ECON7350: Applied Econometrics for Macroeconomics and Finance

Tutorial 4: Dynamic Relationships

At the end of this tutorial you should be able to:

- derive the ECM representation of an ARDL(p, l, s) model;
- create a function in R;
- estimate IRFs to permanent and one-off shocks as well as LRMs;
- construct confidence intervals for IRFs and LRMs;
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Problems https://tutorcs.com

1. Derive the ECM representation of the following ARDL(1, 1, 2) model:

$$y_t = W + c y_t - h + 2 t x_t + c x_t + u + c y_t - x_t + c x_t + c$$

Which parameter(s) in the resulting ECM are long-run multiplier(s) and adjustment parameter(s)?

2. Create a function in R to compute coefficients $\theta_0, \ldots, \theta_h$ in

$$\theta(L) = b(L)/a(L) = \theta_0 + \theta_1 L + \dots + \theta_h L^h + \dots,$$

where
$$a(L) = a_0 + a_1 L + \dots + a_p L^p$$
 and $(L) = b_0 + b_1 L + \dots + b_q L^q$.

3. Create a function in R to compute IRFs (to both one-off and permanent shocks) up to horizon h as well as the LRMs for the ARDL(p, l, s):

$$a(L)y_t = a_0 + b(L)x_t + c(L)w_t + \epsilon_{y,t}.$$

- 4. The file wealth.csv contains observations on:
 - c_t : the log of total real per capita expenditures on durables, nondurables and services;

- a_t : the log of a measure of real per capita household net worth (including all financial and household wealth); and
- y_t : the log of after-tax labour income.

The sample period from 1952Q2 through 2006Q2 (see Koop, G., S. Potter and R. W. Strachan (2008) "Re-examining the consumption-wealth relationship: The role of uncertainty" Journal of Money, Credit and Banking, Vol. 40, No. 2.3, 341-367).

- (a) Estimate an ARDL(1, 2, 2) specified for c_t and use the functions created in Questions 2 and 3 to obtain the estimated IRFs to permanent shocks in a_t and y_t as well the LRMs. Hint: to estimate the ARDL parameters, try the ardl function that is provided by the ARDL package.
- (b) Estimate the ECM representation of the ARDL(1,2,2) and report the results. How do the LRMs in the estimated ECM compare to those computed in part (a)? Hint: use the recm and multipliers functions to convert the output produced by ardl.
- (c) Use the function ardl_irfs_ci that is provided in the file ardl_irfs_ci.R to construct 68% confidence intervals for the IRFs obtained in part (a).

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- ardl_est: this is the output of ardl;
- h: the maximum IRF horizon (default is 40);
- cumirft whether to tought like to aperhanent shock (default is TRUE);
- conf: the confidence level of the intervals (default is 0.95).

It returns the following outputs: Stutores \bullet 1b: an $h \times k$ matrix of lower-bounds for confidence intervals;

- md: an $h \times k$ matrix of mid-points for confidence intervals;
- ub: an $h \times k$ matrix of upper-bounds for confidence intervals.

Note that k is the number of independent variables in the ARDL, so that column j of 1b, md and ub is related the confidence intervals for IRFs to a shock in the jth independent variable.

- (d) Compare the values in md to the IRFs estimates obtained in part (a).
- (e) Use the LRM estimates and standard deviations obtained in part (b) to construct 68% confidence intervals for the LRMs, assuming the sampling distributions of the LRM estimators are approximately normal. How do they compare to the IRF confidence intervals obtained in part (c)?
- (f) Construct an adequate set of ARDL(p, l, s) models for c_t .
- (g) Draw inference about the dynamic relationship between expenditures and wealth.