

ARCH/GARCH

1 Importing packages

```
[4]: #importing packages
import statsmodels.api as sm
from statsmodels.tsa.stattools import adfuller
import pandas as pd
import numpy as np
import statsmodels.formula.api as smf
from sklearn import linear_model
import matplotlib.pyplot as plt
from scipy import stats
```

2 Reading Excel file saved in hard drive

```
[5]: #reading the file
df = pd.read_excel('C:\\Users\\rluck\\OneDrive\\share.xlsx')
df.head()
```

```
[5]:
```

| | OBS | PRICE |
|---|-----|--------|
| 0 | 1 | 975.04 |
| 1 | 2 | 977.07 |
| 2 | 3 | 966.58 |
| 3 | 4 | 964.00 |
| 4 | 5 | 956.05 |

3 Calculating annual return

```
[6]: #computing the annual return from S&P500
df['R'] = 100*np.log(df['PRICE']/df['PRICE'].shift(1))
df['R_squared']=df['R']**2
df.head()
```

```
[6]:
```

| | OBS | PRICE | R | R_squared |
|---|-----|--------|----------|-----------|
| 0 | 1 | 975.04 | NaN | NaN |
| 1 | 2 | 977.07 | 0.207980 | 0.043256 |

| | | | | |
|---|---|--------|-----------|----------|
| 2 | 3 | 966.58 | -1.079423 | 1.165154 |
| 3 | 4 | 964.00 | -0.267277 | 0.071437 |
| 4 | 5 | 956.05 | -0.828108 | 0.685763 |

```
[7]: df.tail(10)
```

```
[7]:
```

| | OBS | PRICE | R | R_squared |
|-----|-----|---------|-----------|-----------|
| 984 | 985 | 1149.50 | -0.686632 | 0.471464 |
| 985 | 986 | 1128.52 | -1.842003 | 3.392973 |
| 986 | 987 | 1140.21 | 1.030542 | 1.062016 |
| 987 | 988 | 1139.45 | -0.066677 | 0.004446 |
| 988 | 989 | 1129.90 | -0.841656 | 0.708384 |
| 989 | 990 | 1144.80 | 1.310082 | 1.716314 |
| 990 | 991 | 1170.35 | 2.207290 | 4.872129 |
| 991 | 992 | 1167.10 | -0.278081 | 0.077329 |
| 992 | 993 | 1158.31 | -0.755999 | 0.571535 |
| 993 | 994 | 1139.93 | -1.599519 | 2.558461 |

4 Remove the first row NaN

```
[8]: #Selecting the sample from
dta =df.iloc[1:993]
dta.head()
```

```
[8]:
```

| | OBS | PRICE | R | R_squared |
|---|-----|--------|-----------|-----------|
| 1 | 2 | 977.07 | 0.207980 | 0.043256 |
| 2 | 3 | 966.58 | -1.079423 | 1.165154 |
| 3 | 4 | 964.00 | -0.267277 | 0.071437 |
| 4 | 5 | 956.05 | -0.828108 | 0.685763 |
| 5 | 6 | 927.69 | -3.011259 | 9.067679 |

```
[9]: dta.tail()
```

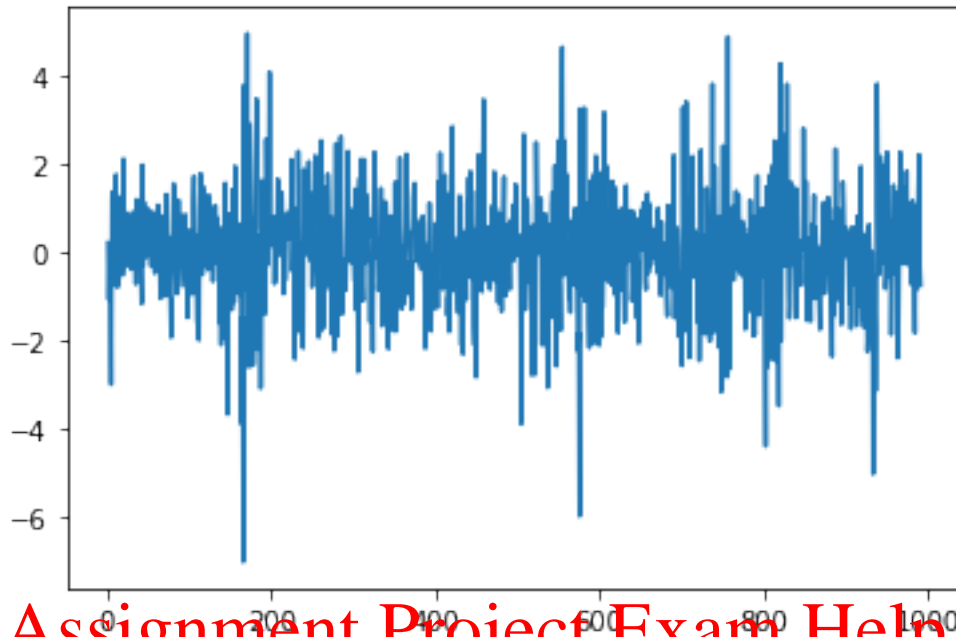
```
[9]:
```

| | OBS | PRICE | R | R_squared |
|-----|-----|---------|-----------|-----------|
| 988 | 989 | 1129.90 | -0.841656 | 0.708384 |
| 989 | 990 | 1144.80 | 1.310082 | 1.716314 |
| 990 | 991 | 1170.35 | 2.207290 | 4.872129 |
| 991 | 992 | 1167.10 | -0.278081 | 0.077329 |
| 992 | 993 | 1158.31 | -0.755999 | 0.571535 |

5 Plotting the time series: Stock Returns (R) and R_squared

```
[10]: #plotting the series
plt.plot(dta["R"])
```

[10]: [<matplotlib.lines.Line2D at 0x2585011a288>]



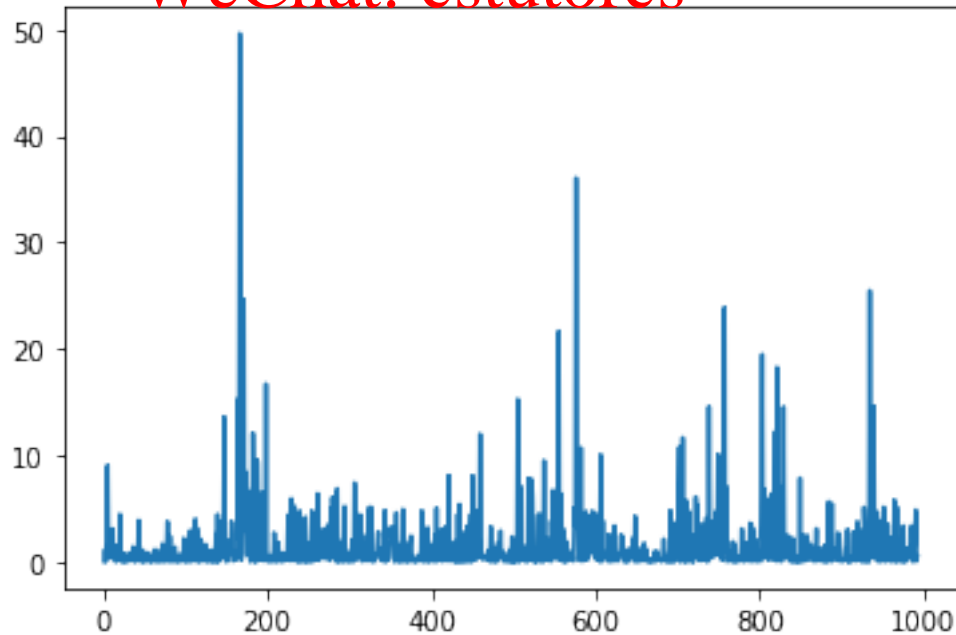
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[11]: `plt.plot(dta["R_squared"])`

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[11]: [<matplotlib.lines.Line2D at 0x25852304c08>]

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6 Histogram and Descriptive Stats for R and R-squared

```
[12]: dta.describe()
```

```
[12]:
```

| | OBS | PRICE | R | R_squared |
|-------|------------|-------------|------------|------------|
| count | 992.000000 | 992.000000 | 992.000000 | 992.000000 |
| mean | 497.500000 | 1260.198357 | 0.017363 | 1.692547 |
| std | 286.510035 | 146.782611 | 1.301519 | 3.393702 |
| min | 2.000000 | 927.690000 | -7.043759 | 0.000000 |
| 25% | 249.750000 | 1130.230000 | -0.716307 | 0.127786 |
| 50% | 497.500000 | 1277.625000 | 0.008016 | 0.565664 |
| 75% | 745.250000 | 1378.312500 | 0.804720 | 1.887633 |
| max | 993.000000 | 1527.460000 | 4.964596 | 49.614541 |

```
[13]: stats.describe(dta['R'])
```

```
[13]: DescribeResult(nobs=992, minmax=(-7.043759037302043, 4.964596183505854),  
mean=0.01736278922631672, variance=1.6929527952681107,  
skewness=-0.14891712656209458, kurtosis=2.0249867442229768)
```

```
[14]: skewness =-0.14891712656209458  
kurtosis =2.0249867442229768  
nobs =992  
JB =(skewness**2+0.25*(kurtosis**2))*nobs/6  
JB
```

```
[14]: 173.15676433983288
```

```
[15]: stats.describe(dta['R_squared'])
```

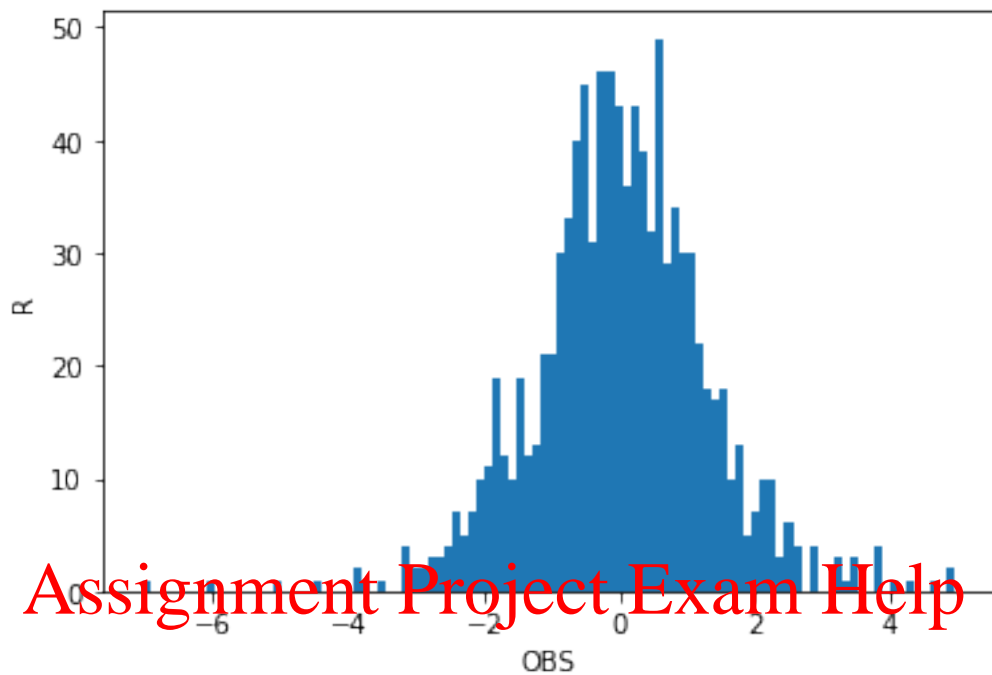
```
[15]: DescribeResult(nobs=992, minmax=(0.0, 49.614541375574206),  
mean=1.6925465579650458, variance=11.51721120039891, skewness=6.16765210396571,  
kurtosis=59.59838877039361)
```

```
[16]: skewness =6.16765210396571  
kurtosis =59.59838877039361  
nobs =992  
JB_R_squared = (skewness**2+0.25*(kurtosis**2))*nobs/6  
JB_R_squared
```

```
[16]: 153103.94385573984
```

```
[17]: import matplotlib.pyplot as plt  
_ = plt.hist(dta['R'],bins=100)  
_ = plt.xlabel('OBS')
```

```
_ = plt.ylabel('R')  
plt.show()
```

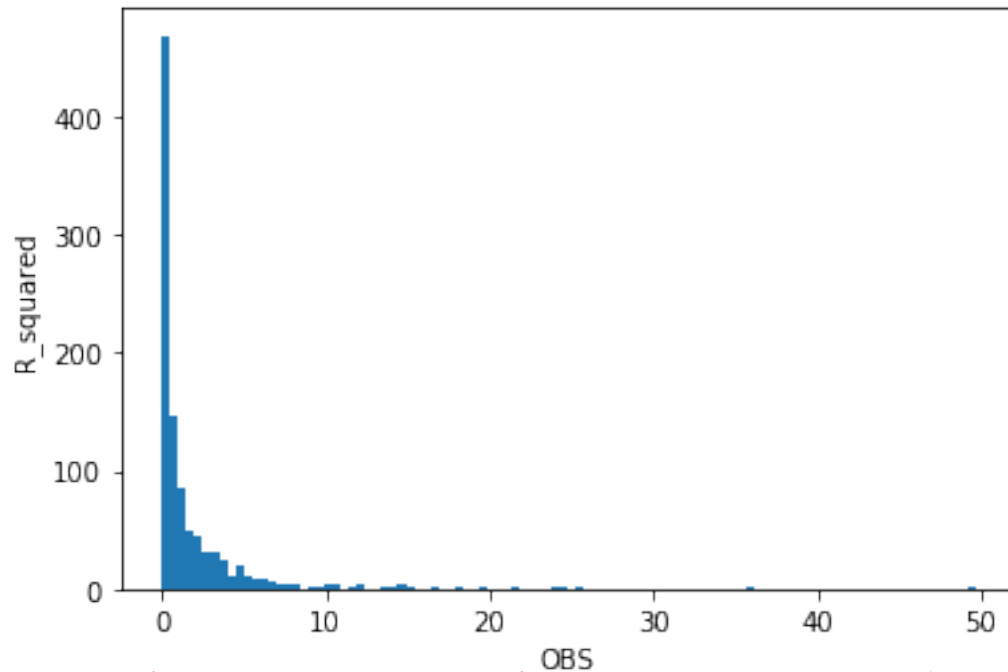


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```
[18]: import matplotlib.pyplot as plt  
_ = plt.hist(dta['R_squared'], bins=100)  
_ = plt.xlabel('OBS')  
_ = plt.ylabel('R_squared')  
plt.show()
```

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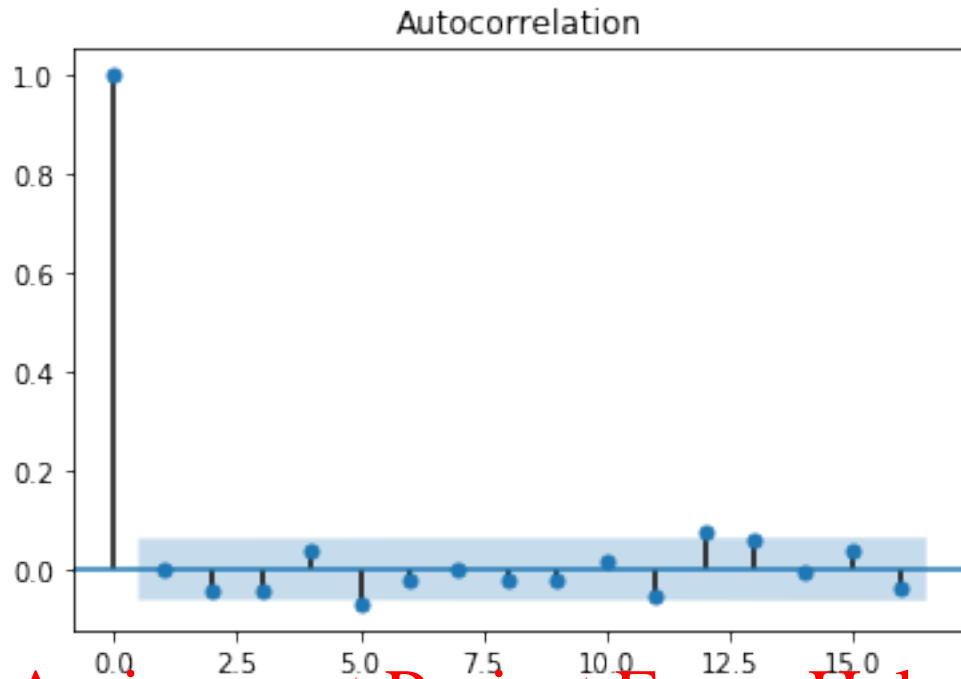
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7 Correlogram: ACF and PACF

```
[19]: #running ACF and PACF for R  
dt= dta["R"]  
sm.graphics.tsa.plot_acf(dt.values.squeeze(),lags=16)  
sm.graphics.tsa.plot_pacf(dt.values.squeeze(),lags=16)  
plt.show()
```

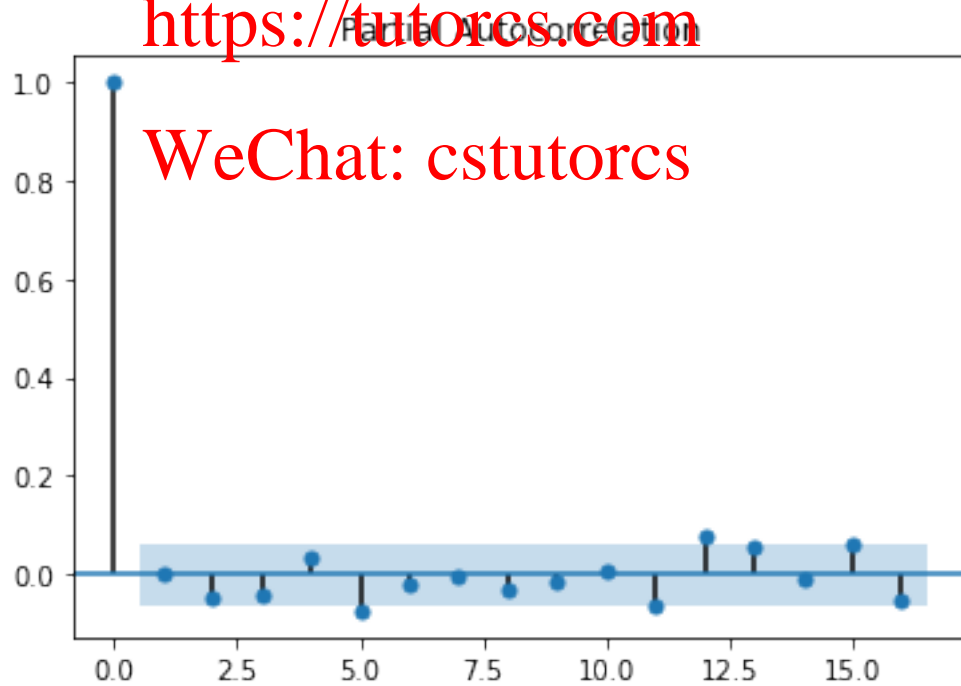
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```
[20]: # Generating the Q tables
import numpy as np
```

```

r,q,p = sm.tsa.acf(dt.values.squeeze(), qstat=True)
data = np.c_[range(1,41), r[1:], q, p]
table = pd.DataFrame(data, columns=['lag', "AC", "Q", "Prob(>Q)"])
print (table.set_index('lag'))

```

| lag | AC | Q | Prob(>Q) |
|------|-----------|-----------|----------|
| 1.0 | 0.001446 | 0.002080 | 0.963620 |
| 2.0 | -0.044905 | 2.010474 | 0.365958 |
| 3.0 | -0.040718 | 3.663503 | 0.300167 |
| 4.0 | 0.037876 | 5.095256 | 0.277663 |
| 5.0 | -0.069898 | 9.976307 | 0.075909 |
| 6.0 | -0.019862 | 10.370809 | 0.109880 |
| 7.0 | -0.000438 | 10.371001 | 0.168506 |
| 8.0 | -0.021094 | 10.816882 | 0.212292 |
| 9.0 | -0.020588 | 11.242059 | 0.259481 |
| 10.0 | 0.014929 | 11.465847 | 0.322393 |
| 11.0 | -0.053056 | 14.295314 | 0.217081 |
| 12.0 | 0.076836 | 20.235581 | 0.062759 |
| 13.0 | 0.056728 | 23.709332 | 0.033911 |
| 14.0 | -0.007241 | 23.762190 | 0.048944 |
| 15.0 | 0.039360 | 25.325770 | 0.045736 |
| 16.0 | -0.040193 | 26.957906 | 0.041953 |
| 17.0 | 0.014454 | 27.169196 | 0.055633 |
| 18.0 | -0.055402 | 30.276587 | 0.034843 |
| 19.0 | 0.021315 | 30.736999 | 0.043136 |
| 20.0 | -0.010348 | 30.845619 | 0.057262 |
| 21.0 | -0.054457 | 33.857101 | 0.037536 |
| 22.0 | -0.015306 | 34.095254 | 0.048040 |
| 23.0 | 0.029443 | 34.977407 | 0.052285 |
| 24.0 | 0.038375 | 36.477531 | 0.049298 |
| 25.0 | -0.033348 | 37.611540 | 0.050457 |
| 26.0 | 0.019285 | 37.991151 | 0.060676 |
| 27.0 | 0.082559 | 44.955799 | 0.016436 |
| 28.0 | -0.000481 | 44.956035 | 0.022290 |
| 29.0 | 0.014995 | 45.186276 | 0.028221 |
| 30.0 | 0.000166 | 45.186304 | 0.037088 |
| 31.0 | 0.005648 | 45.219032 | 0.047656 |
| 32.0 | -0.053608 | 48.170804 | 0.033175 |
| 33.0 | -0.041521 | 49.943454 | 0.029572 |
| 34.0 | -0.088390 | 57.984990 | 0.006341 |
| 35.0 | -0.037059 | 59.400045 | 0.006170 |
| 36.0 | 0.024673 | 60.027922 | 0.007223 |
| 37.0 | -0.011843 | 60.172744 | 0.009385 |
| 38.0 | -0.000472 | 60.172975 | 0.012451 |
| 39.0 | 0.057219 | 63.560549 | 0.007761 |
| 40.0 | -0.073999 | 69.232214 | 0.002797 |

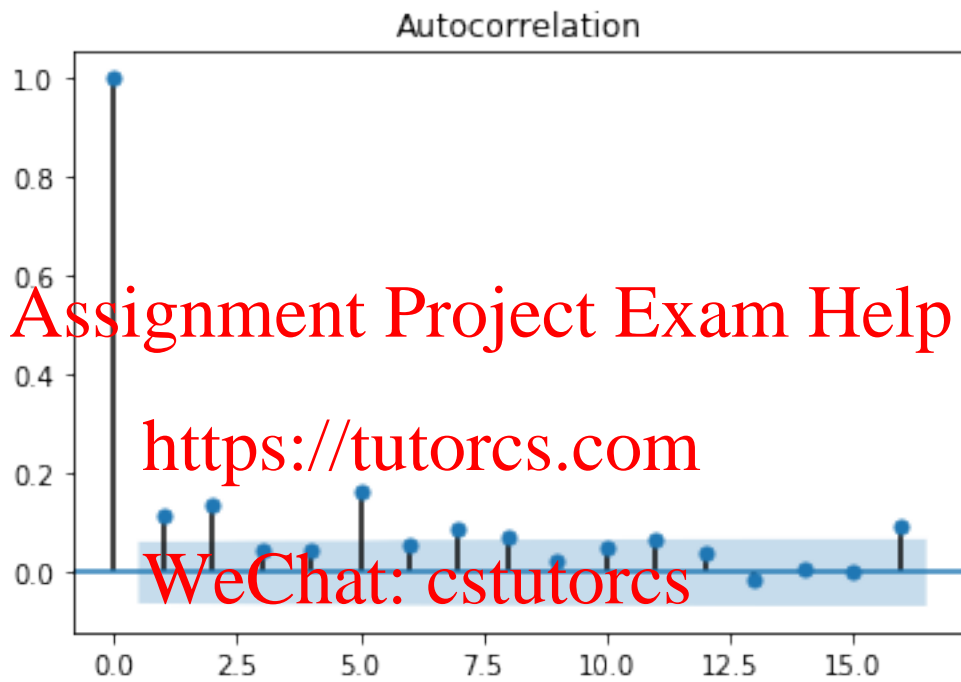
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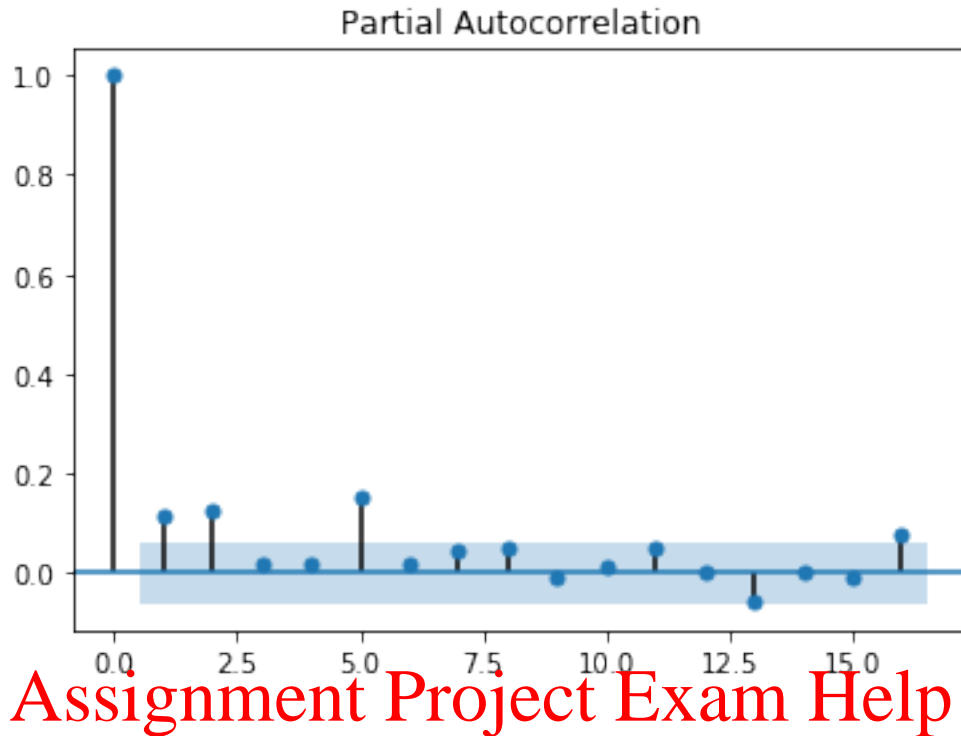
<https://tutorcs.com>

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C:\Users\rluck\anaconda3\lib\site-packages\statsmodels\tsa\stattools.py:572:
FutureWarning: fft=True will become the default in a future version of
statsmodels. To suppress this warning, explicitly set fft=False.
FutureWarning

```
[21]: #running ACF and PACF for R_squared  
dta =dta["R_squared"]  
sm.graphics.tsa.plot_acf(dta.values.squeeze(),lags=16)  
sm.graphics.tsa.plot_pacf(dta.values.squeeze(),lags=16)  
plt.show()
```





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[22]: `# Generating the Q statistics for A-squared`
`import numpy as np`
`r,q,p = sm.tsa.acf(dta.values.squeeze(), qstat=True)`
`data = np.c_[range(1,41), r[1:], q, p]`
`table = pd.DataFrame(data, columns=['lag', 'AC', 'Q', 'Prob(>Q)'])`
`print (table.set_index('lag'))`

| | AC | Q | Prob(>Q) |
|------|-----------|-----------|--------------|
| lag | | | |
| 1.0 | 0.116494 | 13.502985 | 2.381843e-04 |
| 2.0 | 0.137497 | 32.333061 | 9.527196e-08 |
| 3.0 | 0.044784 | 34.332681 | 1.685331e-07 |
| 4.0 | 0.043315 | 36.205192 | 2.625638e-07 |
| 5.0 | 0.163149 | 62.797123 | 3.206890e-12 |
| 6.0 | 0.055165 | 65.840403 | 2.905376e-12 |
| 7.0 | 0.088482 | 73.677864 | 2.660108e-13 |
| 8.0 | 0.072395 | 78.929848 | 8.025910e-14 |
| 9.0 | 0.026343 | 79.625935 | 1.917629e-13 |
| 10.0 | 0.051302 | 82.268635 | 1.800687e-13 |
| 11.0 | 0.065059 | 86.523037 | 7.976883e-14 |
| 12.0 | 0.041789 | 88.280113 | 1.061870e-13 |
| 13.0 | -0.014395 | 88.488810 | 2.716734e-13 |
| 14.0 | 0.010238 | 88.594485 | 6.988975e-13 |
| 15.0 | 0.001890 | 88.598091 | 1.809893e-12 |
| 16.0 | 0.092094 | 97.166798 | 1.173238e-13 |

```

17.0  0.037119   98.560264  1.643206e-13
18.0  0.072691  103.909558  4.233730e-14
19.0  0.076494  109.839392  8.533981e-15
20.0  0.020480  110.264870  1.757295e-14
21.0  0.111044  122.786785  2.195595e-16
22.0  0.050166  125.345073  1.847860e-16
23.0 -0.001220  125.346586  4.499962e-16
24.0  0.044374  127.352379  4.667582e-16
25.0  0.003717  127.366465  1.090264e-15
26.0  0.028585  128.200510  1.785587e-15
27.0  0.082601  135.172333  2.370793e-16
28.0  0.026304  135.880045  4.053453e-16
29.0 -0.005202  135.907755  8.989330e-16
30.0 -0.007790  135.969957  1.932061e-15
31.0  0.009146  136.055794  4.045732e-15
32.0  0.079309  142.516399  6.755564e-16
33.0  0.006202  142.555947  1.427039e-15
34.0 -0.039068  144.126945  1.632971e-15
35.0 -0.018614  144.483956  2.975030e-15
36.0 -0.038176  145.993749  3.443204e-15
37.0 -0.025142  146.639804  5.487456e-15
38.0 -0.043511  148.596627  5.273067e-15
39.0 -0.014017  148.799929  9.805069e-15
40.0 -0.042392  150.662265  9.670111e-15

```

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C:\Users\rluck\anaconda3\lib\site-packages\statsmodels\tsa\stattools.py:572:

FutureWarning: fft=True will become the default in a future version of statsmodels. To suppress this warning, explicitly set fft=False.

FutureWarning

8 ARCH(5) Answer to 3(d)

```

[72]: from arch import arch_model
      model = arch_model(dt, mean='Constant', vol='ARCH', p=5)
      x =model.fit()
      x

```

```

Iteration:      1,   Func. Count:      9,   Neg. LLF: 1641.4320830727252
Iteration:      2,   Func. Count:     21,   Neg. LLF: 1641.117179679314
Iteration:      3,   Func. Count:     32,   Neg. LLF: 1639.8618699736512
Iteration:      4,   Func. Count:     42,   Neg. LLF: 1639.2602976096668
Iteration:      5,   Func. Count:     52,   Neg. LLF: 1638.7165636155444
Iteration:      6,   Func. Count:     63,   Neg. LLF: 1638.5815616395487
Iteration:      7,   Func. Count:     73,   Neg. LLF: 1638.0031576294539
Iteration:      8,   Func. Count:     83,   Neg. LLF: 1637.590224502058
Iteration:      9,   Func. Count:     94,   Neg. LLF: 1637.5781186332947
Iteration:     10,   Func. Count:    104,   Neg. LLF: 1637.4668239040275

```

```

Iteration:      11,   Func. Count:      114,   Neg. LLF: 1637.3821507140146
Iteration:      12,   Func. Count:      123,   Neg. LLF: 1637.3674045891073
Iteration:      13,   Func. Count:      132,   Neg. LLF: 1637.366605883134
Iteration:      14,   Func. Count:      141,   Neg. LLF: 1637.3662139249632
Iteration:      15,   Func. Count:      150,   Neg. LLF: 1637.366197005517
Optimization terminated successfully.      (Exit mode 0)
      Current function value: 1637.3661963353218
      Iterations: 15
      Function evaluations: 151
      Gradient evaluations: 15

```

[72]:

Constant Mean - ARCH Model Results

```

=====
Dep. Variable:              R      R-squared:              -0.001
Mean Model:                Constant Mean    Adj. R-squared:              -0.001
Vol Model:                 ARCH      Log-Likelihood:              -1637.37
Distribution:              Normal      AIC:              3288.73
Method:                   Maximum Likelihood    BIC:              3323.03
                                           No. Observations:              992
Date: Thu Aug 20 2020      Df. Residuals:              985
Time: 17:11:52             Df. Model:              7
                               Mean Model

```

```

=====
coef      std err      t      P>|t|      95.0% Conf. Int.
-----
mu          0.0513   3.935e-02    1.303    0.192 [-2.584e-02,  0.128]

```

```

=====
                               Volatility Model
=====
coef      std err      t      P>|t|      95.0% Conf. Int.
-----
omega          1.0282    0.152    6.765  1.337e-11    [ 0.730,  1.326]
alpha[1]        0.0677   4.075e-02    1.662  9.650e-02    [-1.214e-02,  0.148]
alpha[2]        0.1424   6.086e-02    2.341  1.925e-02    [2.316e-02,  0.262]
alpha[3]        0.0270   2.455e-02    1.100    0.271 [-2.112e-02, 7.511e-02]
alpha[4]        0.0493   4.324e-02    1.140    0.254 [-3.547e-02,  0.134]
alpha[5]        0.1040   4.269e-02    2.437  1.481e-02    [2.037e-02,  0.188]
=====

```

```

Covariance estimator: robust
ARCHModelResult, id: 0x258550e2b08

```

9 3e: ARCH test

```

[62]: from statsmodels.stats.diagnostic import het_arch
      from statsmodels.compat import lzip

```

```
[59]: res = het_arch(dt.values,nlags =5)
      name = ['lm','lmpval','fval','fpval']
      lzip(name,res)
```

```
[59]: [('lm', 52.62649711315813),
      ('lmpval', 4.012739137878328e-10),
      ('fval', 11.050526049487171),
      ('fpval', 2.2665869070632531e-10)]
```

10 4d: ARCH test of standardised residuals

```
[74]: resid = x.resid/x.conditional_volatility
```

```
[75]: #4d: ARCH test
      res = het_arch(resid,nlags =5)
      name = ['lm','lmpval','fval','fpval']
      lzip(name,res)
```

```
[75]: [('lm', 1.841150196914932),
      ('lmpval', 0.870603058565487),
      ('fval', 0.36675536682138066),
      ('fpval', 0.8714901609636871)]
```

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11 GARCH(1,1) Answer to q4e

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```
[140]: #GARCH(1,1)
      model = arch_model(dt, mean='Zero', vol='GARCH', p=1, q=1)
      model.fit()
```

```
Iteration:      1,  Func. Count:      5,  Neg. LLF: 1635.7051459253014
Iteration:      2,  Func. Count:     11,  Neg. LLF: 1635.198292821203
Iteration:      3,  Func. Count:     17,  Neg. LLF: 1634.4683889348146
Iteration:      4,  Func. Count:     23,  Neg. LLF: 1634.142726804497
Iteration:      5,  Func. Count:     29,  Neg. LLF: 1633.820026751518
Iteration:      6,  Func. Count:     35,  Neg. LLF: 1633.7942934149069
Iteration:      7,  Func. Count:     41,  Neg. LLF: 1633.5845044893476
Iteration:      8,  Func. Count:     47,  Neg. LLF: 1633.5188557297743
Iteration:      9,  Func. Count:     53,  Neg. LLF: 1633.41918609823
Iteration:     10,  Func. Count:     58,  Neg. LLF: 1633.3859573686977
Iteration:     11,  Func. Count:     63,  Neg. LLF: 1633.380833530281
Iteration:     12,  Func. Count:     68,  Neg. LLF: 1633.3807015892412
Optimization terminated successfully.      (Exit mode 0)
      Current function value: 1633.380701081655
      Iterations: 12
      Function evaluations: 69
```

Gradient evaluations: 12

[140]:

Zero Mean - GARCH Model Results

```
=====
Dep. Variable:          R    R-squared:          0.000
Mean Model:             Zero Mean  Adj. R-squared:      0.001
Vol Model:              GARCH    Log-Likelihood:    -1633.38
Distribution:           Normal    AIC:             3272.76
Method:                Maximum Likelihood  BIC:             3287.46
                               No. Observations:      992
Date:                  Sat, Jul 25 2020  Df Residuals:    989
Time:                  07:57:24    Df Model:         3
                               Volatility Model
=====
```

```
=====
              coef      std err          t      P>|t|     95.0% Conf. Int.
-----
omega          0.0722   3.410e-02      2.118   3.419e-02 [5.385e-03,  0.139]
alpha[1]        0.0780   2.399e-02      3.252   1.146e-03 [3.100e-02,  0.125]
beta[1]         0.8805   3.299e-02     26.691   5.933e-157 [ 0.816,  0.945]
=====
```

Covariance estimator: robust
ARCHModelResult, id: 0x1ec7e194488

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[]:

12 GARC(2,1), GARCH(1,2) and GARCH(2,2) Answer to q4f

[141]:

```
#GARCH (2,1)
model = arch_model(dt, mean='Zero', vol='GARCH', p=2, q=1)
model.fit()
```

```
Iteration:      1,  Func. Count:      6,  Neg. LLF: 1634.4763048908176
Iteration:      2,  Func. Count:     14,  Neg. LLF: 1634.3114071546615
Iteration:      3,  Func. Count:     21,  Neg. LLF: 1633.898626097601
Iteration:      4,  Func. Count:     28,  Neg. LLF: 1633.6129513377468
Iteration:      5,  Func. Count:     35,  Neg. LLF: 1633.4056492048512
Iteration:      6,  Func. Count:     42,  Neg. LLF: 1633.20362402841
Iteration:      7,  Func. Count:     49,  Neg. LLF: 1633.1525418386232
Iteration:      8,  Func. Count:     56,  Neg. LLF: 1633.0365456637537
Iteration:      9,  Func. Count:     63,  Neg. LLF: 1632.964882807908
Iteration:     10,  Func. Count:     70,  Neg. LLF: 1632.9547557375658
Iteration:     11,  Func. Count:     76,  Neg. LLF: 1632.954485222734
Iteration:     12,  Func. Count:     82,  Neg. LLF: 1632.9543347483414
Optimization terminated successfully.      (Exit mode 0)
Current function value: 1632.9543338562553
Iterations: 12
```

Function evaluations: 83
Gradient evaluations: 12

[141]:

Zero Mean - GARCH Model Results

| | | | | | |
|----------------|--------------------|-------------------|----------|-----------|---------------------|
| Dep. Variable: | R | R-squared: | 0.000 | | |
| Mean Model: | Zero Mean | Adj. R-squared: | 0.001 | | |
| Vol Model: | GARCH | Log-Likelihood: | -1632.95 | | |
| Distribution: | Normal | AIC: | 3273.91 | | |
| Method: | Maximum Likelihood | BIC: | 3293.51 | | |
| | | No. Observations: | 992 | | |
| Date: | Sat, Jul 25 2020 | Df Residuals: | 988 | | |
| Time: | 07:57:24 | Df Model: | 4 | | |
| | Volatility Model | | | | |
| ===== | | | | | |
| | coef | std err | t | P> t | 95.0% Conf. Int. |
| ----- | | | | | |
| omega | 0.0814 | 4.475e-02 | 1.819 | 6.890e-02 | [-6.304e-03, 0.169] |
| alpha[1] | 0.0521 | 3.809e-02 | 1.367 | 0.172 | [-2.258e-02, 0.127] |
| alpha[2] | 0.0345 | 4.683e-02 | 0.736 | 0.462 | [-5.733e-02, 0.126] |
| beta[1] | 0.8668 | 4.806e-02 | 18.038 | 9.771e-73 | [0.773, 0.961] |
| ===== | | | | | |

Covariance estimator: robust
ARCHModelResult, id: 0x1ec7e0fe388

[142]:

```
#GARCH (1,2)
model = arch_model(df, mean='t-1', vol='GARCH', p=1, q=2)
model.fit()
```

```
Iteration:      1,  Func. Count:      6,  Neg. LLF: 1637.5020935283383
Iteration:      2,  Func. Count:     14,  Neg. LLF: 1637.3630476546887
Iteration:      3,  Func. Count:     21,  Neg. LLF: 1635.5390948880922
Iteration:      4,  Func. Count:     29,  Neg. LLF: 1635.4513712241176
Iteration:      5,  Func. Count:     36,  Neg. LLF: 1634.9403158235568
Iteration:      6,  Func. Count:     43,  Neg. LLF: 1633.881149795298
Iteration:      7,  Func. Count:     49,  Neg. LLF: 1633.7161883728404
Iteration:      8,  Func. Count:     55,  Neg. LLF: 1633.3916902708702
Iteration:      9,  Func. Count:     62,  Neg. LLF: 1633.3817391556056
Iteration:     10,  Func. Count:     69,  Neg. LLF: 1633.38101239148
Iteration:     11,  Func. Count:     76,  Neg. LLF: 1633.3807015808443
Optimization terminated successfully.      (Exit mode 0)
Current function value: 1633.3807015474256
Iterations: 11
Function evaluations: 76
Gradient evaluations: 11
```

[142]:

Zero Mean - GARCH Model Results

```
=====
Dep. Variable:          R    R-squared:          0.000
Mean Model:            Zero Mean    Adj. R-squared:          0.001
Vol Model:             GARCH    Log-Likelihood:        -1633.38
Distribution:          Normal    AIC:                3274.76
Method:               Maximum Likelihood    BIC:                3294.36
                               No. Observations:          992
Date:                 Sat, Jul 25 2020    Df Residuals:          988
Time:                 07:57:25    Df Model:              4
                               Volatility Model
=====
```

```
=====
              coef      std err          t      P>|t|     95.0% Conf. Int.
-----
omega          0.0722   3.493e-02     2.068   3.862e-02 [3.782e-03, 0.141]
alpha[1]        0.0780   2.386e-02     3.271   1.072e-03 [3.127e-02, 0.125]
beta[1]         0.8805    0.175     5.039   4.685e-07 [ 0.538, 1.223]
beta[2]         4.5110e-14    0.163   2.775e-13     1.000 [ -0.319, 0.319]
=====
```

Covariance estimator: robust

ARCHModelResult, id: 0x1ec7e16f6c8

[143]:

```
#GARCH (2,2)
model = arch_model(dt, mean='Zero', vol='GARCH', p=2, q=2)
model.fit()
```

```
Iteration:      1,  Func. Count:      7,  Neg. LLF: 1633.8456883994468
Iteration:      2,  Func. Count:     16,  Neg. LLF: 1632.0020951730494
Iteration:      3,  Func. Count:     26,  Neg. LLF: 1631.9962682958353
Iteration:      4,  Func. Count:     34,  Neg. LLF: 1631.7125855588226
Iteration:      5,  Func. Count:     43,  Neg. LLF: 1631.7070695589769
Iteration:      6,  Func. Count:     51,  Neg. LLF: 1631.5885046883052
Iteration:      7,  Func. Count:     60,  Neg. LLF: 1631.5882871287859
Iteration:      8,  Func. Count:     68,  Neg. LLF: 1631.5727647406475
Iteration:      9,  Func. Count:     75,  Neg. LLF: 1631.5723289793957
```

Optimization terminated successfully. (Exit mode 0)

Current function value: 1631.5723279871504

Iterations: 9

Function evaluations: 76

Gradient evaluations: 9

[143]:

Zero Mean - GARCH Model Results

```
=====
Dep. Variable:          R    R-squared:          0.000
Mean Model:            Zero Mean    Adj. R-squared:          0.001
Vol Model:             GARCH    Log-Likelihood:        -1631.57
=====
```



```

Distribution:           Normal      AIC:           3273.14
Method:               Maximum Likelihood  BIC:           3297.64
                                     No. Observations:   992
Date:                 Sat, Jul 25 2020  Df Residuals:   987
Time:                 07:57:25      Df Model:       5
                                     Volatility Model

```

| | coef | std err | t | P> t | 95.0% Conf. Int. |
|----------|--------|-----------|-------|-----------|-------------------------|
| omega | 0.1311 | 7.046e-02 | 1.861 | 6.272e-02 | [-6.959e-03, 0.269] |
| alpha[1] | 0.0393 | 2.745e-02 | 1.432 | 0.152 | [-1.448e-02, 9.311e-02] |
| alpha[2] | 0.0997 | 4.896e-02 | 2.036 | 4.174e-02 | [3.730e-03, 0.196] |
| beta[1] | 0.2862 | 0.166 | 1.723 | 8.491e-02 | [-3.938e-02, 0.612] |
| beta[2] | 0.4996 | 0.140 | 3.577 | 3.479e-04 | [0.226, 0.773] |

```

Covariance estimator: robust
ARCHModelResult, id: 0x1ec7e1fcd48

```

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