

Solutions for Homework 2

Problem 1 Find the tensor product

$$\begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix} \otimes \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}.$$

Solution:

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$$\begin{pmatrix} 0 & 0 & -i & 0 \\ 0 & 0 & 0 & i \\ i & 0 & 0 & 0 \\ 0 & -i & 0 & 0 \end{pmatrix}$$

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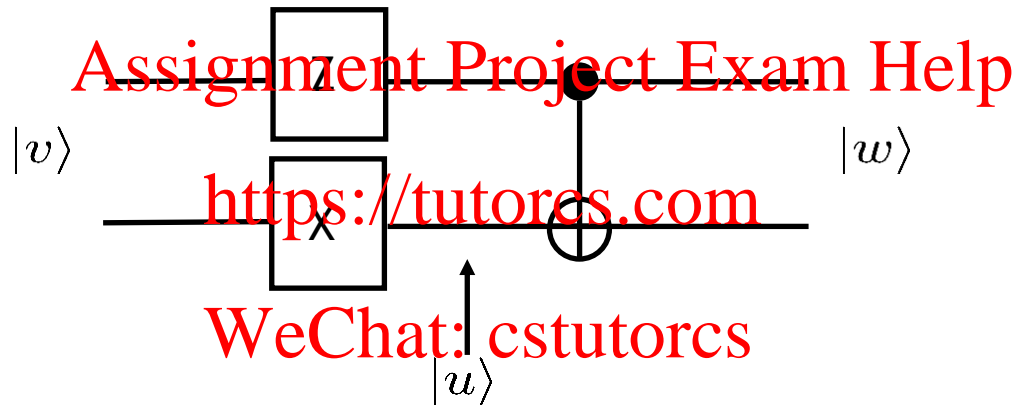
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Home Work 2

Problem 2 For the input state

$$|v\rangle = \alpha_{00}|00\rangle + \alpha_{01}|01\rangle + \alpha_{10}|10\rangle + \alpha_{11}|11\rangle$$

find the state $|w\rangle$ at the output of the following circuit

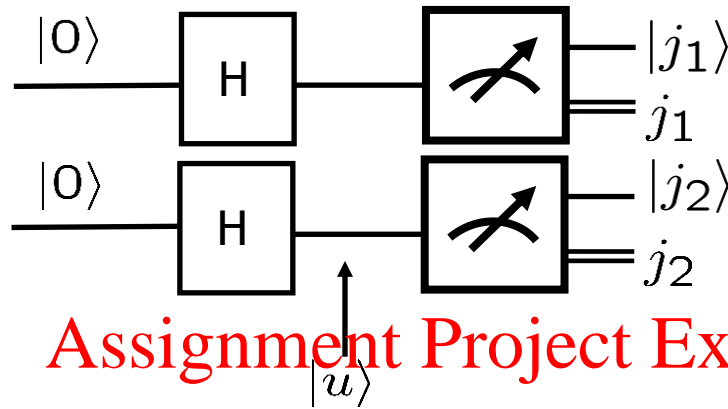


Solution

$$|u\rangle = \alpha_{00}|01\rangle + \alpha_{01}|00\rangle - \alpha_{10}|11\rangle - \alpha_{11}|10\rangle$$

$$|w\rangle = \alpha_{00}|01\rangle + \alpha_{01}|00\rangle - \alpha_{10}|10\rangle - \alpha_{11}|11\rangle$$

Problem 3



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Find the classical and quantum outputs and the corresponding probabilities.

Solution

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$$|u\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) = \frac{1}{2}(|00\rangle + |01\rangle + |10\rangle + |11\rangle)$$

Cl. Outputs

0 0
0 1
1 0
1 1

Q. Outputs

$|0\rangle |0\rangle$
 $|0\rangle |1\rangle$
 $|1\rangle |0\rangle$
 $|1\rangle |1\rangle$

Probability

$\frac{1}{4}$
 $\frac{1}{4}$
 $\frac{1}{4}$
 $\frac{1}{4}$

Problem 4 Let we have two qubits in the state

$$\frac{1}{\sqrt{2}}(|01\rangle + |10\rangle)$$

Let we act on the second qubit by the unitary rotation H. Find the new state of these two qubits.

Solution

$$\begin{aligned} & \frac{1}{\sqrt{2}}|0\rangle \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle) + \frac{1}{\sqrt{2}}|1\rangle \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle) \\ &= \frac{1}{2}(|00\rangle - |01\rangle + |10\rangle + |11\rangle) \end{aligned}$$

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