

SEC204

Computer Architecture and Low Level Programming

Assignment Project Exam Help

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School of Computing
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Outline

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- Positional Numbering Systems
 - Signed Integer Representation
 - Floating Point Representation
 - Character Codes
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Basics (1)

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- The bit is the most basic unit of information in a computer
 - ▣ Switching activity 0 or 1
- A Byte is a group of 8 bits
 - ▣ A byte is the smallest possible addressable unit of computer storage
 - ▣ The term, “addressable,” means that a particular byte can be retrieved according to its location in memory
- A word is a contiguous group of bytes, e.g., an integer uses 4 bytes
- Word sizes of 4 or 8 bytes are most common

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Basics (2)

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Kilo- (K) = 1 thousand = 10^3 and 2^{10}

Mega- (M) = 1 million = 10^6 and 2^{20}

Giga- (G) = 1 billion = 10^9 and 2^{30}

Tera- (T) = 1 trillion = 10^{12} and 2^{40}

Peta- (P) = 1 quadrillion = 10^{15} and 2^{50}

Exa- (E) = 1 quintillion = 10^{18} and 2^{60}

Zetta- (Z) = 1 sextillion = 10^{21} and 2^{70}

Yotta- (Y) = 1 septillion = 10^{24} and 2^{80}

Normally, powers of 2 are used for measuring capacity

Milli- (m) = 1 thousandth = 10^{-3}

Micro- (μ) = 1 millionth = 10^{-6}

Nano- (n) = 1 billionth = 10^{-9}

Pico- (p) = 1 trillionth = 10^{-12}

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Basics (3)

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- Hertz = clock cycles per second (frequency)
 - ▣ $1\text{MHz} = 1,000,000\text{Hz}$
 - ▣ Processor speeds are measured in MHz or GHz
- Byte = a unit of storage
 - ▣ $1\text{KB} = 2^{10} = 1024\text{ Bytes}$
 - ▣ $1\text{MB} = 2^{20} = 1,048,576\text{ Bytes}$
 - ▣ $1\text{GB} = 2^{30} = 1,099,511,627,776\text{ Bytes}$
- Main memory (RAM) is measured in GB
- Disk storage is measured in GB for small systems, TB (2^{40}) for large systems

POSITIONAL NUMBERING SYSTEMS (1)

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- Positional numbering systems are systems in which the placement of a digit in connection to its intrinsic value determines its actual meaning in a numeral string
- The organization of any computer depends considerably on how it represents numbers, characters, and control information
 - **There are several positional numbering systems such as Decimal, Binary, Octal, Hexadecimal etc**
- The positioning system is provided as a subscript, e.g., 14_{10} , 10101_2 , 82_{16}

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POSITIONAL NUMBERING SYSTEMS (2)

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- Our decimal system is the base-10 system. It uses powers of 10 for each position in a number

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- The binary system is also called the base-2 system

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- The hexadecimal system is the base-16 system

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- The Mayan and other Mesoamerican cultures used a number system based in a base-20 system

Decimal System

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□ **Decimal system:** Our well known and used system.

□ **It uses 10 different digits: 0,1,2,3,4,5,6,7,8,9**

□ Our decimal system is the base 10 system. It uses powers of 10 for each position in a number

□ For example, the decimal number 947 in powers of 10 is

$$947 =$$

$$= 9 \times 100 + 4 \times 10 + 7 \times 1 =$$

$$= 9 \times 10^2 + 4 \times 10^1 + 7 \times 10^0$$

□ $70216 = 7 \times 10000 + 0 \times 1000 + 2 \times 100 + 1 \times 10 + 6 \times 1 =$

$$= 7 \times 10^4 + 0 \times 10^3 + 2 \times 10^2 + 1 \times 10^1 + 6 \times 10^0$$

□ The decimal number 3812.46 in powers of 10 is $(3 \times 10^3 + 8 \times 10^2 + 1 \times 10^1 + 2 \times 10^0 + 4 \times 10^{-1} + 6 \times 10^{-2})$

Binary System

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- A binary number is a number expressed in the base-2 numeral system or binary numeral system, which uses only two symbols: typically 0 (zero) and 1 (one)
- The base is 2
- **2 different digits are used: 0, 1**
- For example, $101_2 = 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0$
 $= 1 \times 4 + 0 \times 2 + 1 \times 1$
 $= 5_{10}$
- The binary number 11001 in powers of 2 is: $1 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 = 16 + 8 + 0 + 0 + 1 = 25_{10}$
- $1011.101_2 =$
 $= 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 + 1 \times 2^{-1} + 0 \times 2^{-2} + 1 \times 2^{-3} =$
 $= 1 \times 8 + 0 \times 4 + 1 \times 2 + 1 \times 1 + 1 \times 0.5 + 0 \times 0.25 + 1 \times 0.125$
 $= 11.625_{10}$

Octal system

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- The base is 8
- **8 different digits are used only: 0,1,2,3,4,5,6,7**
- For example: $436_8 = 4 \times 8^2 + 3 \times 8^1 + 6 \times 8^0$
 $= 4 \times 64 + 3 \times 8 + 6 \times 1$
 $= 286_{10}$

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Convert the following octal number 205.24₈ to decimal:

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$$\begin{aligned} 205.24_8 &= 2 \times 8^2 + 0 \times 8^1 + 5 \times 8^0 + 2 \times 8^{-1} + 4 \times 8^{-2} \\ &= 2 \times 64 + 0 + 5 + 2 \times 0.125 + 4 \times 0.015625 \\ &= \mathbf{133.3125_{10}} \end{aligned}$$

Hexadecimal system

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- The base is 16
- **16 different digits are used: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F**
(we do not use numbers with 2 digits like 10, 11, 12, ..., but **A instead of 10, B instead of 11, C instead of 12, etc**)
- Example: $3B1_{16} = 3 \times 16^2 + 11 \times 16^1 + 1 \times 16^0$
 $= 3 \times 256 + 11 \times 16 + 1 =$
 $= 768 + 176 + 1 =$
 $= 945_{10}$

Convert the following hexadecimal number $20C.2_{16}$ to decimal

$$\begin{aligned} 20C.2_{16} &= 2 \times 16^2 + 0 \times 16^1 + 12 \times 16^0 + 2 \times 16^{-1} = \\ &= 2 \times 256 + 0 + 12 \times 1 + 2 \times 0.0625 = \\ &= 512 + 12 + 0.125 = \\ &= \mathbf{524.125_{10}} \end{aligned}$$

In the Lab session

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- You will learn how to convert from a system to another...

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Positional Numbering Systems - General case

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- Base: r
- Uses r different digits: $0, 1, 2, 3, \dots, r-1$

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$$N_r = A_{n-1} A_{n-2} \dots A_1 A_0 A_{-1} A_{-2} \dots A_{-(m-1)} A_{-m}$$

$$N_r = A_{n-1} \times r^{n-1} + A_{n-2} \times r^{n-2} + \dots + A_1 \times r^1 + A_0 \times r^0 + A_{-1} \times r^{-1} + A_{-2} \times r^{-2} + \dots + A_{-(m-1)} \times r^{-(m-1)} + A_{-m} \times r^{-m}$$

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To better understand the above formula consider that if $234.03_5 = ?_{10}$ then $n=3$, $m=2$ and $r=5$

- The left most digit (A_{n-1}) is called Most Significant Bit-(MSB) while the right most (A_{-m}) Least Significant Bit-(LSB)

Basic arithmetic operations

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- The basic arithmetic operations are applied to **all** the previous numerical systems. There are:
 - Addition **Assignment Project Exam Help**
 - Subtraction
 - Multiplication **<https://tutorcs.com>**
 - Division **WeChat: cstutorcs**
- **Examples are provided in the lab session...**

Signed integer representation

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Introduction

- In practice we have to use negative binary numbers too. **We need to define signed binary numbers**

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- ✓ **There are three ways in which signed binary integers may be expressed:**

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1. **Signed magnitude**
2. **One's complement**
3. **Two's complement**

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Signed Magnitude Representation (1)

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- **Allocate the high-order (leftmost) bit to indicate the sign of a number**
 - ▣ The high-order bit is the leftmost bit. It is also called the most significant bit
 - ▣ 0 is used to indicate a positive number; 1 indicates a negative number
- The remaining bits contain the value of the number
- Note that we also **pay attention to the number of bits used** to represent signed binary numbers
 - ▣ i.e. if using 4 bit numbers, then we use 0001_2 rather than 1_2
- In an 8-bit word, signed magnitude representation places the absolute value of the number in the 7 bits to the right of the sign bit

For example:

+3 is: 00000011

- 3 is: 10000011

Signed Magnitude Representation (2)

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- ❑ The "binary addition algorithm" does NOT work with sign-magnitude

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$$0 \ 0 \ 1 \ 1_2 = 3_{10}$$

$$1 \ 1 \ 0 \ 0_2 = -4_{10} \quad \text{https://tutorcs.com}$$

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$$\begin{array}{r} 0 \quad 0 \ 1 \ 1 \\ 1 \ + \ 1 \ 0 \ 0 \\ \hline 1 \quad 1 \ 1 \ 1 \end{array} \text{ this is wrong}$$

Signed Magnitude: intuitive for humans, difficult for computers

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- ❑ Signed magnitude representation is easy for people to understand, but it requires complicated computer hardware

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- ❑ Also it allows two different representations for zero: positive zero and negative zero
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- ❑ As such, computer systems employ **complement systems** for signed number representation

Signed Integer Representation

Complement Systems

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- In binary systems, these are:
 - **One's Complement.** To represent **negative** values, **invert all the bits** in the binary representation of the number (swapping 0s for 1s and vice versa)
 - 1 becomes 0 and 0 becomes 1
 - To represent **positive** numbers no change is applied

For example, using 8-bit one's complement representation

+ 3 is: 00000011

- 3 is: 11111100

More examples

$X=11011100$, $1C(X)=00100011$

$X=1011$, $1C(X)=?$

- One's complement still has the disadvantage of having two different representations for zero: positive zero and negative zero
- In addition positive and negative integers need to be processed separately
- Two's complement solves this problem
- **Two's complement**
 - One's Complement add 1

Signed Integer Representation

Two's Complement

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Two's complement $2C(X)$

- ❑ You represent **positive** numbers, just like the unsigned numbers
- ❑ To represent **negative** numbers start with the corresponding positive number, invert all the bits. Then add 1
- ❑ For example, using 8-bit two's complement representation:

+ 3 is: 00000011

11111100

+ 1

- 3 is: 11111101

1. Start with positive number

2. Invert bits

3. Add 1

-3 in 8-bit Two's Complement Representation is 11111101

- ✓ **Negative numbers must always start with '1'**
- ✓ **Both positive and negative numbers must have the same number of bits**

Floating-Point Representation (1)

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- To represent real numbers with fractional values, floating-point representation is used
- Floating-point numbers are often expressed in scientific notation
 - ▣ For example: $0.125 = 1.25 \times 10^{-1}$
- Remember that when a number is **multiplied by its base**, e.g., 10, then we add a zero or we move the ',' by one position to the right
 - ▣ $235 \times 10 = 2350$
 - ▣ $1.345 \times 10 = 13.45$
 - ▣ $110_2 \times 2 = 1100_2$ ($6 \times 2 = 12_{10}$)
 - ▣ $101.11_2 \times 2 = 1011.1$ ($5.75 \times 2 = 11.5_{10}$)

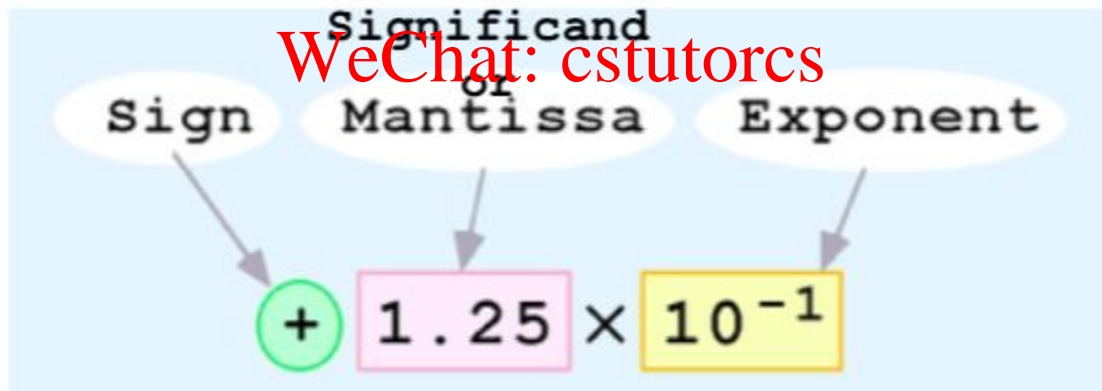
Floating-Point Representation (2)

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- Computers use a form of scientific notation for floating-point representation
 - Single Precision floating point format 32-bit
 - Double Precision floating point format 64-bit
- Numbers written in scientific notation have three components:

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Single precision Floating-Point format (1)

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A binary number is represented in FP format as follows:

1. We write the number using only a single non-zero digit before the radix point :

e.g., $1011010010001 = 1.011010010001 \times 2^{12}$

$1101.10111 = 1.10110111 \times 2^3$

2. Then we transform the number to the following format using 32 bits

$$N = (-1)^S (1+F)(2^{E-127})$$

Sign-S	Exponent-E	Mantissa (fraction) - F
1-bit	8 - bits	23 - bits

S: Sign, 0/1 for positives/negatives, respectively

E: Exponent. $E-127 = \text{exp}$, where exp is the corresponding exponent

F: Significant or Mantissa. We write the fractional part in 23 bits

$E = 127 + \text{exp}$ in order to avoid using negative numbers. $\text{exp} = [-127, 128]$ and therefore $E = [0, 255]$ – 255 needs 8 bits

Single precision Floating-Point format (2)

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Convert the positive number $N=1011010010001$ in Floating point format

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Step1: $1011010010001 = 1.011010010001 \times 2^{12}$

Step2: $N = (-1)^S (1+F)2^E$

$S = 0$ (positive number)

$E - 127 = 12$, and thus $E = 139_{10}$ and $E = 10001011_2$

$F = 011010010001000000000000$

Therefore N in FP format is:

0	10001011	011010010001000000000000
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Single precision Floating-Point format (3)

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Suppose that the 32-bit floating-point representation pattern is the following. Find the binary number

1	10010001	100011100010000000000000
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S is 1 and thus the number is negative

E is 10010001 = 145_{10} , and thus the exponent is $\text{exp} = E - 127 = 145 - 127 = 18$

F = 100011100010000000000000

$$N = (-1)^S (1 + F)(2^{E-127})$$

N is $(-1)^1 \times 1.100011100010000000000000 \times 2^{18}$ or

N = - 11000111000100000000

Floating-Point Representation (1)

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- No matter how many bits we use in a FP representation, the model is finite
 - ▣ The real number system is, of course, infinite, so our models can give nothing more than an approximation of a real value
 - ▣ e.g., how to represent 33.3333333333333333333333?
- At some point, every model breaks down, introducing errors into our calculations
 - ▣ By using a greater number of bits in our model, we can reduce these errors, but we can never totally eliminate them

Why is $0.1 + 0.2$ not equal to 0.3 in most programming languages?

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- computers use a binary floating point format that cannot accurately represent a number like 0.1_{10}
- 0.1_{10} is already rounded to the nearest number in that format
- 0.1_{10} doesn't exist in the FP representation
- 0.1_{10} is already rounded to the nearest number in that format, which results in a small rounding error
- This means that 0.1_{10} is converted to a binary number that's just very close to 0.1_{10}
- The error is tiny since 0.1_{10} is
 $0.1000000000000000000055511151231257827$
- The constants 0.2_{10} and 0.3_{10} are also approximations to their true values
- So, $0.1_{10} + 0.2_{10} == 0.3000000000000000000044408920985006_{10}$

Character Codes

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- So far, we have learnt how to represent numbers. How about text?
- To represent text characters, we use character codes
 - ▣ Essentially, we assign a number for each character we want to represent
- As computers have evolved, character codes have evolved. Larger computer memories and storage devices permit richer character codes
- Some of the character codes are
 1. BCD
 2. ASCII (American Standard Code for Information Interchange) (7 bits)
 3. Extended ASCII (8-bits)
 4. Unicode
 5. and others
- A binary number of n bits gives 2^n different codes
 - ▣ For $n=2$ there are $2^2=4$ different codes, i.e., bit combinations {00, 01, 10, 11}

Binary Coded Decimal (BCD) code

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- when numbers, letters or words are represented by a specific group of symbols, it is said that the number, letter or word is being encoded. The group of symbols is called as a code

- **Binary Coded Decimal (BCD) code**

- ▣ In this code each decimal digit is represented by a 4-bit binary number
- ▣ BCD is a way to express each of the decimal digits with a binary code
- ▣ In the BCD, with four bits we can represent sixteen numbers (0000 to 1111)

$$256_{10} = 0010\ 0101\ 0110_{\text{BCD}}$$

And vise versa

$$0011\ 1000\ 1001_{\text{BCD}} = 389_{10}$$

ASCII Code

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- The most widely accepted code is called the American Standard Code for Information Interchange (ASCII).
- The ASCII code associates an integer value for each symbol in the character set, such as letters, digits, punctuation marks, special characters, and control characters
- The ASCII table has 128 characters, with values from 0 through 127. Thus, 7 bits are sufficient to represent a character in ASCII

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ASCII Code

Dec	Hx	Oct	Char	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr
0	0	000	NUL (null)	32	20	040	 	Space	64	40	100	@	@	96	60	140	`	`
1	1	001	SOH (start of heading)	33	21	041	!	!	65	41	101	A	A	97	61	141	a	a
2	2	002	STX (start of text)	34	22	042	"	"	66	42	102	B	B	98	62	142	b	b
3	3	003	ETX (end of text)	35	23	043	#	#	67	43	103	C	C	99	63	143	c	c
4	4	004	EOT (end of transmission)	36	24	044	$	\$	68	44	104	D	D	100	64	144	d	d
5	5	005	ENQ (enquiry)	37	25	045	%	%	69	45	105	E	E	101	65	145	e	e
6	6	006	ACK (acknowledge)	38	26	046	&	&	70	46	106	F	F	102	66	146	f	f
7	7	007	BEL (bell)	39	27	047	'	'	71	47	107	G	G	103	67	147	g	g
8	8	010	BS (backspace)	40	28	050	((72	48	110	H	H	104	68	150	h	h
9	9	011	TAB (horizontal tab)	41	29	051))	73	49	111	I	I	105	69	151	i	i
10	A	012	LF (NL line feed, new line)	42	2A	052	*	*	74	4A	112	J	J	106	6A	152	j	j
11	B	013	VT (vertical tab)	43	2B	053	+	+	75	4B	113	K	K	107	6B	153	k	k
12	C	014	FF (NP form feed, new page)	44	2C	054	,	,	76	4C	114	L	L	108	6C	154	l	l
13	D	015	CR (carriage return)	45	2D	055	-	-	77	4D	115	M	M	109	6D	155	m	m
14	E	016	SO (shift out)	46	2E	056	.	.	78	4E	116	N	N	110	6E	156	n	n
15	F	017	SI (shift in)	47	2F	057	/	/	79	4F	117	O	O	111	6F	157	o	o
16	10	020	DLE (data link escape)	48	30	060	0	0	80	50	120	P	P	112	70	160	p	p
17	11	021	DC1 (device control 1)	49	31	061	1	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	DC2 (device control 2)	50	32	062	2	2	82	52	122	R	R	114	72	162	r	r
19	13	023	DC3 (device control 3)	51	33	063	3	3	83	53	123	S	S	115	73	163	s	s
20	14	024	DC4 (device control 4)	52	34	064	4	4	84	54	124	T	T	116	74	164	t	t
21	15	025	NAK (negative acknowledge)	53	35	065	5	5	85	55	125	U	U	117	75	165	u	u
22	16	026	SYN (synchronous idle)	54	36	066	6	6	86	56	126	V	V	118	76	166	v	v
23	17	027	ETB (end of trans. block)	55	37	067	7	7	87	57	127	W	W	119	77	167	w	w
24	18	030	CAN (cancel)	56	38	070	8	8	88	58	130	X	X	120	78	170	x	x
25	19	031	EM (end of medium)	57	39	071	9	9	89	59	131	Y	Y	121	79	171	y	y
26	1A	032	SUB (substitute)	58	3A	072	:	:	90	5A	132	Z	Z	122	7A	172	z	z
27	1B	033	ESC (escape)	59	3B	073	;	;	91	5B	133	[[123	7B	173	{	{
28	1C	034	FS (file separator)	60	3C	074	<	<	92	5C	134	\	\	124	7C	174	|	
29	1D	035	GS (group separator)	61	3D	075	=	=	93	5D	135]]	125	7D	175	}	}
30	1E	036	RS (record separator)	62	3E	076	>	>	94	5E	136	^	^	126	7E	176	~	~
31	1F	037	US (unit separator)	63	3F	077	?	?	95	5F	137	_	_	127	7F	177		DEL

Extended ASCII Characters

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- ASCII was designed in the 1960s for teleprinters and telegraphy, and some computing
- The number of printable characters was deliberately kept small, to keep teleprinters and line printers inexpensive
- When computers and peripherals standardized on eight-bit bytes, it became obvious that computers and software could handle text that uses 256-character sets at almost no additional cost in programming, and no additional cost for storage
- An eight-bit character set (using one byte per character) encodes 256 characters, so it can include ASCII plus 128 more characters
- The extra characters represent characters from foreign languages and special symbols for drawing pictures

A set of codes that extends the basic ASCII set. The extended ASCII character set uses 8 bits, which gives it an additional 128 characters

128	Ç	144	É	160	á	176	⌘	192	Ł	208	⌚	224	α	240	≡
129	ü	145	æ	161	í	177	⌘	193	ł	209	⌚	225	β	241	±
130	é	146	Æ	162	ó	178	⌘	194	ŧ	210	π	226	Γ	242	≥
131	â	147	ô	163	û	179		195	ƚ	211	⌚	227	π	243	≤
132	ä	148	ö	164	ñ	180	‡	196	—	212	⌚	228	Σ	244	∫
133	à	149	ò	165	ñ	181	‡	197	ƚ	213	⌚	229	σ	245	∫
134	â	150	û	166	²	182	‡	198	ƚ	214	π	230	μ	246	÷
135	ç	151	ù	167	³	183	‡	199	⌚	215	‡	231	τ	247	≈
136	ê	152	ÿ	168	¿	184	‡	200	⌚	216	‡	232	Φ	248	°
137	ë	153	Ö	169	¿	185	‡	201	ƚ	217	ƚ	233	⊕	249	.
138	è	154	Ü	170	¬	186	‡	202	⌚	218	ƚ	234	Ω	250	.
139	ï	155	©	171	½	187	‡	203	ƚ	219	■	235	δ	251	√
140	î	156	£	172	¾	188	‡	204	‡	220	■	236	∞	252	∞
141	ì	157	¥	173	¡	189	‡	205	=	221	■	237	φ	253	²
142	Ä	158	£	174	«	190	‡	206	‡	222	■	238	ε	254	■
143	Å	159	ƒ	175	»	191	‡	207	⌚	223	■	239	∩	255	

Source: www.LookupTables.com

UNICODE

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- Many of today's systems embrace Unicode that can encode the characters of every language in the world
 - ▣ The Java programming language, and some operating systems now use Unicode as their default character code
 - UTF-8 (8-bits: essentially the extended ASCII Table)
 - UTF-16 (16 bits: Most spoken languages in the world, widely used)
 - UTF-32 (32 bits: includes past languages, space inefficient)

Any questions?

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