expanded first.
- Greedy search = best-first with the estimated cost to reach the goal as a heuristic measure.
 - Generally faster than uninformed Perch ject Exam Help
 - not complete.
- A* search = best-first with measure path cost so far + estimated path cost to goal.
 - combines advantages of uniform-cost and greedy searches
 - complete, optimal and optimally efficient tutores
 - space complexity still exponential
- Hill climbing and simulated annealing: iteratively improve on current state
 - lowest space complexity, just O(1)
 - risk of getting stuck in local extrema (unless following proper simulated annealing schedule)
- Genetic algorithms: parallelize the search problem