Linear Programming and its Applications Assignment Project Exam Help Sanjay Dominik Jena

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MBA 8419 - Decision Making Technology

Overview of the presentation

Assignment roll and ject Exam Help

- General Form
- Applications and the use of EXCEL's Solver Turner / t
 - Finance
 - Operations management
- Powers the a models colved itores
 - Graphical solution
 - Sensitivity analysis

Problem ⇒ optimization model



FIGURE – Taken from Anderson et. al. (2012), Chap.2

Problem ⇒ optimization model

General characteristics ssignment Project Exam Help

- Desire to max or min some quantity
 - Objective of the LP
- petinopor réstitutiphon constrains
 - limit the values the decisions can take
 - implicitly limit the degree to which the objective can be

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- Satisfying customer demands
- Budgets
- Limited supplies
- Limited capacities (space, time, employees, etc.)
- etc.



Problem ⇒ optimization model

Assignment Project Exam Help

De inition what decisions Deficition: what is need to be nade and how be tile pursue do they influence the state of the system under study.

Deficition: what is need to be not be tile pursue of the system under study.

Characteristics:

- · Varying impacts on the
- category
- Can be made over multiple time periods

be tile pursue in solving the problem or in modifying the system (i.e., what criteria is used to evaluate the decisions).

Characteristics:

decisions

Definition: set of obligations and limits that need to be enforced and that define admissible/feasible decisions.

Characteristics:

• Slard

- Soft
- Non-negativity
- Integrity

FIGURE – Process to formulate a problem



General form

Decision variables

ssignment Project Exam Help

Subjective
$$\sum_{a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n} \frac{c_1x_1 + c_2x_2 + \dots + c_nx_n}{\sum_{a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n} \sum_{s=0}^{s} b_1}$$

We Carrate $\sum_{a_{11}x_1 + a_{12}x_2 + \dots + a_{1n}x_n} \sum_{s=0}^{s} b_1$

$$\vdots \\ a_{m1}x_1 + a_{m2}x_2 + \ldots + a_{mn}x_n \begin{pmatrix} \leq \\ \geq \\ = \end{pmatrix} b_m$$

 $x_1, x_2, \dots, x_n \ge 0$ and x_j is integer, $\forall j \in E$ and given $E \subseteq \{1, 2, \dots, n\}$

Marketing

Types of problems

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Description: Choose between a set of available media options such as to maximize the promotional effort for a given set of products or services, targeted at specific segments of a given population

https://tutores.com

Sales territory coverage

Description: Assign a set of salespersons to a set of existing or potential customers such as to minimize costs, or, ensure that the workload (or valv) ming the salespersons are uniform distributed

Marketing research

Description : To understand the composition and nature of a targeted market, establish the number and types of studies that need to be performed to obtain the desired information while minimizing the costs

Assignment Project Exam Help

Context: Market Survey Inc. (MSI), specializes in evaluation of consumer reaction to new products, services, and advertising consumer reaction to a recently marketed household product.

Strategy: cdor-tydoor personal interviews with families (i.e., households) that either have, or don't have, children.

Contract: MSI must conduct 1 000 interviews

Marketing research (cont'd)

Assigned in Project Exam Help

- 2 Interview at least 400 households without children
- 3 The total number of households interviewed during the evening must be at least as great as the number of households interviewed during the day.
- At least 40% of the interviews for households with children must be conducted during the evening
- 5 A least 60% of the interviews for figure holds without children must be conducted auring the evening

	Interview cost					
Household	Day	Evening				
Children	20\$	25\$				
No Children	18\$	20\$				

TABLE - Unitary costs per interview_type

Marketing

Marketing research (cont'd)

Model: Project Exam Help DC = the number of daytime interviews of households with children,

EC = the number of evening interviews of households with children,

DNC = the number of daytime interviews of households without children.

ENC = the number of evening interviews of households without children.

Objective Function: min 20DC + 25EC + 18DNC + 20ENC

Subject to :

DNC + ENC > 400

 $EC + ENC \ge DC + DNC$

EC > 0,4(DC + EC)

 $ENC \geq 0, 6(DNC + ENC)$

DC, EC, DNC, ENC > 0 and integer.

Marketing

Solving the problem using EXCEL

Assignment Project Exam Help Standard Form:

- Each column is associated with a specific decision variable
 Fach line is associated to a linear function (i.e., objective dan boostrail stell UTCS. COIN
- Use of the Solver function
 - Define the variable cells
 - Define the objective cell and macon min S
 - Make Unconstrained Variables Non-Negative
 - Select solving method :
 - GRG Nonlinear ⇒ for nonlinear optimization models
 - Simplex LP ⇒ exact method for linear optimization models
 - Evolutionary ⇒ heuristic method for optimization models

Assignment Project Exam Help Optimal solution to the MSI problem

Number of Interviews
Children 240 160 400

No Children 240 360 600

Total 480 520 1000

We Charle Colimbia Quir CS

Types of problems

ssignment Project Exam Help

Description: Considering a set of available stocks and bonds, determine the amount of investment that a company (or particular) should make in each financial instrument with the objective of minimizing risk, hitips://tutoics.com

- Valuation of financial instruments
 - **Description**: In the context of trading within financial markets, detern what is the value of the assets that are being traded
- Financial planning

Description: Figure out what funding decisions should be made to best raise the necessary capital from the financial markets to finance an organization's activities



Finance

Description: Portfolio models are used to determine the % of the investment funds that should be made in each available assets.

Goal Detydeshe betutatant Gesvesnoum d return.

Context: Hauck Investment Services designs annuities and long term investment plans for investors with a variety of risk tolerandes Hauckwould like to the propagation of the total can be used to determine an optimal portfolio involving a mix of six mutual funds. A variety of measures can be used to indicate risk, but for portfolios of financial assets all are related to variability in return.

Finance

Designing Portfolio of Mutual Funds (cont'd)

Managers at Handh Financial Services think that the returns of past years can be used to represent the possibilities (i.e., scenarios) for the next year. Therefore, the following information will be used as planning scenarios for the next 12 months:

TOS://TUTOTCSAIGUARITIR (%) Mutual Fund Year 1 Year 2 Year 3 Year 4 Year 5 Foreign Stock 10,06 13.12 13.47 45.42 -21.93 Intermediate-Ferm Bond 17.64 3,25 7.51 -1.33 7.36 Lavge-Cal Growth 18.71 41,46 -23,26Large-Cap Value 32,36 20,61 12,93 7,06 -5,37Small-Cap Growth 3.85 -9.02 33.44 19.40 58.68 Small-Cap Value 24.56 25.32 -6.70 5.43 17.31

TABLE – Mutual fund performance in 5 selected years

Finance

Conservative Portiglio Project Fxam Help

to risk. Determine the proportion of the portfolio to invest in each of the six mutual funds so that the portfolio provides the best return possible with a

FS = proportion of portfolio invested in the Foreign Stock mutual fund

IB = proportion of portfolio invested in the Intermediate-Term Bond fund

LG = plotorten of portolip invested in the Large Gao Growth fund

LV = proportion of portfolio invested in the Large-Cap Value fund

SG = proportion of portfolio invested in the Small-Cap Growth fund

SV = proportion of portfolio invested in the Small-Cap Value fund

Finance

Assignment Project Exam Help FS + IB + LG + LV + SG + SV = 1

The partfolio return over the next year will depend on which scenario will occur $\frac{1}{1} \frac{1}{1} \frac{1$

$$R_1 = 10.06FS + 17.64IB + 32.41LG + 32.36LV + 33.44SG + 24.56SV$$

$$R_2 = 13.12FS + 3.25IB + 18.71LG + 20.61LV + 19.40SG + 25.32SV$$

$$R_3 = \sqrt{3}$$
, $C_5 + 7$, $C_7 + 3$, $C_7 + 1$, $C_7 +$

$$R_4 = 45,42FS + 1,33IB + 41,46LG + 7,06LV + 58,68SG + 5,43SV$$

$$R_5 = -21,93FS + 7,36IB - 23,26LG - 5,37LV - 9,02SG + 17,31SV$$

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M = minimum return for the portfolio

To define M, we need to add the following minimum-return constaints ps://tutorcs.com

 $R_1 \geq M$ Scenario 1 minimum return Scenario 2 minimum return Maccenario 8 minimum return Viscenario 4 minimum return Scenario 5 minimum return

Finance

on, provides the following five minimum-return constraints:

```
10,06FS + 17,64IB + 32,41LG + 32,36LV + 33,44SG + 24,56SV > M
                                                                             Scenario 1
13, 12FS + 3, 25/B + 18/71LG + 20, 61/V + 19, 40SG + 25, 32SV \ge M
13, 41AS + 7257B + 33, 224G + 12, 63V + 3, 25G + 670SV \ge M
                                                                             Scenario 2
                                                                             Scenario 3
 45,42FS+1,33IB+41,46LG+7,06LV+58,68SG+5,43SV>M
                                                                             Scenario 4
 -21.93FS + 7.36IB - 23.26LG - 5.37LV - 9.02SG + 17.31SV > M
                                                                             Scenario 5
```

Objective Euclinat: Cstutorcs

Apply a maximin approach

max M

Finance

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s.t.

$$\begin{array}{c} 10.06FS + 17,64/B + 32,41LG + 32,36LV + 33,44SG + 24,56SV \geq M \\ 13,12FS + 3,25/B + 18,712G + 20,012V + 3,85SG + 25,32SV \geq M \\ 13,47FS + 7,51/B + 33,28LG + 12,93LV + 3,85SG - 6,70SV \geq M \\ \hline \\ 13,47FS + 7,51/B + 33,28LG + 12,93LV + 3,85SG - 6,70SV \geq M \\ \hline \\ 13,47FS + 7,51/B + 23,28LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 13,47FS + 7,36/B + 23,28LG + 12,93LV + 3,85SG - 6,70SV \geq M \\ \hline \\ 13,47FS + 7,36/B + 23,28LG + 12,93LV + 3,85SG + 5,43SV \geq M \\ \hline \\ 14,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 17,31SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 7,06LV + 58,68SG + 5,43SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 12,93/LV + 12,82SG + 17,31/SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 12,93/LV + 12,82SG + 17,31/SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 12,93/LV + 12,82SG + 17,31/SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 12,93/LV + 12,82SG + 17,31/SV \geq M \\ \hline \\ 15,42FS + 11,33/B + 41,46LG + 12,82SG + 12,82SG$$

Finance

Moderate Risk Portfolio

Note contain clients are Prilling to accept a moderate amount 1p

Assumption

Clients in this category art willing to accept some risks but do not want the annual return for the portfolio to drop below 2%

Therefore, M = 2 $Vec{hat}_{oen}$ Cistuation in Cetson

- $R_2 \ge 2$ Scenario 2 minimum return
- $R_3 \ge 2$ Scenario 3 minimum return
- $R_4 > 2$ Scenario 4 minimum return
- $R_5 \ge 2$ Scenario 5 minimum return

Finance

Objective Function

A different objective is needed here \Rightarrow Maximize the expected Self-Edhinobit Project Exam Help

Assumption

Assuming that p_i, for j = 1,...,5, are the probabilities of observing the Scenarios it OTCS.COM

Then, $R = p_1R_1 + p_2R_2 + p_3R_3 + p_4R_4 + p_5R_5$, defines an estimator of the expected value of the return

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$$\max p_1 R_1 + p_2 R_2 + p_3 R_3 + p_4 R_4 + p_5 R_5$$

If all scenarios are equiprobable, then

$$\max \frac{1}{5}R_1 + \frac{1}{5}R_2 + \frac{1}{5}R_3 + \frac{1}{5}R_4 + \frac{1}{5}R_5$$

Finance

Model Assignment Project Exam Help s.t.

FS + IB + LG + LV + SG + SV = 1. FS, IB, LG, LV, SG, SV > 0

Operations management

Types of problems

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Description: Planning and executing the various distribution operations of a company to serve its clients in a timely manner, while minimizing

https://tutorcs.com

Description: Planning and scheduling the production operations of a company, which may include the procurement processes, the myndigen int of rivertory, establishing the podection levels through time, assigning ressources, etc., while minimizing the overall costs.

Logistics Network Design

Description: Design, manage and coordinate a logistics network such as to perform the necessary operations while minimizing costs.

Operations management

Production Scheduling

Description : Electronic components for a major airplane engine manufacturer. The airplane engine manufacturer notifies the Bollinger sales office each quarter of its month reducing the local transfer of the next three months. The requirements may vary considerably, depending on the type of engine the manufacturer is

> Component April May June 322A 5 000 1 000 3 000 802B 1 000 500 3 000

TABLE – Three-month demand schedule for BEC

Operations management

Production Scheduling (cont'd)

DE PRINTS (TO CASE), a difficult statement is sextent product C 1) tion control department. The production control department then develops a three-month production plan for the components. The production manager will want to identify the following:

- pttos://stutores.com
- Inventor holding cost
- Change-in-production-level costs

at: cstutores Costs \

- 322A costs 205 per unit produced, while 802B costs 105 per unit produced
- Inventory holding costs are 1.5% of the cost of the product (monthly)
- Cost associated with ↑ the production level for any month is 0.50\$ per unit increase
- Cost associated with ↓ the production level for any month is 0.20\$ per unit decrease

Operations management

Production Scheduling (cont'd)

| SignMachine | Capacity | Color | Capacity | Storage | Capacity |

TABLE - Machine, Labor and Storage Capacities for BEC

Composent	Machine (houts/unit)	Cholusium)	Storage (square feet/unit)
322A	0.10	0.05	2
802B	0.08	0.07	3

TABLE – Machine, Labor and Storage requirements for components 322A and 802B



Operations management

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- x_{im} = production volume in units for product *i* in month *m*
- s_{im} = inventory level for product i at the end of month m
- https://tuttordsicoemecessary during month m
- D_m = decrease in the total production level necessary Weethrat: cstutorcs

Where.

$$i = 1 \Rightarrow 322A$$
 and $i = 2 \Rightarrow 802B$
 $m = 1 \Rightarrow April, m = 2 \Rightarrow May and m = 3 \Rightarrow June$

Operations management

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min Total Cost = Total production cost + Inventory holding cost + Change-in-production-level costs

Total
$$| \mathbf{A}_{13} | \mathbf{A}_{13$$

Inventory holding cost = $(0.015 \times 20)(s_{11} + s_{12} + s_{13}) + (0.015 \times 10)(s_{21} + s_{22} + s_{23})$

Change-in-production-level costs = $0.50(l_1 + l_2 + l_3) + 0.20(D_1 + D_2 + D_3)$

Theref We Chat: cstutorcs

min $20x_{11} + 20x_{12} + 20x_{13} + 10x_{21} + 10x_{22} + 10x_{23} + 0.30s_{11} + 0.30s_{12} + 0.30s_{13} + 0.15s_{21} + 0.15s_{22} + 0.15s_{23} + 0.50l_1 + 0.50l_2 + 0.50l_3 + 0.20D_1 + 0.20D_2 + 0.20D_3$

Operations management

Subject to:



Inventories at the beginning/of the three-month scheduling period were 500 units for compo lent 3 24) and 200 yin is for component 802B The domain would like to have 400 and 200 units, respectively for each product, in the inventory at the end of the planning.

Month 1:
$$500 + x_{11} - s_{11} = 1000$$

$$s_{21} + x_{22} - s_{22} = 500$$

Month 3:
$$s_{12} + x_{13} - s_{13} = 5000$$

 $s_{22} + x_{23} - s_{23} = 3000$

Ending inventory:

$$s_{13} \ge 400$$

 $s_{23} > 200$

Operations management

Subject to (cont'd): Project Exam Help Machines:

```
Month 1: 0.10x_{11} + 0.08x_{21} \le 400
\begin{array}{l} \text{Month}_2: 0.10x_{12} + 0.08x_{22} \leq 500 \\ \text{Month}_3: 0.08x_{2} + 0.08x_{3} = 0.0
```

Labor:

Month 1:
$$0.05x_{11} + 0.07x_{21} \le 300$$

Month 2: $0.05x_{11} + 0.07x_{22} \le 300$
Month 4: $0.05x_{11} + 0.07x_{22} \le 300$
Month 4: $0.05x_{11} + 0.07x_{22} \le 300$

Storage:

```
Month 1 : 2s_{11} + 3s_{21} \le 10000
Month 2 : 2s_{12} + 3s_{22} < 10000
Month 3: 2s_{13} + 3s_{23} < 10000
```

Operations management

Subject to (cont'd):

Production levels during the month of March were 1 500 units of 322A

and 1 000 units of 802B

Month 1:
$$(x_{11} + x_{21}) - 2.500 = I_1 - D_1$$

s://tutorcs.com There are three possible cases:

- If $(x_{11} + x_{21}) 2500 > 0$ then $I_1 > 0$ and $D_1 = 0$
- If $(x_1) + x_2 = 0$ and $(x_1) + x_2 = 0$

Month 2:
$$(x_{12} + x_{22}) - (x_{11} + x_{21}) = I_2 - D_2$$

Month 3:
$$(x_{13} + x_{23}) - (x_{12} + x_{22}) = I_3 - D_3$$

Non-negativity and integrality:

 $x_{im}, s_{im}, I_m, D_m > 0$ and integer, $\forall i, m$.

Graphical solution

Consider the optimization problem (P):

szignment Project Exam Help subject to

- (C1) $10x_1 + 5x_2 < 200$
- $\begin{array}{c} \text{(C2) } 2x_1 + 3x_2 \leq 60 \\ \text{(C3) } 1539 \text{S:} // tutorcs.com \end{array}$
- (C4) $x_2 < 14$
- (C5) $x_1, x_2 > 0$

Dimensioned that cstutores

- 2 decision variables
- 4 technological constraints
- 2 non-negativity constraints

The feasible region of the model can be graphically represented

Graphical solution

Graphical representation of the feasible region

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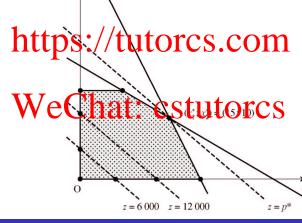
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Graphical solution

Solving the problem graphically

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Graphical solution

Extreme points and the optimal solution. Salgential Chitis Pth Ole Camp Exam Help

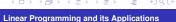
- Interior : none of the constraints is satisfied as an equation
- Border: at least one constraint is satisfied as an equation
- Exprine ocaled at the intersection of two constraints (two constraints are satisfied as equations)

Theorem

If an optimal 30 ution to a precific linear program in model exists, then such a solution can be found at an extreme point of the feasible region.

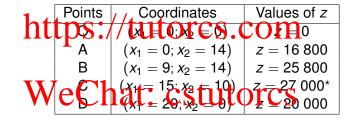
Note: This result means that if you are looking for the optimal solution to a linear program, one does not need to evaluate all feasible solution points.

Only the feasible solutions that occur at the extreme points of the feasible region need to be evaluated.



Graphical solution

Assignment Project Exam Help Evaluation of z at the extreme points



Sensitivity analysis

Substitution of the continual solution obtained for a linear programming model progr

sensitive to modifications to the values of the parameters of the model?

When the value of the coefficient of a decision variable in the objective function changes does that neges saily anal (have nie primal solution obtained?

What is the impact of a change in the right-hand side value of a constraint with respect to the optimal solution found?

Types what es hat: cstutorcs We will consider two types of modifications in the model:

- Modification of the value of a c_i (a coefficient in the objective function)
- Modification of the value of a b_i (the right-hand side of a constraint)

Sensitivity analysis

Modifying a ci SS1 SS1 SS Brahm Leving to Peroject Exam Help

$$\max Z = C_1 X_1 + C_2 X_2$$

In the standard form, the previous function can be expressed as : $x_2 = \frac{-c_1}{c_2}x_1 + \frac{z}{c_2}$

Therefore ttps://tutorcs.com

• When c; Por c₂ ↓ ⇒ the value of the slope of the objective function ↓

- When $c_1 \downarrow$ or $c_2 \uparrow \Rightarrow$ the value of the slope of the objective function \uparrow

Observation: When the modification brings the objective function to cross the feasible region We meet the martimal course to anterior CS

Conclusion:

As long as:

slope of (C1)
$$\leq \frac{-c_1}{c_2} \leq$$
 slope of (C2)

The optimal solution remains the same



Sensitivity analysis

Modifying a b_i

The optimal solution extreme point 6 (x, 1 = 15) x = 10) x is at the intersection of point intersection of poi

etinitions

- A constraint is active at a given solution if the solution satisfies the constraint as an equation
- Apistan is nactive at a given splittion the solution satisfies the constraint as an inequality

Therefore

- If $b_1 \uparrow 1$ (i.e., $200 \rightarrow 201$) and b_2 remains the same Invact: CSTULTOTCS

 Optimal solution becomes $C' = (x_1 = 15.15, x_2 = 9.9)$ Value of the solution: $z' = 27\ 030$ (i.e., $\Delta = +30$)
- If $b_2 \uparrow 1$ (i.e., $60 \rightarrow 61$) and b_1 remains the same Impact :

Optimal solution becomes $C'' = (x_1 = 14.75, x_2 = 10.5)$

Value of the solution : z'' = 27 350 (i.e., $\Delta = +350$)

Sensitivity analysis

Assignment Project Exam Help

Parameters	X1	X2				Model					
Values cj	1000	1200		,	1.	Variables	X1	X2			
- h1	-11	10	•	/ /	/ 1	Values 1	~ PE	con	1		
111	1	Jb 2	b3	b∦		uw			R.H.S		L.H.S
Values bj	200	- 60	34	14		(C1)	10	5	200	<=	200
						(C2)	2	3	60	<=	60
						(C3)	1	0	15	<=	34
**	7		11		4	(C4)	0	1	10	<=	14
M	/ P	• (ľ	1	ว1	. ()		orcs			
•			1	1	u		luc		Val. Z		
						cj	1000	1200	27000		

Sensitivity analysis

Answer Report

A Sisting and the policy of the policy function, the decision variables, and the policy of the polic

Objective Cell (Max) Cell Name Original Value Final Value \$1,\$11 cj yal, Z 27000 27000 Variable Cells

	Cell	Name	Original Value	Final Value	Integer	
	\$H\$3 Va		15	15	Contin	
TT 7 - 4	ŞIŞ	Values X2	10	10	Contin	
we		nau	: CSI	lute	ICS	

Constraints

·U	iistiai	1113				
	Cell	Name	Cell Value	Formula	Status	Slack
	\$J\$5	(C1) R.H.S	200	\$J\$5<=\$L\$5	Binding	0
	\$J\$6	(C2) R.H.S	60	\$J\$6<=\$L\$6	Binding	0
	\$J\$7	(C3) R.H.S	15	\$J\$7<=\$L\$7	Not Binding	19
	\$J\$8	(C4) R.H.S	10	\$J\$8<=\$L\$8	Not Binding	4

Sensitivity analysis

Assignment Project Exam Help

_			Final	Reduced	Objective	Allowable	Allowable
	Cell	Name	Value	Cost	Coefficient	Increase	Decrease
		Values X1	15	0	1000	1400	200
1-44-	\$1\$3	Values K2	10	0	1200	300	700
http) S	// L	ut	Or	CS.C	CON	

			Final	Shadow	Constraint	Allowable	Allowable
	Cell	Name	Value	Price	R.H. Side	Increase	Decrease
	\$J\$5	(C1) R.H.S	200	30	200	100	40
\mathbf{X}	\$ \$6	(12) R H.S	1 •60	○ 350	-1149	1108	20
YY (\$.\$7	(3) RH	15		tute	1+30	19
	\$J\$8	(C4) R.H.S	10	0	14	1E+30	4

Variables: if reduced cost is 0, the current objective coefficient can be increased or decreased by the indicated "allowable" values without changing the current optimal solution.

Constraints: the RHS of the constraint can be increased or decreased by up to the indicated "allowable" amount, and for any unit increase/decrease the objective function will increase/decrease by the amount indicated as shadow price.