# ECON7350: Applied Econometrics for Macroeconomics and Finance

#### Tutorial 11: Multivariate Processes - I/II

At the end of this tutorial you should be able to:

- Use R to construct an adequate set of VAR(p) models;
- Use R to forecast one of the variables generated by a VAR(p) process;
- Derive a structural VAR from a reduced form VAR using the Cholesky factorisation;
- · ASSI Summent or displecations ix amanded in SVAR;
- Use R to obtain inference on Granger causality.

# Problems with Solutions

The data file morey demissive contains quarterly observations for the following variables from 1950(11) about CSTULIOTCS

- RGDP: real US GDP;
- GDP: nominal GDP;
- M2: money supply;
- Tb3mo: three-month rate on US treasury bills.

Using this sample, we will work with the following variables:

- Log Real GDP:  $\operatorname{lrgdp}_t = \operatorname{ln} \operatorname{RGDP}_t$ ;
- GDP Deflator:  $price_t = GDP_t/RGDP_t$ ;
- Log Real Money Supply:  $lrm2_t = ln(M2_t/price_t)$ ;
- Short-term Interest Rate:  $rs_t = tb3mo_t$ .
- 1. Consider forecasting  $\operatorname{lrgdp}_t$  using a VAR(p) model of the multivariate process  $\{\mathbf{x}_t\}$ , where  $\mathbf{x}_t = (\operatorname{lrgdp}_t, \operatorname{lrm} 2_t, \operatorname{rs}_t)'$ .
  - (a) Construct and adequate set of VAR(p) models.

**Solution** For this tutorial we need the following packages.

```
library(zoo)
library(vars)
library(pracma)
```

The package vars provides the functionality we will use to work with VAR(p) models. The package pracma provides the function perms, which generates all possible permutations of the elements of a given vector. This is used in Question 2 to examine all possible orderings of the variables in the VAR.

Next, we load the data and generate required variables.

```
mydata <- read.delim("money_dem.csv", header = TRUE, sep = ",")

date <- as.yearqtr(mydata$DATE)
lrgdp <- log(mydata$RGDP)
price <- mydata$GDP/mydata$RGDP
lrm2 <- log(mydata$M2) - log(price)
rs <- mydata$TB3mo
x <- Aigdirghniment) Project Exam Help</pre>
```

To construct an adequate set of VAR(p) models for forecasting, we will consider VARs with  $p = 1, \dots, 20$ . Note that the VAR function provided by the vars package does not allow particles input UKCONGS work must be as the VAR(0) is a very special case (and generally not of interest in time-series applications).

The AIC and BIC clearly agree on p = 2, 3, 4 as the top three specifications. The remaining specifications appear to be quite a bit inferior, so we proceed with an adequate set consisting of the three specifications above.

```
adq_set_var <- as.matrix(ic_var[2:4,])
adq_idx_var <- c(2:4)</pre>
```

The serial.test function provides several tests for VAR residual autocorrelation. We will focus on the LM test by setting type = "BG", but other tests are just as

valid.

```
nmods <- length(adq idx var)</pre>
for (i in 1:nmods)
  p < adq idx var[i]</pre>
  print(paste0("Checking VAR(", p, ")"))
  print(serial.test(VAR_est[[p]], type = "BG"))
}
## [1] "Checking VAR(20)"
##
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR est[[p]]
## Chi-squared = 55.601, df = 45, p-value = 0.1337
##
   [1] "Checking VAR(20)"
##
##
   *Aussignment Project Exam Help
##
##
## data: Residuals of VAR object VAR_est[[p]]
## Chi-squared = 55.601, df = 45, p-value = 0.1337
            nups://tutorcs.com
## [1] "Checking VAR(20)"
##
   Breusch-GWre CMhat: CStutorcs
##
##
## data: Residuals of VAR object VAR est[[p]]
## Chi-squared = 55.601, df = 45, p-value = 0.1337
Unfortunately, estimated residual autocorrelations appear to be quite high for all
```

three models. This is a concern, so we proceed by checking all 20 VARs we have estimated so far.

```
for (p in 1:20)
{
  print(paste0("Checking VAR(", p, ")"))
  print(serial.test(VAR_est[[p]], type = "BG"))
}
## [1] "Checking VAR(1)"
##
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR est[[p]]
## Chi-squared = 189.99, df = 45, p-value < 2.2e-16
##
```

```
## [1] "Checking VAR(2)"
##
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR est[[p]]
## Chi-squared = 96.62, df = 45, p-value = 1.239e-05
##
## [1] "Checking VAR(3)"
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR_est[[p]]
## Chi-squared = 88.246, df = 45, p-value = 0.0001246
## [1] "Checking VAR(4)"
##
##
   Breusch-Godfrey LM test
##
## data: Seisidralane MR Project Exama Help
##
## [1] "Checking VAR(5)",
             https://tutorcs.com
##
   Breusch-Godfrey LM test
##
## data: Resolutes of WAR tobject WAR test [p]
## Chi-squared = 83.481, at = 45, p-value = 0.0004291
##
## [1] "Checking VAR(6)"
##
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR_est[[p]]
## Chi-squared = 66.097, df = 45, p-value = 0.02188
##
## [1] "Checking VAR(7)"
##
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR est[[p]]
## Chi-squared = 74.501, df = 45, p-value = 0.003709
##
## [1] "Checking VAR(8)"
##
##
   Breusch-Godfrey LM test
```

```
##
## data: Residuals of VAR object VAR_est[[p]]
## Chi-squared = 60.642, df = 45, p-value = 0.05967
##
   [1] "Checking VAR(9)"
##
##
##
   Breusch-Godfrey LM test
##
## data:
        Residuals of VAR object VAR est[[p]]
## Chi-squared = 60.593, df = 45, p-value = 0.06017
##
## [1] "Checking VAR(10)"
##
##
    Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR est[[p]]
## Chi-squared = 62.07, df = 45, p-value = 0.04646
##
   <sup>[1</sup>A"$signMeh"t Project Exam Help
##
##
##
   Breusch-Godfrey LM test
         Respitting St. Wat bot Ot On estom
## Chi-squared = 58.862, df = 45, p-value = 0.08044
##
## [1] "Check We Chat: cstutorcs
##
   Breusch-Godfrey LM test
##
##
## data: Residuals of VAR object VAR est[[p]]
## Chi-squared = 59.21, df = 45, p-value = 0.07596
##
## [1] "Checking VAR(13)"
##
##
    Breusch-Godfrey LM test
##
## data:
         Residuals of VAR object VAR est[[p]]
## Chi-squared = 58.196, df = 45, p-value = 0.08961
##
   [1] "Checking VAR(14)"
##
##
   Breusch-Godfrey LM test
##
##
## data:
        Residuals of VAR object VAR est[[p]]
## Chi-squared = 47.223, df = 45, p-value = 0.3819
```

```
##
##
   [1] "Checking VAR(15)"
##
##
   Breusch-Godfrey LM test
##
         Residuals of VAR object VAR est[[p]]
  Chi-squared = 51.487, df = 45, p-value = 0.2348
##
   [1] "Checking VAR(16)"
##
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR est[[p]]
  Chi-squared = 42.506, df = 45, p-value = 0.5782
##
   [1] "Checking VAR(17)"
##
##
##
   Breusch-Godfrey LM test
                   ient Project Exam Help
##
  Chi-squared = 49, df = 45, p-value = 0.3157
   [1] "Checkintty AS18 / tutorcs.com
##
##
   Breusch-Godfrey LM test
##
##
         Residuals of VAR object VAR_est[[p]]
  Chi-squared = 46.546, df = 45, p-value = 0.4085
##
##
   [1] "Checking VAR(19)"
##
##
##
   Breusch-Godfrey LM test
##
## data: Residuals of VAR object VAR est[[p]]
  Chi-squared = 60.162, df = 45, p-value = 0.06476
##
##
   [1] "Checking VAR(20)"
##
##
   Breusch-Godfrey LM test
##
         Residuals of VAR object VAR est[[p]]
## Chi-squared = 55.601, df = 45, p-value = 0.1337
```

White noise residuals are rejected for all specifications with  $p \leq 7$ , which indicates that we need to consider higher lag orders. For  $p \geq 8$ , both AIC and BIC clearly agree that lower p values are preferred. We will proceed with p = 8, 9, 10 as the

adequate set.

```
adq_set_var <- as.matrix(ic_var[8:10,])
adq_idx_var <- c(8:10)</pre>
```

(b) How many intercept and slope coefficients need to be estimated for each VAR(p) in the adequate set?

**Solution** We can compute the total number of coefficients using the simple formula k = n(1 + np).

(c) Check the stability of each estimated VAR(p) model. How does this affect forecasting?

**Solution** The vars package provides a handy function roots to ascertain the stability of an estimated VAR(p). In fact, it generates estimates of the absolute values of the *eigenvalues* of the companion form. Unfortunately, it does not provide confidence intervals for the estimated eigenvalues.

Warning: the vars package also has a function called stability, but this is not related to the roots of the characteristic equation (instead, it is concerned with structural breaks in the process).

```
nmods <- length(adq_idx_var)
for (i in 1:nmods)
{
   p <- adq_idx_var[i]</pre>
```

```
## [1] "VAR(8): Maximum absolute eigenvalue is 1.00159063636763"
## [1] "VAR(9): Maximum absolute eigenvalue is 1.00063351477022"
## [1] "VAR(10): Maximum absolute eigenvalue is 1.00056830228862"
```

We find that the largest eigenvalue is approximately 1 in absolute value—i.e., the smallest root is close to a unit root. We should be aware that forecasts will be less reliable at longer horizons. Do we want to consider imposing an explicit restriction of an exact unit root? We will explore this in Tutorial 12!

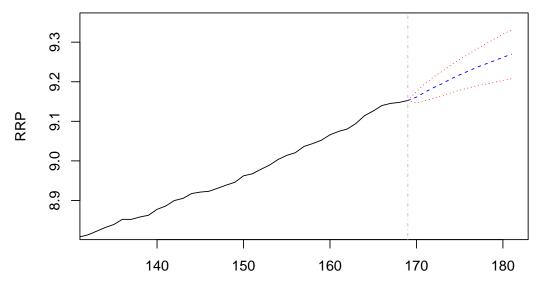
(d) Forecast  $\operatorname{lrgdp}_t$  for 12 quarters past the end of the sample. Plot the point estimates along with 95% predictive intervals. Interpret the results.

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Solution We can use the predict function to generate forecasts; the function plot will then automatically produce 95% predictive intervals. Unfortunately, these intervals only account for forecast uncertainty, but not estimation uncertainty (i.e., parameter estimates treated as given in deriving the predictive intervals).

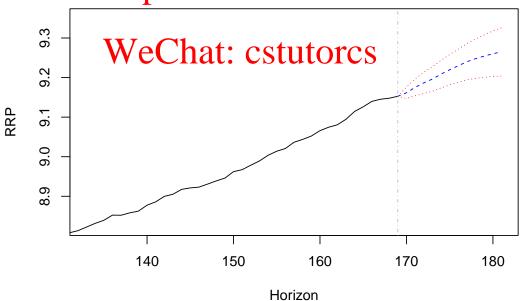
```
hrz = 12
VAR_fcst <- 1 We Chat: cstutores
xlim <- c(length(date) - 3 * hrz,</pre>
               length(date) + hrz)
ylim <- c(lrgdp[xlim[1]],</pre>
          max(lrgdp) + 0.2)
for (i in 1:nmods)
  p <- adq idx var[i]</pre>
  VAR_fcst[[i]] <- predict(VAR_est[[p]],</pre>
                            n.ahead = hrz)
  plot(VAR_fcst[[i]], names = "lrgdp",
           xlim = xlim, ylim = ylim,
           main = "Forecast for Log Real GDP",
           xlab = "Horizon",
           ylab = "RRP")
}
```

#### **Forecast for Log Real GDP**

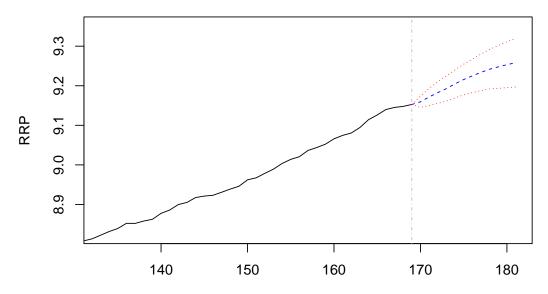


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#### **Forecast for Log Real GDP**



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Forecasts for the three VAR specifications look qualitatively similar. Also, to note is that the near unit post estimated for each VAR places not seem to be of any consequence in terms of forecasts up to 12 quarters ahead—they are still quite accurate in the sense of having relatively small predictive intervals (but keeping in mind that tese do not take into account estimate uncertainty).

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- 2. Analyse the dynamic relationships between  $lrgdp_t$ ,  $lrm2_t$  and  $rs_t$ . For all VAR specifications relevant to this question please use p = 8.
  - (a) Using the Cholesky decomposition, compute the IRFs for all the possible orderings of the system and study the responses. Are the responses sensitive to ordering? Choose the most reasonable ordering and explain your answer.

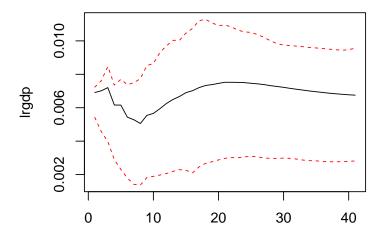
**Solution** We compare IRFs of six orderings, which are obtained from all possible permutations of  $\mathbf{x}_t$ . In R, we can do this by employing the funcation perms from the pracma package. Then, we compute the IRFs using the irf function within nested for loops.

```
orders <- perms(1:3)
vnames <- c("lrgdp", "lrm2", "rs")
for (i in 1:3)</pre>
```

```
{
  for (j in 1:3)
  {
   for (k in 1:nrow(orders))
    {
     title_i_j_k <- paste0("Response of ",</pre>
                           vnames[i],
                           " to a shock in ",
                           vnames[j],
                           "; x = (",
                           paste0(vnames[orders[k,]],
                                 collapse = ", "),
                           ") "")
      irf_i_j_k <- irf(VAR(x[,orders[k,]], 8),</pre>
                         n.ahead = 40,
                         response = vnames[i],
                         impulse = vnames[j],
                                         Exam Help
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     plot(irf_i_j_k, main = title_i_j_k)
   }
            https://tutorcs.com
  }
}
```

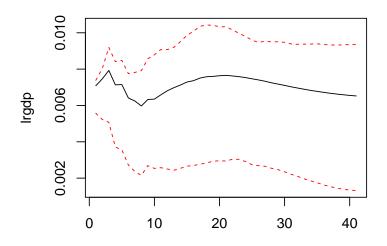
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Response of Irgdp to a shock in Irgdp; x = (rs, Irm2, Irgdp)'



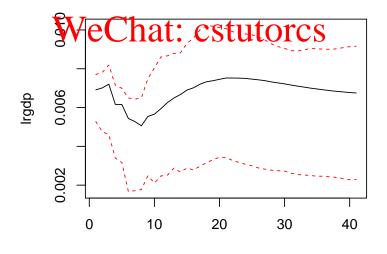
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Response of Irgdp to a shock in Irgdp; x = (rs, Irgdp, Irm2)'



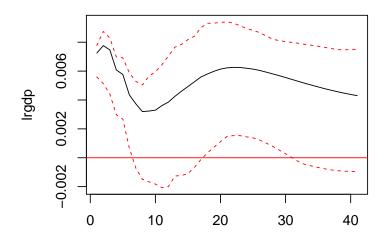
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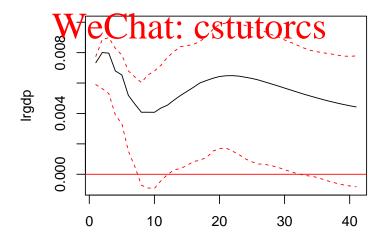
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Response of Irgdp to a shock in Irgdp; x = (Irm2, Irgdp, rs)'



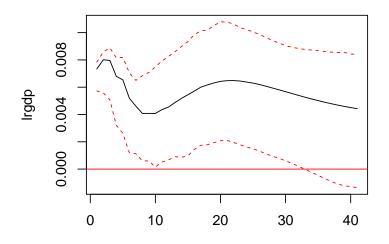
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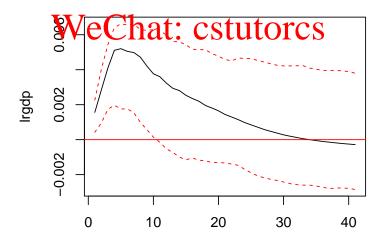
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Response of Irgdp to a shock in Irgdp; x = (Irgdp, rs, Irm2)'



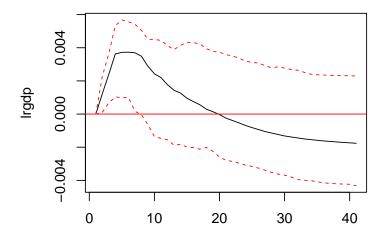
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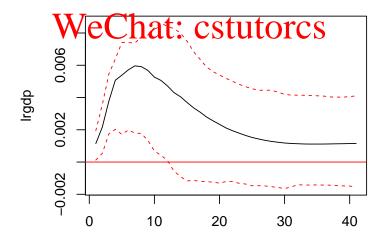
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Response of Irgdp to a shock in Irm2; x = (rs, Irgdp, Irm2)'



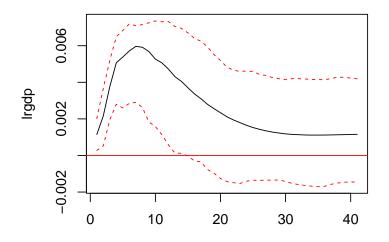
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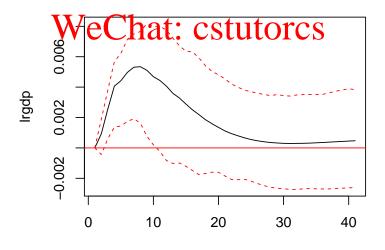
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Response of Irgdp to a shock in Irm2; x = (Irm2, Irgdp, rs)'



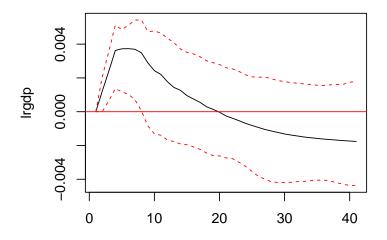
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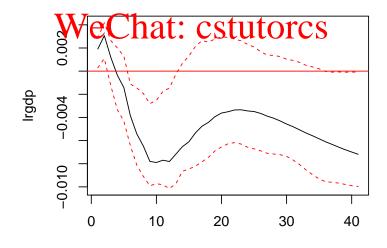
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Response of Irgdp to a shock in Irm2; x = (Irgdp, rs, Irm2)'



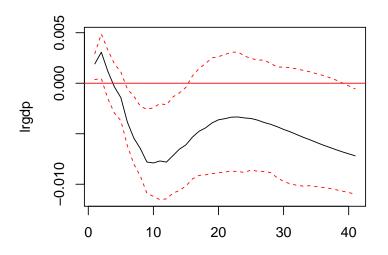
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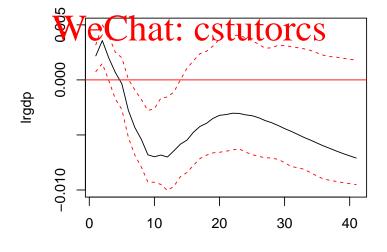
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Response of Irgdp to a shock in rs; x = (rs, Irgdp, Irm2)'



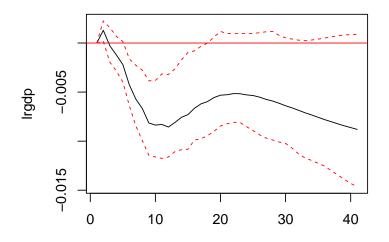
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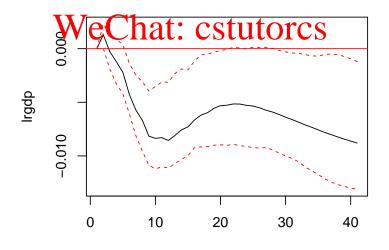
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Response of Irgdp to a shock in rs; x = (Irm2, Irgdp, rs)'



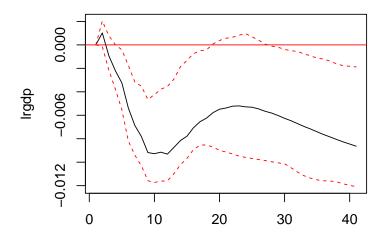
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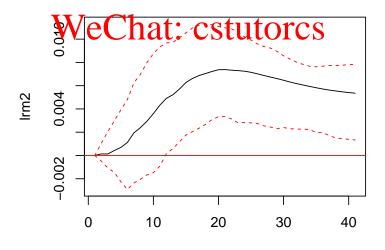
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Response of Irgdp to a shock in rs; x = (Irgdp, rs, Irm2)'



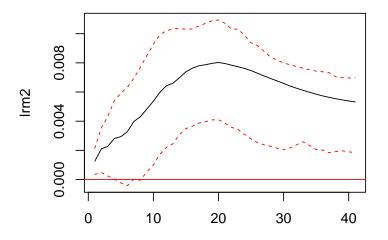
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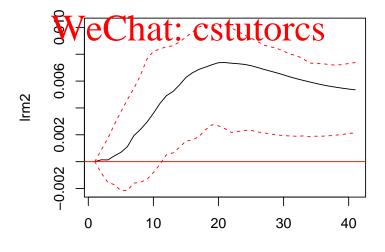
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Response of Irm2 to a shock in Irgdp; x = (rs, Irgdp, Irm2)'



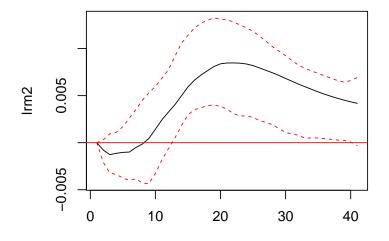
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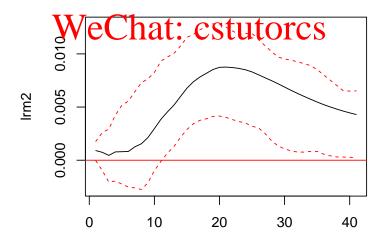
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Response of Irm2 to a shock in Irgdp; x = (Irm2, Irgdp, rs)'



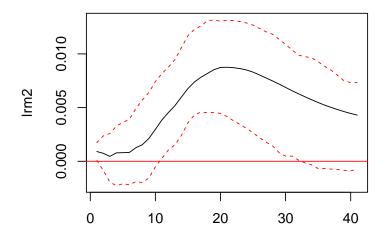
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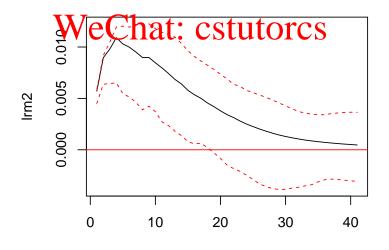
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Response of Irm2 to a shock in Irgdp; x = (Irgdp, rs, Irm2)'



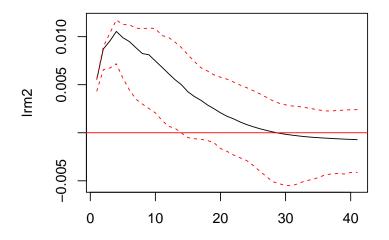
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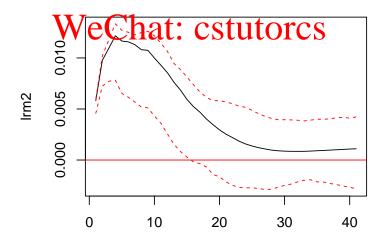
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Response of Irm2 to a shock in Irm2; x = (rs, Irgdp, Irm2)'



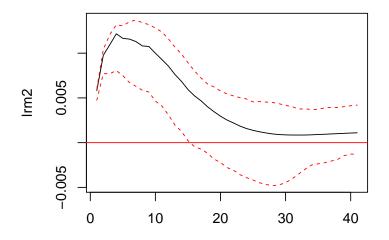
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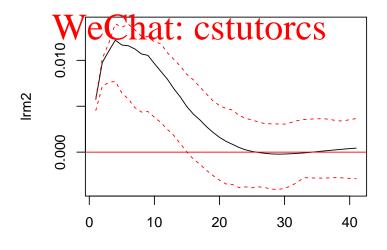
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Response of Irm2 to a shock in Irm2; x = (Irm2, Irgdp, rs)'



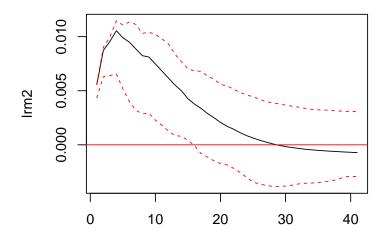
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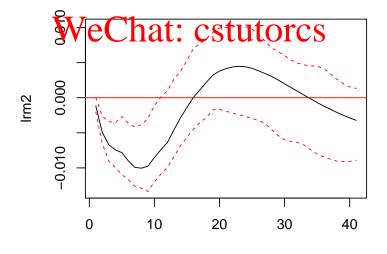
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Response of Irm2 to a shock in Irm2; x = (Irgdp, rs, Irm2)'

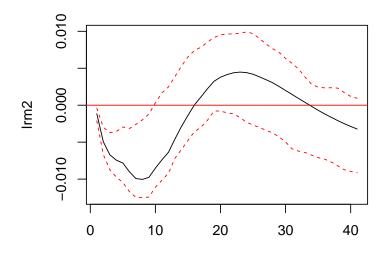


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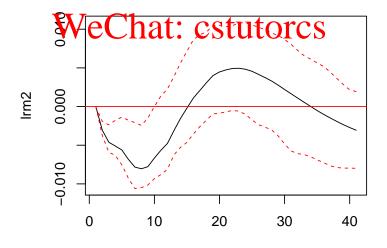


Response of Irm2 to a shock in rs; x = (rs, Irgdp, Irm2)'



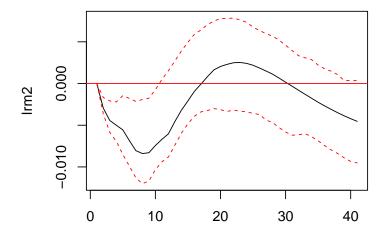
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https://tutorcs.com Response of Irm2 to a shock in rs; x = (Irm2, rs, Irgdp)'



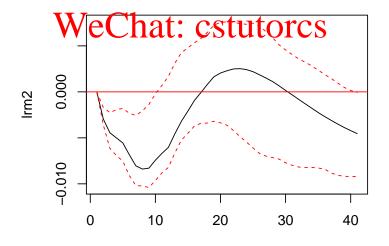
95 % Bootstrap CI, 100 runs

Response of Irm2 to a shock in rs; x = (Irm2, Irgdp, rs)'



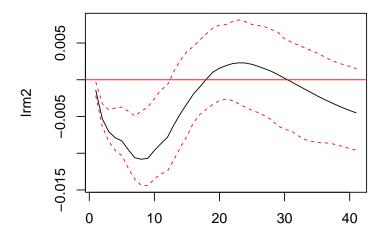
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https://tutorcs.com Response of Irm2 to a snock in rs; x = (Irgdp, Irm2, rs)'



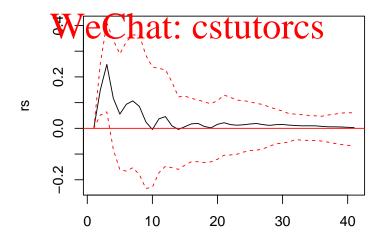
95 % Bootstrap CI, 100 runs

Response of Irm2 to a shock in rs; x = (Irgdp, rs, Irm2)'



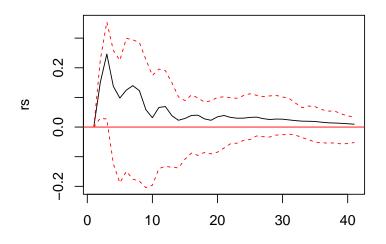
#### Assignment Project Exam Help

https://tutorcs.com Response of rs to a shock in Irgdp; x = (rs, Irm2, Irgdp)'



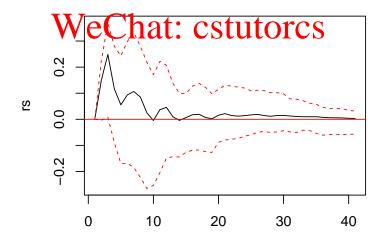
95 % Bootstrap CI, 100 runs

Response of rs to a shock in Irgdp; x = (rs, Irgdp, Irm2)'



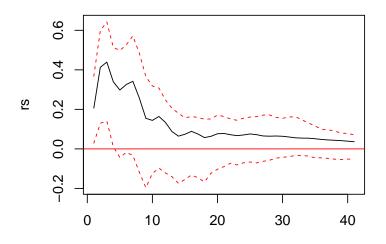
#### Assignment Project Exam Help

https://tutorcs.com Response of rs to a shock in Irgdp; x = (Irm2, rs, Irgdp)'



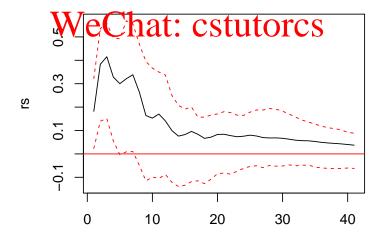
95 % Bootstrap CI, 100 runs

Response of rs to a shock in Irgdp; x = (Irm2, Irgdp, rs)'



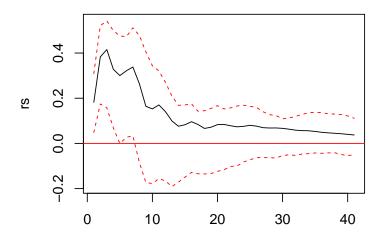
# Assignment Project Exam Help

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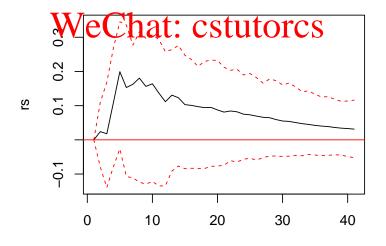
95 % Bootstrap CI, 100 runs

Response of rs to a shock in Irgdp; x = (Irgdp, rs, Irm2)'



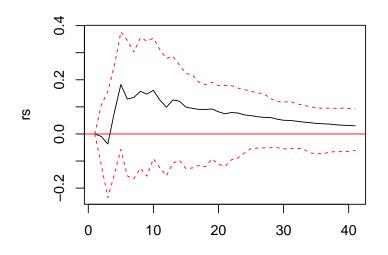
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https://tutorcs.com Response of rs to a shock in Irm2; x = (rs, Irm2, Irgdp)'



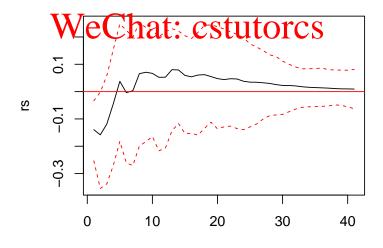
95 % Bootstrap CI, 100 runs

Response of rs to a shock in Irm2; x = (rs, Irgdp, Irm2)'



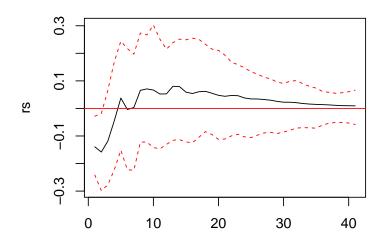
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https://tutorcs.com Response of rs to a shock in Irm2; x = (Irm2, rs, Irgdp)'



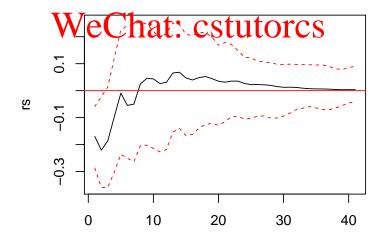
95 % Bootstrap CI, 100 runs

Response of rs to a shock in Irm2; x = (Irm2, Irgdp, rs)'



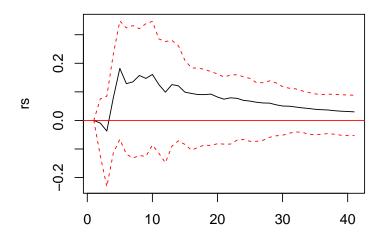
# Assignment Project Exam Help

https://tutorcs.com Response of rs to a shock in Irm2; x = (Irgap, Irm2, rs)



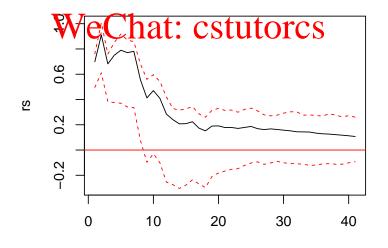
95 % Bootstrap CI, 100 runs

Response of rs to a shock in Irm2; x = (Irgdp, rs, Irm2)'



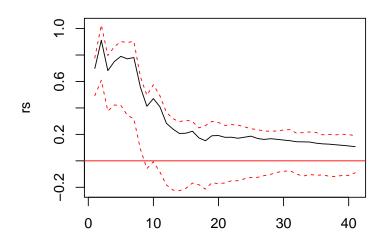
# Assignment Project Exam Help

https://tutorcs.com Response of rs to a shock in rs, x = (rs, Irm2, Irgdp)'



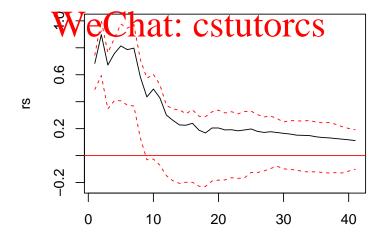
95 % Bootstrap CI, 100 runs

Response of rs to a shock in rs; x = (rs, lrgdp, lrm2)'



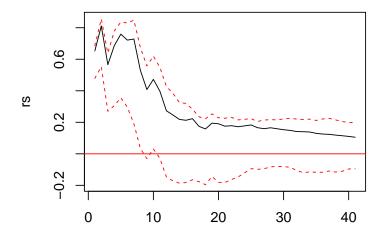
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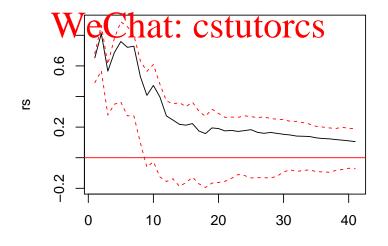
95 % Bootstrap CI, 100 runs

Response of rs to a shock in rs; x = (Irm2, Irgdp, rs)'



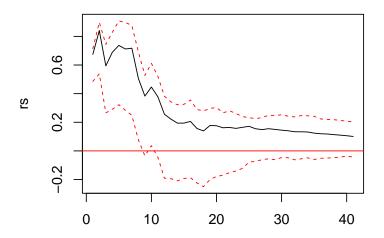
#### Assignment Project Exam Help

https://tutorcs.com Response of rs to a shock in rs, x = (Irgop, Irm2, rs)'



95 % Bootstrap CI, 100 runs

Response of rs to a shock in rs; x = (lrgdp, rs, lrm2)'



#### Assignment Project Exam Help

The following are some obsevations that stand out.

- i (dlrgdp<sub>t</sub>, dlibt<sub>t</sub>) vs. (tlrg0) CsS dCa2). We observe similar patterns in impulse responses, but note that the response of interest rates to a change in money supply is fairly different within the two orderings. When money supply is overed prior contemporare rates, there is a significant contemporaneous response of interest rates to a change in money supply; no significant response is observed in the alternative case (money supply prior to interest rates).
- ii  $(dlrgdp_t, dlrm2_t, drs_t)$  vs.  $(dlrm2_t, drs_t, dlrgdp_t)$ : These two orderings exhibit patterns that are very similar to IRFs in Part (i). However, the response of interest rates to a change in GDP is larger when GDP is ordered prior to interest rates, than the other way around.
- 1.  $(drs_t, dlrgdp_t, dlrm2_t)$  vs.  $(drs_t, dlrm2_t, dlrgdp_t)$ : The IRFs are very similar for these two orderings and do not show any significant sensitivity to switching the order of GDP and money supply when interest rates or ordered first.

Data is not informative on which ordering is most suitable, so we need to draw on economic theory if we are to focus on one particular ordering. There are a number of ways to reason in the present setting. A conventional approach used in analysing dynamic responses to monetary policy shocks (e.g., interest rates) separates all non-policy variables into fast-moving and slow-moving variables. Then, all slow-moving variables are ordered prior to the interest rate variable and all fast-moving variables are placed after.

Typically, fast-moving variables are taken to be financial indicators and asset

prices, whereas *slow*-moving variables are those related real economic activity. In the literature, it has been shown that under reasonable conditions the particular ordering *within* groups of slow-moving and fast-moving variables is not important for the purpose of drawing inference on the response of economic variables to a change in interest rates.

In our setting, one might argue that GDP is certainly a *slow*-moving variable, so it should definitely be ordered before interest rates. It is also reasonable to assume that GDP does not respond to money supply within one quarter. It may be less clear on how to classify money supply. Fortunately, the comparison of IRFs carried out in Part (i) suggests that it may not matter much on whether money supply is ordered prior to interest rates or vice-versa.

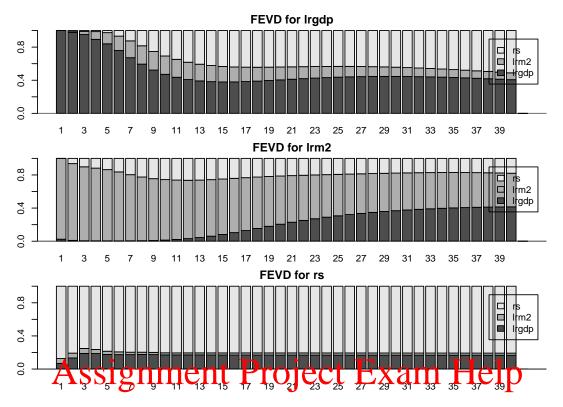
If we focus on two orderings that put drs last, i.e.,  $(dlrgdp_t, dlrm2_t, drs_t)$  and  $(dlrm2_t, dlrgdp_t, drs_t)$ , we observe that (as theory suggests) all responses to interest rates are indistinguishable, and the IRFs for the other impulses / responses are also "qualitatively" the same. Therefore, inference drawn based on these IRFs may be considered to be robust to changes in the ordering of GDP and money supply (which is reassuring in case our intuition that GDP does not respond to money supply within one quarter fails).

This is the type of approach macroeconomists frequently undertake in policy analysis. One word of caution: it is tempting to look at the IRFs and choose an

ordering (or more generally set of identifying restrictions) based on what yields the "most reasonable" results. This, however, is circular reasoning—by undertaking such an approach we are simply finding "the right method" that confirms what we hypothesised before seeing the data. Such an approach has been shown to lead to very dangerous concusional. CSTUTOICS

(b) Using the ordering chosen in Part (a), compute the FEVDs and comment on your findings.

**Solution** For this part we also fix the order to be  $(\lg dp_t, \operatorname{lrm} 2_t, \operatorname{rs}_t)$ . The fevd function only computes decompositions at the estimated values of the VAR parameters and does not provide confidence intervals, unfortunately.



It is useful to view forecast error variance intuitively as capturing unpredictable fluctuations in https://projections.cfchartimated FEVDs are the following.

- 1. Most of short-term fluctuations in GDP are explained by the GDP specific shock, but the incortance of money supply shocks begins to materialise after about one year, and interest rate shocks appears to play a significant role after around two years. In the long-run, about 50% of the fluctuations in Log Real GDP are attributed to shocks in interest rates.
- 2. Similar to GDP, most of short-term fluctuations in money supply are explained by the money supply specific shock. Interest rates begin to play a role in explaining the fluctuations in money supply from the second quarter and peak at around two years. In the medium term, however, GDP specific shocks increase in importance and explain about 50% of the fluctuations in the money supply in the long-run.
- 3. Fluctuations in interest rates at all horizons are attributed mostly to interest rate shocks, with a small proportion of the variation explained by GDP shocks, while money supply shocks play a negligible role at all horizons.
  - (c) Obtain inference on Granger causality among  $lrgdp_t$ ,  $lrm2_t$  and  $rs_t$ .

**Solution** The function causality in the vars package is very handy to implement Granger causality tests. The option cause is used to specify which variable is being tested as Granger-causing other variables in the system. For example, if we set cause = "lrgdp", the function will test if lrgdp Granger-causes lrm2 and rs simultaneously.

```
for (i in 1:3)
{
  ctest i <- causality(VAR est[[8]],</pre>
                        cause = vnames[i])
  print(ctest_i$Granger)
}
##
##
    Granger causality HO: lrgdp do not Granger-cause lrm2 rs
##
## data: VAR object VAR_est[[8]]
  F-Test = 2.0514, df1 = 16, df2 = 408, p-value = 0.009689
##
##
    Assignment Project Exam He Granger Gasality HO: 1rm2 do not Granger-cause 1rgdp
##
##
## data: VAR object VAR est[[8]]
## F-Test = 113147 Sf.1/ FlellOre Sos Colline = 0.1779
##
##
    Granger charty hats de stutantes suse lrgdp lrm2
##
##
## data: VAR object VAR est[[8]]
## F-Test = 5.3824, df1 = 16, df2 = 408, p-value = 2.09e-10
```

We confirm that GDP Granger-causes either real money supply or interest rates (or both) at the 1% significance level. Likewise, interest rates are confirmed to Granger-cause either GDP or money supply (or both) at very small significance level. However, we do not have sufficient evidence to confirm that money supply does not Granger-cause GDP and interest rates.