

Монгол Улсын Их Сургууль

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“Компьютерийн зохион байгуулалт ба архитектур” хичээлийн 1-р лабораторийн тайлан

“Программ хангамж” хөтөлбөрийн 2-р түвшний оюутан:

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2025 он

Lab 1

2-2 Binary numbers)

5) a. $11_2 = 3$ f. $1100_2 = 12$

b. $100_2 = 4$ g. $1011_2 = 11$

c. $111_2 = 7$ h. $1111_2 = 15$

d. $1000_2 = 8$

e. $1001_2 = 9$

6) a. $1110_2 = 14$ e. $10101_2 = 21$

b. $1010_2 = 10$ f. $11101_2 = 16 + 8 + 4 + 1 = 29$

c. $11100_2 = 28$ g. $10111_2 = 16 + 4 + 2 + 1 = 23$

d. $10000_2 = 16$ h. $11111_2 = 16 + 8 + 4 + 2 + 1 = 31$

7) a. $110011.11_2 = 32 + 16 + 2 + 1 + 0.5 + 0.25 = 51.75$

b. $101010.01_2 = 32 + 8 + 2 + 0.25 = 42.25$

c. $1000001.111 = 64 + 1 + 0.5 + 0.25 + 0.125 = 65.875$

d. $111000.101 = 64 + 32 + 16 + 8 + 0.5 + 0.125 = 120.625$

e. $1011100.10101 = 64 + 16 + 8 + 4 + 0.5 + 0.125 + 0.03125 = 92.65625$

f. $1110001.0001 = 64 + 32 + 16 + 1 + 0.0625 = 113.0625$

g. $1011010.1010_2 = 64 + 16 + 8 + 2 + 0.5 + 0.0625 =$
 $= 90.5625$

h. $111111.1111_2 = 64 + 32 + 16 + 8 + 4 + 2 + 1 + 0.5 + 0.25 +$
 $+ 0.125 + 0.0625 + 0.03125 = 127.96875$

8) Овогдөн тооны 2-мн илэрүүдтэ илэрүүлэгдэ
 хамгийн их 10-мн тоо

- (a) 2 - 3
- (b) 3 - 7
- (c) 4 - 15
- (d) 5 - 31
- (e) 6 - 63
- (f) 7 - 127
- (g) 8 - 255
- (h) 9 - 511
- (i) 10 - 1023
- (j) 11 - 2047

9) Дараах тоонуудыг дүгнэнэ эхн сум

- (a) 17 - 5 сум
- (b) 35 - 6 сум
- (c) 49 - 6 сум
- (d) 63 - 7 сум
- (e) 81 - 7 сум
- (f) 114 - 7 сум
- (g) 132 - 8 сум
- (h) 205 - 8 сум

? 10) Generate the binary sequence for each decimal sequence

(a) $0 \rightarrow 7$ $0000 \rightarrow 0110$

(b) $8 \rightarrow 15$ $1000 \rightarrow 1110$

(c) $16 \rightarrow 31$ $10000 \rightarrow 11110$

(d) $32 \rightarrow 63$ $100000 \rightarrow 111110$

(e) $64 \rightarrow 75$ $1000000 \rightarrow 1001101$

2-3 Decimal to Binary conversion

11) (a) $10 = 2^3 + 2^1 = 1010$

(b) $17 = 2^4 + 2^0 = 10001$

(c) $24 = 2^4 + 2^3 = 11000$

(d) $49 = 2^5 + 2^4 = 110001$

(e) $61 = 2^5 + 2^4 + 2^3 + 2^2 + 2^0 = 111101$

(f) $93 = 2^6 + 2^4 + 2^3 + 2^2 + 2^0 = 1011101$

(g) $125 = 2^6 + 2^5 + 2^4 + 2^1 + 2^2 + 2^0 = 1111101$

(h) $186 = 2^7 + 2^5 + 2^4 + 2^3 + 2^1 = 10111010$

12) (a) $0.32 = 0.25 + 0.0625 = 0.0101$

(b) $0.246 =$

(c) $0.0981 =$

13) (a)
$$\begin{array}{r} 15 \overline{) 2} \\ \underline{14} 7 2 \\ 1 6 3 2 \\ 1 2 1 2 \\ \phantom{} 1 2 1 2 \\ \phantom{\phantom{}} 1 2 1 2 \\ \phantom{\phantom{\phantom{}}} 1 2 1 2 \end{array}$$

$15 = 1111_2$

(b)
$$\begin{array}{r} 21 \overline{) 2} \\ 20 \quad 10 \overline{) 2} \\ \underline{1} \quad 10 \quad 5 \overline{) 2} \\ \quad \quad 0 \quad 4 \quad 2 \overline{) 2} \\ \quad \quad \quad 1 \quad 0 \end{array}$$
 $21 = 10101_2$

(c)
$$\begin{array}{r} 28 \overline{) 2} \\ 27 \quad 14 \overline{) 2} \\ \underline{0} \quad 14 \quad 7 \overline{) 2} \\ \quad \quad 0 \quad 6 \quad 3 \overline{) 2} \\ \quad \quad \quad 1 \quad 2 \quad 1 \overline{) 2} \\ \quad \quad \quad \quad 1 \quad 1 \quad 0 \end{array}$$
 $28 = 11100_2$

(d)
$$\begin{array}{r} 34 \overline{) 2} \\ 34 \quad 17 \overline{) 2} \\ \underline{0} \quad 16 \quad 8 \overline{) 2} \\ \quad \quad 1 \quad 8 \quad 4 \overline{) 2} \\ \quad \quad \quad 0 \quad 4 \quad 2 \overline{) 2} \\ \quad \quad \quad \quad 0 \quad 2 \quad 1 \end{array}$$
 $34 = 100010_2$

(e)
$$\begin{array}{r} 40 \overline{) 2} \\ 40 \quad 20 \overline{) 2} \\ \underline{0} \quad 20 \quad 10 \overline{) 2} \\ \quad \quad 0 \quad 10 \quad 5 \overline{) 2} \\ \quad \quad \quad 0 \quad 4 \quad 2 \overline{) 2} \\ \quad \quad \quad \quad 1 \quad 2 \quad 1 \end{array}$$
 $40 = 101000_2$

(f)
$$\begin{array}{r} 59 \overline{) 2} \\ 58 \quad 29 \overline{) 2} \\ \underline{1} \quad 28 \quad 14 \overline{) 2} \\ \quad \quad 1 \quad 14 \quad 7 \overline{) 2} \\ \quad \quad \quad 0 \quad 6 \quad 3 \overline{) 2} \\ \quad \quad \quad \quad 1 \quad 2 \quad 1 \end{array}$$
 $59 = 111011_2$

$$\begin{array}{r}
 (g) \quad 65 \overline{) 2} \\
 \underline{64} \quad 32 \overline{) 2} \\
 1 \quad 16 \overline{) 2} \\
 \quad 0 \quad 8 \overline{) 2} \\
 \quad \quad 0 \quad 4 \overline{) 2} \\
 \quad \quad \quad 0 \quad 2 \overline{) 2} \\
 \quad \quad \quad \quad 0 \quad 1
 \end{array}$$

$$65 = 1000001_2$$

$$\begin{array}{r}
 (h) \quad 73 \overline{) 2} \\
 \underline{72} \quad 36 \overline{) 2} \\
 1 \quad 18 \overline{) 2} \\
 \quad 0 \quad 9 \overline{) 2} \\
 \quad \quad 0 \quad 4 \overline{) 2} \\
 \quad \quad \quad 0 \quad 2 \overline{) 2} \\
 \quad \quad \quad \quad 0 \quad 1
 \end{array}$$

$$73 = 1001001_2$$

14) (a)

$$\begin{array}{ll}
 0.98 \cdot 2 = 1.96 & (1) \\
 0.96 \cdot 2 = 1.92 & (1) \\
 0.92 \cdot 2 = 1.84 & (1) \\
 0.84 \cdot 2 = 1.68 & (1) \\
 0.68 \cdot 2 = 1.36 & (1) \\
 0.36 \cdot 2 = 0.72 & (0) \\
 0.72 \cdot 2 = 1.44 & (1) \\
 0.44 \cdot 2 = 0.88 & (0) \\
 0.88 \cdot 2 = 1.76 & (1) \\
 0.76 \cdot 2 = 1.52 & (1) \\
 0.52 \cdot 2 = 1.04 & (1)
 \end{array}$$

$$0.98 = 0.1111101011$$

(b)

$$\begin{array}{ll}
 0.347 \cdot 2 = 0.694 & (0) \\
 0.694 \cdot 2 = 1.388 & (1) \\
 0.388 \cdot 2 = 0.776 & (0) \\
 0.776 \cdot 2 = 1.552 & (1) \\
 0.552 \cdot 2 = 1.104 & (1) \\
 0.104 \cdot 2 = 0.208 & (0) \\
 0.208 \cdot 2 = 0.416 & (0) \\
 0.416 \cdot 2 = 0.832 & (0) \\
 0.832 \cdot 2 = 1.664 & (1)
 \end{array}$$

$$0.347 = 0.010110001$$

(c) $0.9028 \cdot 2 = 1.8056$ (1)
 $0.8056 \cdot 2 = 1.6112$ (1)
 $0.6112 \cdot 2 = 1.2224$ (1)
 $0.2224 \cdot 2 = 0.4448$ = 0
 $0.4448 \cdot 2 = 0.8896$ = 0
 $0.8896 \cdot 2 = 1.7792$ = 1
 $0.7792 \cdot 2 = 1.5584$ = 1
 $0.5584 \cdot 2 = 1.1168$ = 1

$0.9028 = 0.11100111_2$

2-4 Binary arithmetic

15) (a) $11 + 01 = 100$
 (b) $10 + 10 = 100$
 (c) $101 + 11 = 1000$
 (d) $111 + 110 = 1001$
 (e) $1001 + 101 = 1110$
 (f) $1101 + 1011 = 10000$

16) (a) $11 - 1 = 10$
 (b) $101 - 100 = 1$
 (c) $110 - 101 = 1$
 (d) $1110 - 11 = 001010$
 (e) $1100 - 1001 = 0011$
 (f) $11010 - 10111 = 00011$

17) (a) $11 \times 11 = 1001$
 (b) $100 \times 10 = 1000$
 (c) $111 \times 101 = 100011$
 (d) $1001 \times 110 = 110110$
 (e) $1101 \times 1101 = 10101001$
 (f) $1110 \times 1101 = 10110110$

18) (a) $100 : 10 = 10$
 (b) $1001 : 11 = 11$
 (c) $1100 : 100 = 11$

2-5 1's and 2's complements

1's complements

19. (a) 101 - 010
 (b) 110 - 001
 (c) 1010 - 0101
 (d) 11010111 - 00101000
 (e) 1110101 - 0001010
 (f) 00001 - 11110

2's complements

20. (a) 10 - 10
 (b) 111 - 001
 (c) 1001 - 0111
 (d) 1101 - 0011
 (e) 11100 - 00100
 (f) 10011 - 01101
 (g) 10110000 - 01010000
 (h) 00111101 - 11000001

2-6 Signed numbers

8-bit sign-magnitude number

21. (a) +29 - 00011101

(b) -35 - 11010101

(c) +100 - 01100100

(d) -123 - 11111011

22. 8 bit number in the 1's complement form

(a) -34 - 11011101

+34 - 00100010

(b) 57 - 11000110

(c) -99 - 10011100

(d) +115 - 10001100

23) 8 bit number in the 2's complement form

(a) $+12 = 01110100$

(b) $-68 = 10111100$

(c) $101 = 10011011$

(d) $-125 = 10000011$

24) Determine decimal value of each sign-magnitude form

(a) $10011001 = -25$

(b) $01110100 = 116$

(c) $10111111 = -63$

25) Determine decimal value of 1's complement

(a) $10011001 = -128 + 16 + 8 + 1 + 1 = -102$

(b) $01110100 = 64 + 32 + 16 + 4 = 116$

(c) $10111111 = -128 + 32 + 16 + 8 + 4 + 2 + 1 + 1 = -64$

26) Determine decimal value of 2's complement

(a) $10011001 = -128 + 16 + 8 + 1 = -103$

(b) $01110100 = 64 + 32 + 16 + 4 = 116$

(c) $10111111 = -128 + 32 + 16 + 8 + 4 + 2 + 1 = -65$

27) Express sign-magnitude binary to single precision floating point format

(a) $011110000101011 = 1.1110000101011 \cdot 2^{14} =$
 $= 0'10001101'111000010101100000000$

$$(b) 100110000011000 = 1.00110000011000 \cdot 2^{14} \\ = 01000110100110000011000000000000$$

(28)

$$(a) 11000000101001001110001000000000 \\ (-1)^1 (1.01001001110001) (2^{128-127}) = \\ -10.1001001110001$$

$$(b) 01100110010000111101001000000000 \\ (-1)^0 (1.10000111101001) \cdot 2^{104-117} = \\ 1.10000111101001 \cdot 2^{97}$$

2-7 Arithmetic operations with signed numbers

(29) Add using 2's complement form:

a. 33, 15

$$\begin{array}{r} 33 = 00100001 \\ 15 = 00001111 \\ \hline 11011111 \end{array} \quad \begin{array}{r} 11011111 \\ + 11100001 \\ \hline 11010000 \end{array} \quad 11010000 (00110000)$$

b. 56, -27

$$\begin{array}{r} 56 = 00111000 \\ -27 = 10011011 \\ \hline 10010111 \end{array} \quad \begin{array}{r} 11001000 \\ + 01100101 \\ \hline 100101101 \\ + 11001000 \\ \hline 11100101 \\ + 1100101 \\ \hline 100101101 \\ + 00111000 \\ \hline 11100101 \\ \hline 100011101 \end{array} \quad \begin{array}{l} 00101101 (11010010) \\ 10101101 (01010011) \\ (00011101) - 29 \end{array}$$

(c) -46 25

$$\begin{array}{r} 25 = 00011001 \\ -46 = 10101110 \\ \hline 11101011 \end{array} \quad \begin{array}{r} 00011001 \\ + 11010010 \\ \hline 11101011 \end{array} \quad 10010101 \quad (-2^8)$$

(d) -110 -84

$$\begin{array}{r} -110 = 11101110 \\ -84 = 11010100 \\ \hline 10111110 \end{array} \quad \begin{array}{r} 10010010 \\ + 1101100 \\ \hline 10111110 \end{array} \quad \begin{array}{r} 10000000 \\ 00111110 \\ \hline 111000010 \end{array}$$

(d) -110 -84

$$\begin{array}{r} -110 = 11101110 \\ -84 = 11010100 \\ \hline 10011110 \end{array} \quad \begin{array}{r} 10010010 \\ + 10101100 \\ \hline 10011110 \end{array} \quad \begin{array}{r} 11000010 \\ -194 \\ \hline 10011110 \end{array}$$

30) addition in 2's complement form

(a) $00010110 + 00110011 = 01001001$

$$\begin{array}{r} 00010110 \\ + 00110011 \\ \hline 01001001 \end{array}$$

(b) $01110000 + 10101111 = 00011111$

$$\begin{array}{r} 01110000 \\ + 10101111 \\ \hline 00011111 \end{array}$$

$$31) (a) \quad 10001100 + 00111001 = 00101101$$

$$\begin{array}{r} +00111001 \\ 11110100 \\ \hline 110101101 \end{array}$$

$$(b) \quad 11011001 + 11000111 = 11000000$$

$$\begin{array}{r} +01011001 \\ 01100111 \\ \hline 11000000 \end{array}$$

$$32) (a) \quad 00110011 - 00010000 = 00100011$$

$$\begin{array}{r} +00110011 \\ 11110000 \\ \hline 100100011 \end{array}$$

$$(b) \quad 01100101 - 11101000 = 01111101$$

$$\begin{array}{r} +01100101 \\ 00011000 \\ \hline 01111101 \end{array}$$

$$33) \quad 01101010 \cdot 11110001 = 111000110110$$

$$11110001 \rightarrow 00001111$$

$$\begin{array}{r} 1101010 \\ \times 00001111 \\ \hline 1101010 \\ +1101010 \\ \hline 100111110 \\ +1101010 \\ \hline 1011100110 \\ +1101010 \\ \hline 11000110110 \end{array}$$

$$34) 01000100 : 00011001$$

$$\begin{array}{r} 01000100 \\ + 11100111 \\ \hline 00101011 \end{array}$$

$$\begin{array}{r} 00101011 \\ + 11100111 \\ \hline 00010010 \end{array}$$

$$\begin{array}{r} 00010010 \\ + 11100111 \\ \hline 1111001 \end{array}$$

$$\begin{array}{r} 1111001 \\ + 11100111 \\ \hline 11100000 \end{array}$$

$$\begin{array}{r} 11100000 \\ + 11100111 \\ \hline 11000111 \end{array}$$

$$\begin{array}{r} 11000111 \\ + 11100111 \\ \hline 10101110 \end{array}$$

$$\begin{array}{r} 10101110 \\ + 11100111 \\ \hline 10010101 \end{array}$$

$$\begin{array}{r} 10010101 \\ + 11100111 \\ \hline 01111100 \end{array}$$

$$\begin{array}{r} 01111100 \\ + 11100111 \\ \hline 01100011 \end{array}$$

$$\begin{array}{r} 01100011 \\ + 11100111 \\ \hline 01001010 \end{array}$$

$$\begin{array}{r} 01001010 \\ + 11100111 \\ \hline 00110001 \end{array}$$

$$\begin{array}{r} 00110001 \\ + 11100111 \\ \hline 00011000 \end{array}$$

$$00000010$$

2-8 Hexadecimal numbers

$$35) a. 38_{16} = 00111000$$

$$b. 59_{16} = 01011001$$

$$c. A4_{16} = 101000010100$$

$$d. 5C8_{16} = 010111001000$$

$$e. 4100_{16} = 0100000100000000$$

$$f. FB17_{16} = 111101100010111$$

$$g. 8A9D_{16} = 1000101010011101$$

36) a. $1110 = E_{16}$

b. $10 = 2_{16}$

c. $10111 = 17_{16}$

d. $10100110 = A6_{16}$

e. $1111110000 = 3F0_{16}$

f. $100110000010 = 982_{16}$

37) a. $23_{16} = 35$

b. $92_{16} = 146$

c. $1A_{16} = 26$

d. $8D_{16} = 141$

e. $F3_{16} = 243$

f. $EB_{16} = 267$

g. $5C2_{16} = 1474$

h. $700_{16} = 1792$

38) a. $8 = 8$

b. $14 = E$

c. $33 = 24$

d. $52 = 34$

e. $284 = 11C$

f. $2890 = B4A$

g. $4019 = FB3$

h. $6500 = 1964$

39) a. $37_{16} + 29_{16} = 60_{16}$

b. $A0_{16} + 6B_{16} = 10B_{16}$

c. $FF_{16} + BB_{16} = 1BA_{16}$

40) a. $51_{16} - 40_{16} = 11_{16}$

b. $C8_{16} - 3A_{16} = 8E_{16}$

c. $FD_{16} - 8B_{16} = 75_{16}$

2-9 Octal Numbers

- 41)
- a. $12_8 = 10$
 - b. $27_8 = 33$
 - c. $56_8 = 46$
 - d. $64_8 = 52$
 - e. $103_8 = 67$
 - f. $557_8 = 367$
 - g. $163_8 = 115$
 - h. $1024_8 = 532$
 - i. $7765_8 = 4085$

- 42)
- a. $15 = 17_8$

$$\begin{array}{r} 15 \overline{) 8} \\ 8 \\ \hline 0 \end{array}$$
 - b. $27 = 33_8$

$$\begin{array}{r} 27 \overline{) 8} \\ 24 \\ \hline 4 \end{array}$$
 - c. $46 = 56_8$

$$\begin{array}{r} 46 \overline{) 8} \\ 40 \\ \hline 8 \end{array}$$
 - d. $70 = 62_8$

$$\begin{array}{r} 70 \overline{) 8} \\ 48 \\ \hline 22 \end{array}$$
 - e. $100 = 144_8$

$$\begin{array}{r} 100 \overline{) 8} \\ 96 \\ \hline 4 \end{array}$$
 - f. $142 = 216_8$

$$\begin{array}{r} 142 \overline{) 8} \\ 136 \\ \hline 6 \end{array}$$
 - g. $219 = 333_8$

$$\begin{array}{r} 219 \overline{) 8} \\ 216 \\ \hline 3 \end{array}$$
 - h. $435 = 663_8$

$$\begin{array}{r} 435 \overline{) 8} \\ 432 \\ \hline 3 \end{array}$$

- 43)
- a. $13_8 = 001011$
 - b. $57_8 = 161111$
 - c. $101_8 = 001000001$
 - d. $321_8 = 011010001$
 - e. $540_8 = 101100000$
 - f. $4653_8 = 100110101011$
 - g. $13271_8 = 001100010111001$
 - h. $45600_8 = 100101110000000$
 - i. $100213_8 = 001000000010001001$

- 44)
- a) $111_2 = 7_8$
 - b) $10_2 = 2_8$
 - c) $110111_2 = 67_8$
 - d) $101010_2 = 52_8$
 - e) $1100_2 = 14_8$
 - f) $1011110_2 = 136_8$
 - g) $1011100011001_2 = 5431_8$
 - h) $10110000011_2 = 2603_8$
 - i) $111111101111000_2 = 77570_8$

2-10 Binary Coded Decimal (BCD)

45) convert to 8421 BCD:

- | | |
|-------------------|-------------------------|
| a. 10 = 0001 0000 | g. 44 = 0100 0100 |
| b. 13 = 0001 0011 | h. 57 = 0101 0111 |
| c. 18 = 0001 1000 | i. 69 = 0110 1001 |
| d. 21 = 0010 0001 | j. 98 = 1001 1000 |
| e. 25 = 0010 0101 | k. 125 = 0001 0010 0101 |
| f. 36 = 0011 0110 | l. 156 = 0001 0101 0110 |

- 46)
- a. 10 = 1010
 - b. 13 = 1101
 - c. 18 = 10010
 - d. 21 = 10101
 - e. 25 = 11001
 - f. 36 = 100100

- 47)
- a. 104 = 0001 0000 0100
 - b. 128 = 0001 0010 1000
 - c. 132 = 0001 0011 0010
 - d. 150 = 0001 0101 0000
 - e. 126 = 0001 1000 0110
 - f. 210 = 0010 0001 0000
 - g. 359 = 0011 0101 1001
 - h. 547 = 0101 0100 0111

- 48) a) $0001 = 1$
 b) $0110 = 6$
 c) $1001 = 9$
 d) $00011000 = 18$
 e) $00011001 = 19$
 f) $00110010 = 32$
 g) $01000101 = 45$
 h) $10011000 = 98$
 i) $100001110000 = 870$

- 49) a. $10000000 = 86$
 b. $0010'00110111 = 237$
 c. $0011'0100'0110 = 346$
 d. $0100'0010'0001 = 421$
 e. $0111'0101'0100 = 754$

- 50) a. $0010 + 0001 = 0011$
 b. $0101 + 0011 = 1000$
 c. $0111 + 0010 = 1001$
 d. $1000 + 0001 = 1001$

- 51) a. $1000 + 0110 = 1110 = 00010100$
 b. $0111 + 0101 = 1100 = 00010010$
 c. $1001 + 1000 = 10001 = 00010111$
 d. $1001 + 0111 = 10000 = 00010110$

2-11 Digital Codes

53) Gray code allows only a bit difference

- 54) a. $11011 = 10110$
 b. $1001010 = 1101111$
 c. $1111011101110 = 1000110011001$

55. Gray to binary

a. $1010 = 1100$

b. $00010 = 00011$

c. $11000010001 = 10000011110$

58.

1001000	1100101	1101100	1101100	1101111	0101110
0100000	1001000	1101111	1110111	0100000	1100001
1110010	1100101	0100000	1111001	1101111	1110101
0111111					

He mm, Hello - How are you?

